

Multi-Dimensional Data Visualization

Slides courtesy of Chris North

- What is the Cleveland's ranking for quantitative data among the visual variables:
 - Angle, area, length, position, color

Where are we?

- Tabular (multi-dimensional)
 - Spatial & Temporal
 - 1D / 2D
 - 3D
 - Networks
 - Trees
 - Graphs
 - Text & Documents
- ✓ Fundamentals / Eval
 - Navigation strategies
 - Overview strategies
 - Interaction techniques
- Design
- Development
- Evaluation

The Simple Stuff

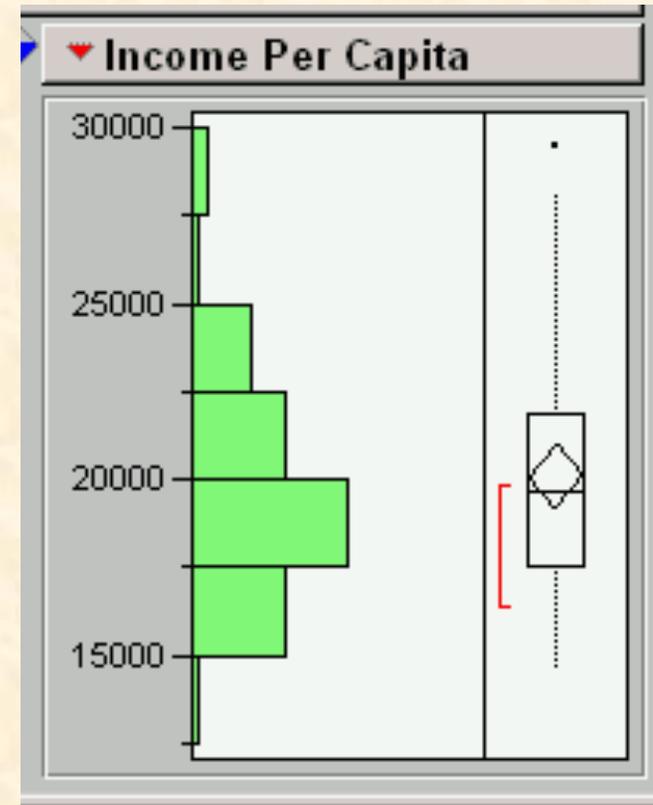
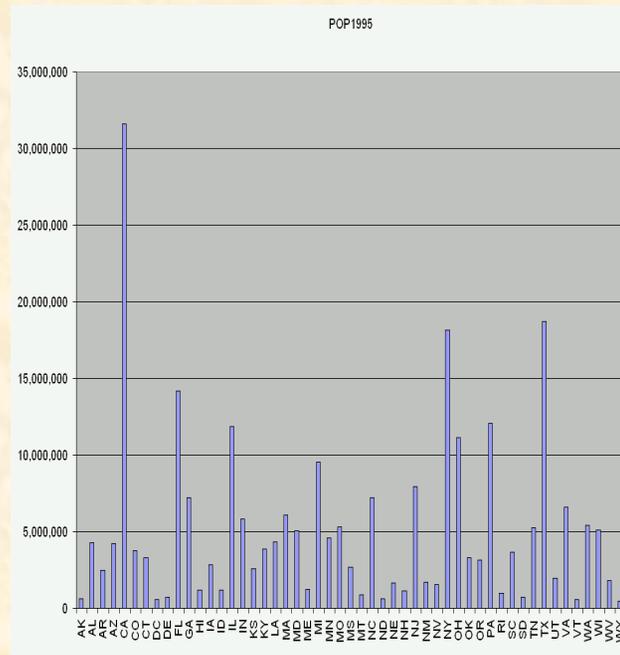
- Univariate
- Bivariate
- Trivariate

The screenshot shows a Microsoft Excel spreadsheet with the following data:

	A	B	C	D	E	F	G	H	I	J
1	Year	Length	Title	Subject	Actor	Actress	Director	Popularity	Awards	*Image
2	integer	integer	string	string	string	string	string	integer	string	string
3	1990	125	Wild at Heart	Drama	Cage, Nicolas	Dem, Laura	Lynch, David	6	No	NicholasCage.gif
4	1961	120	Goodbye Again	Drama	Perkins, Anthon	Bergman, Ingrid	Litvak, Anatole	6	No	NicholasCage.gif
5	1990	135	Hunt for Red Oct	Drama	Connery, Sean		McTiernan, J.	8	No	NicholasCage.gif
6	1984	108	Terminator, The	Action	Schwarzenegge	Hamilton, Linda	Cameron, J.	17	No	T2.gif
7	1991	136	Terminator 2	Action	Schwarzenegge	Hamilton, Linda	Cameron, J.	8	No	T2.gif
8	1993	65	John Cleese on H	Comedy	Cleese, John	Booth, Connie		62	No	NicholasCage.gif
9	1987	103	Au Revoir les Enf	Drama	Manesse, Gasp	Racette, Francis	Malle, Louis	35	No	NicholasCage.gif
10	1983	128	The Ballad of Nar	Drama	Missing	Imamura, Shoh		15	No	NicholasCage.gif
11	1990	138	Cyrano De Berge	Drama	Depardieu, Geri	Brochet, Anne	Rappeneau, Je	86	No	NicholasCage.gif
12	1990	107	Green Card	Comedy	Depardieu, Geri	MacDowell, Anc	Weir, Peter	25	No	NicholasCage.gif
13	1987	118	Hope & Glory	War	Hayman, David	Miles, Sarah	Boorman, John	3	No	NicholasCage.gif
14	1982	122	Missing	Drama	Lemmon, Jack	Spacek, Sissy	Costa-Gavras,	30	No	NicholasCage.gif
15	1986	125	The Mission	Drama	Niro, Robert De	Lunghi, Cherie	Joffe, Roland	20	No	NicholasCage.gif
16	1987	101	My Life As a Dog	Comedy	Glanzelius, Anton		Hallstrom, Lass	21	No	NicholasCage.gif
17	1984	150	Paris, Texas	Drama	Stanton, Harry	Kinski, Nastass	Wim Wenders	27	No	NicholasCage.gif
18	1984	106	Romancing the S	Action	Douglas, Micha	Turner, Kathleen	Silvestri, Rober	83	No	NicholasCage.gif
19	1982	120	The State of Thin	Drama		Isabelle Weinga	Wenders, Wim	40	No	NicholasCage.gif
20	1986	98	Summer	Comedy	Gauthier, Vince	Riviere, Marie	Rohmer, Eric	11	No	NicholasCage.gif
21	1955	108	Smiles of a Sumr	Comedy	Bjornstrand, Gu	Jacobsson, Ulla	Bergman, Ingm	58	No	Bergman.gif
22	1987	98	Under the Sun of	Drama	Depardieu, Geri	Bonnaire, Sandi	Pialat, Maurice	45	No	NicholasCage.gif
23	1985	105	Vagabond	Drama	Meril, Macha	Bonnaire, Sandi	Varda, Agnes	49	No	NicholasCage.gif
24	1988	115	Working Girl	Comedy	Ford, Harrison	Griffith, Melanie	Nichols, Mike	25	No	NicholasCage.gif
25	1984	106	A Year of the Qui	Drama	Wilson, Scott	Komorowska, M	Zanussi, Krzys	78	No	NicholasCage.gif
26	1983	134	Yentl	Music	Patinkin, Mand	Streisand, Barb	Streisand, Barb	46	No	NicholasCage.gif
27	1982	111	Yol	Drama	Akan, Tarik		Guney, Yilmaz	53	No	NicholasCage.gif
28	1992	102	The Addams Farr	Comedy	Julia, Raul	Huston, Anjelic	Sonnenfeld, B.	8	No	NicholasCage.gif
29	1992	88	Adventures in Din	Action	Katz, Omri	Hoffman, Shaw	Thompson, Bre	19	No	NicholasCage.gif
30	1992	95	Alan & Naomi	Drama	Haas, Lukas	Aquino, Vanessa	Vanwageningen, S	3	No	NicholasCage.gif

Univariate

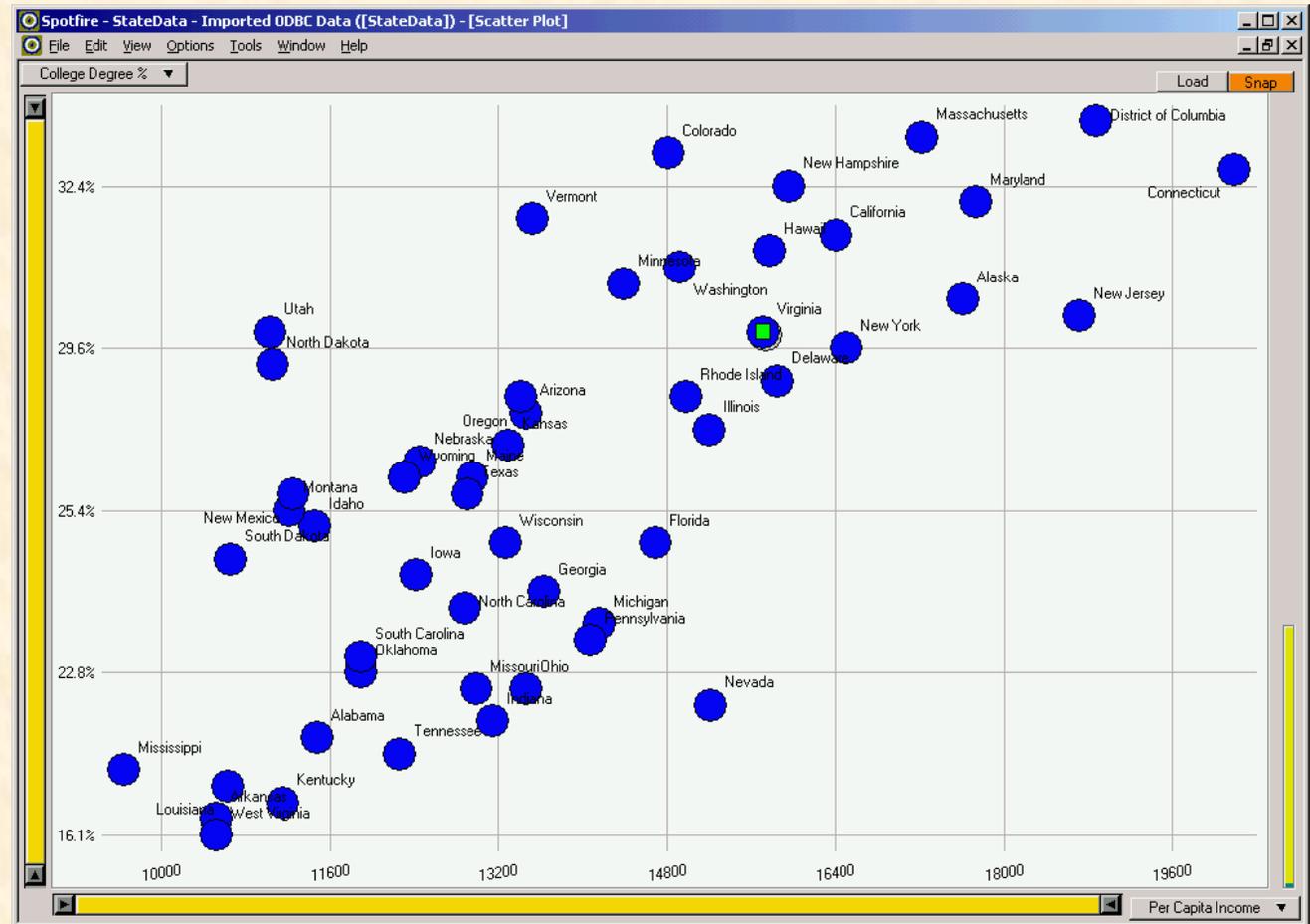
- Dot plot
- Bar chart (item vs. attribute)
- Tukey box plot
- Histogram



Bivariate

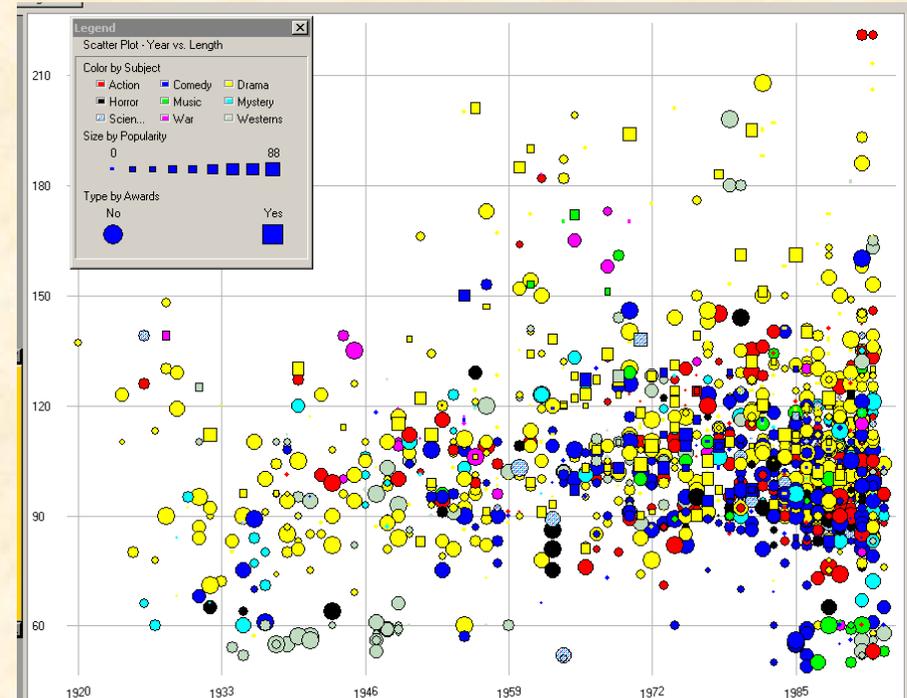
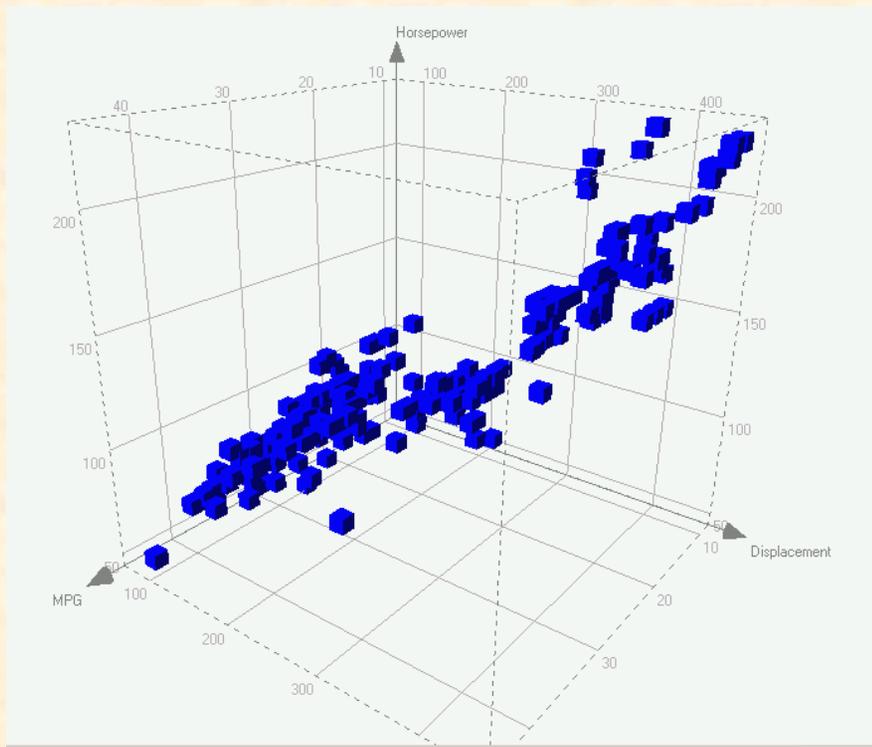
- Scatterplot

-



Trivariate

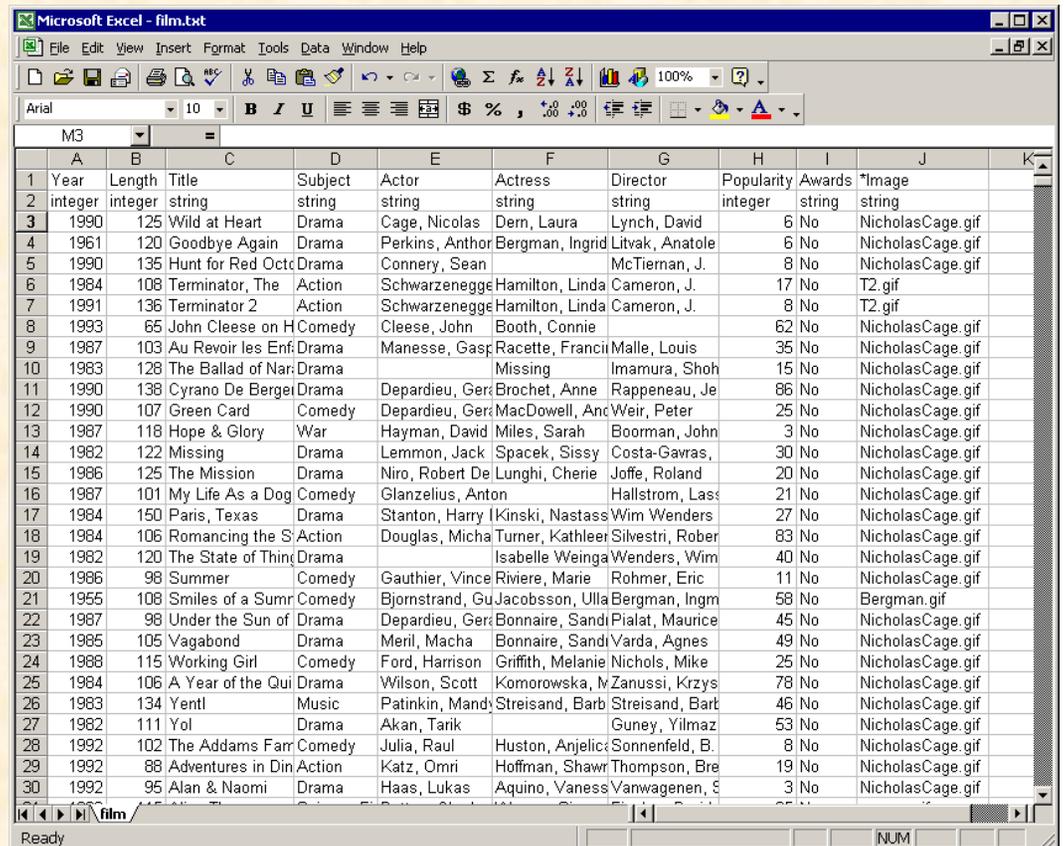
- 3D scatterplot, spin plot
- 2D plot + size (or color...)



Multi-Dimensional Data

- Each attribute defines a dimension
- Small # of dimensions easy
 - Data mapping, Cleveland's rules
- What about **many** dimensional data? n-D

What does 10-D space look like?



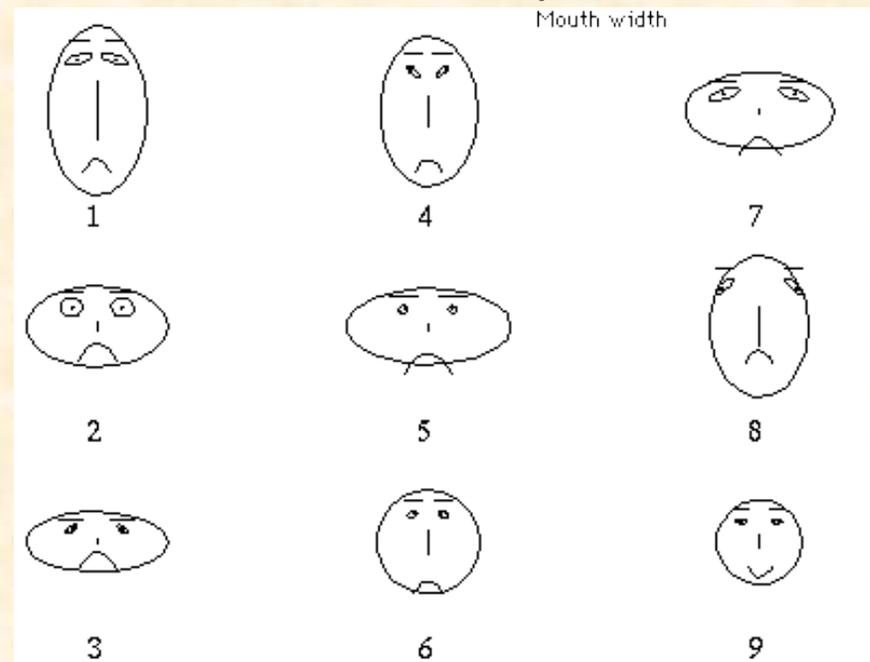
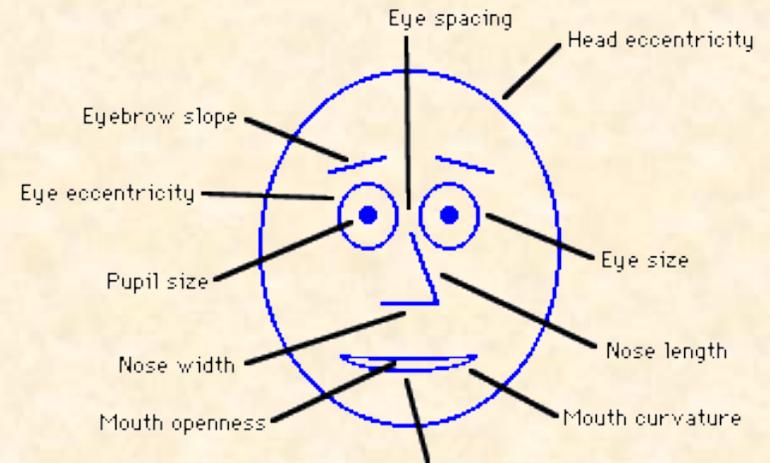
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Map n-D space onto 2-D screen

- Visual representations:
 - Complex glyphs
 - E.g. star glyphs, faces, embedded visualization, ...
 - Multiple views
 - E.g. plot matrices, brushing histograms, Spotfire, ...
 - Non-orthogonal axes
 - E.g. Parallel coords, star coords, ...
 - Tabular layout
 - E.g. TableLens, ...
- Interactions:
 - Dynamic Queries
 - Brushing & Linking
 - Selecting for details, ...

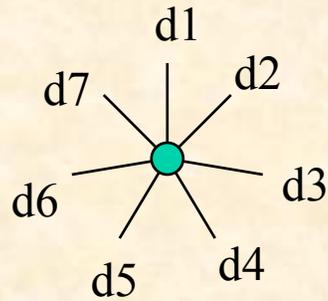
Glyphs: Chernoff Faces

- 10 Parameters:
 - Head Eccentricity
 - Eye Eccentricity
 - Pupil Size
 - Eyebrow Slope
 - Nose Size
 - Mouth Vertical Offset
 - Eye Spacing
 - Eye Size
 - Mouth Width
 - Mouth Openness



- <http://hesketh.com/schampeo/projects/Faces/chernoff.html>

Glyphs: Stars



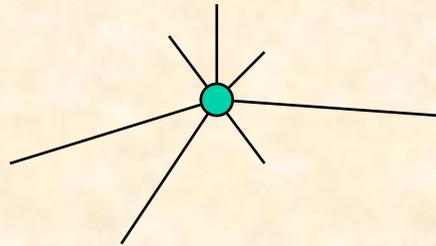
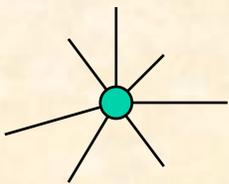
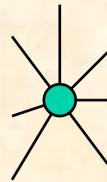
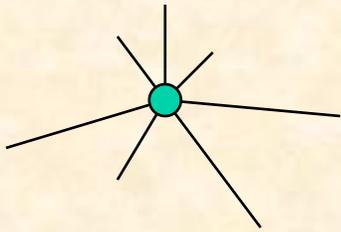
Evaluation of Alternative Glyph Designs for Time Series Data in a Small Multiple Setting

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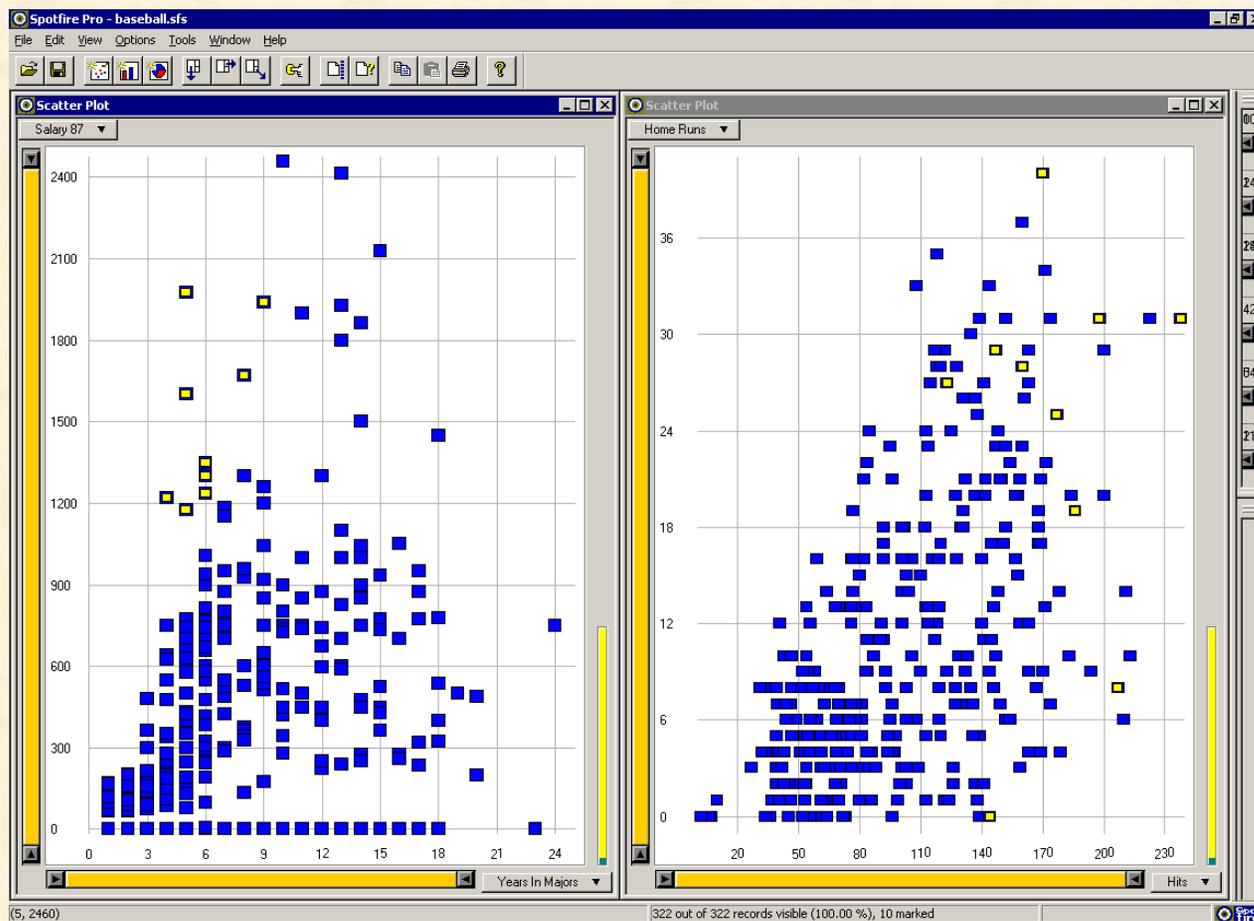
Petra Isenberg³
³INRIA
petra.isenberg@inria.fr

[http://hal.inria.fr/docs/00/78/15/04/
PDF/Fuchs_2013_EOA.pdf](http://hal.inria.fr/docs/00/78/15/04/PDF/Fuchs_2013_EOA.pdf)



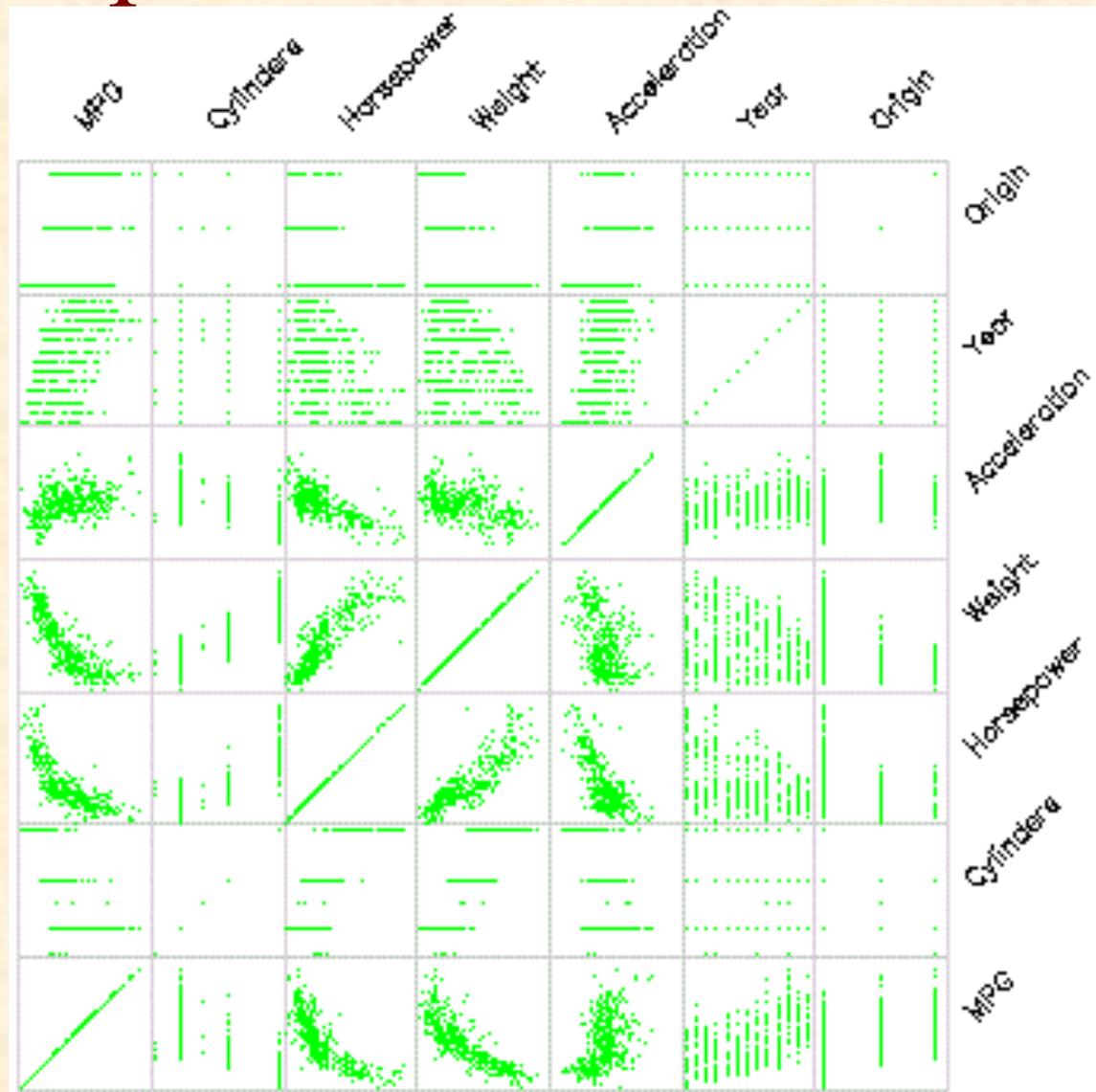
Multiple Views with Brushing-and-linking

Robert Kosara: brush and linking, Parallel Coordinates:
<http://vimeo.com/13437693>



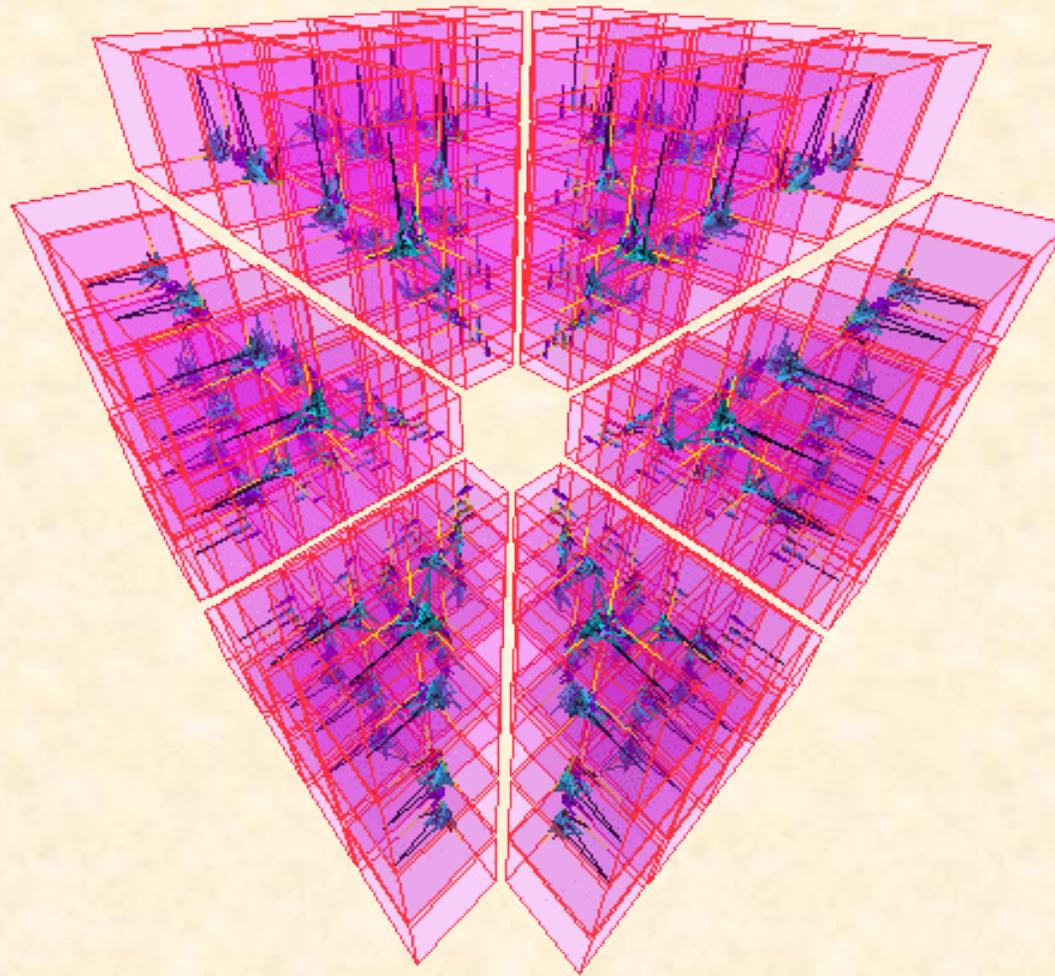
Scatterplot Matrix

- All pairs of attributes
- Brushing and linking



- <http://noppa5.pc.helsinki.fi/koe/3d3.html>

... on steroids

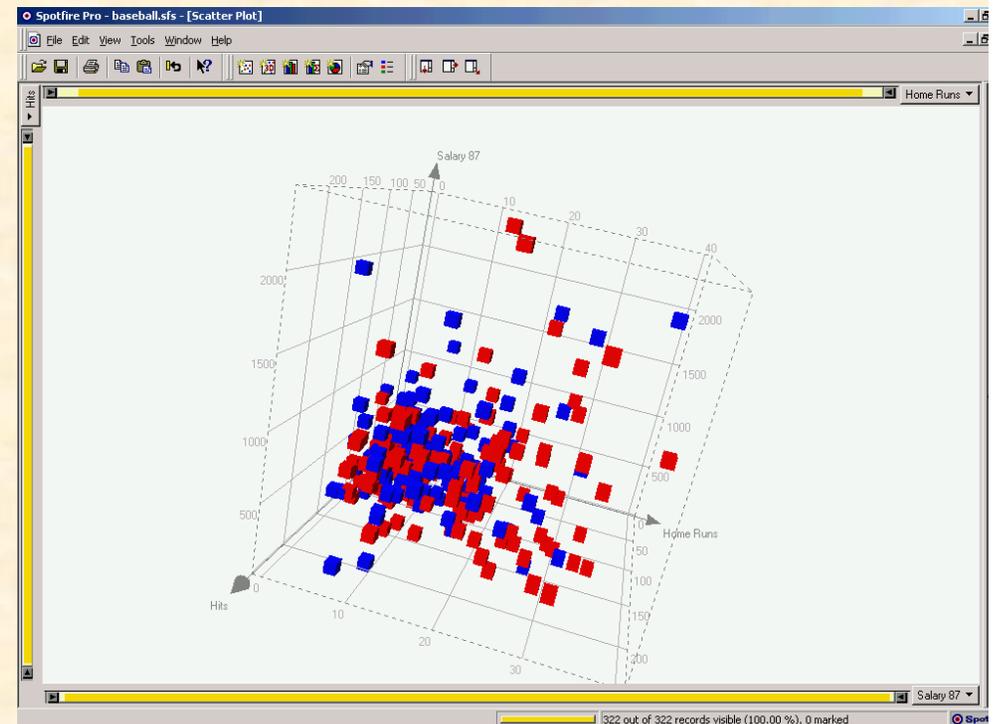


Different Arrangements of Axes

- Axes are good
 - Lays out all points in a single space
 - “position” is 1st in Cleveland’s rules
 - Uniform treatment of dimensions

- Space > 3D ?

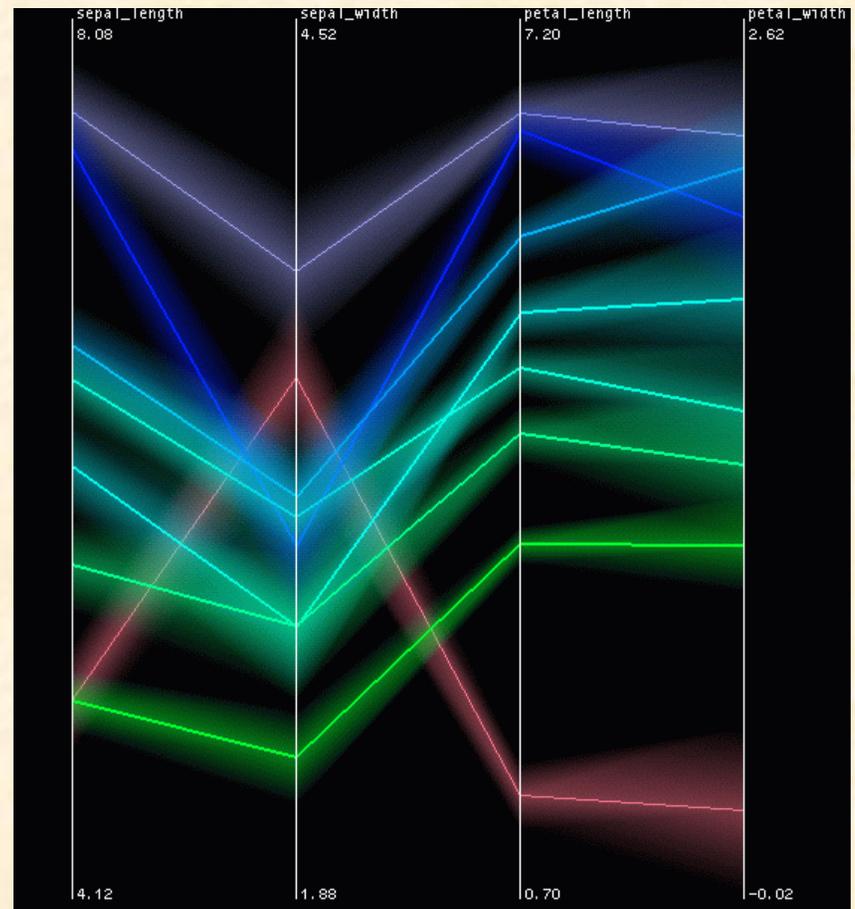
- Must trash orthogonality



Parallel Coordinates

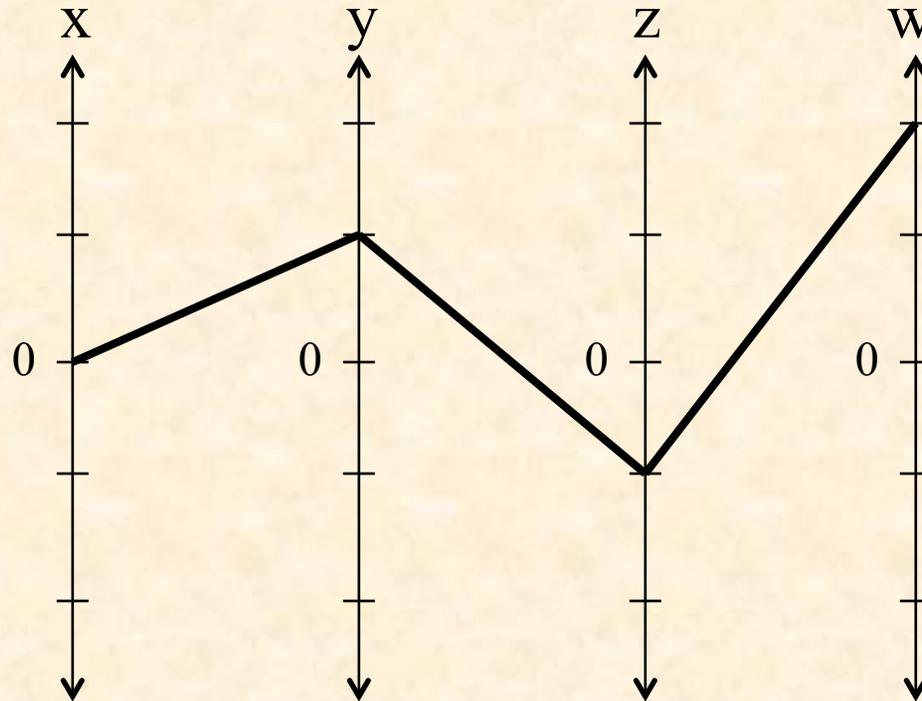
- Inselberg, “Multidimensional detective”
(parallel coordinates)

-

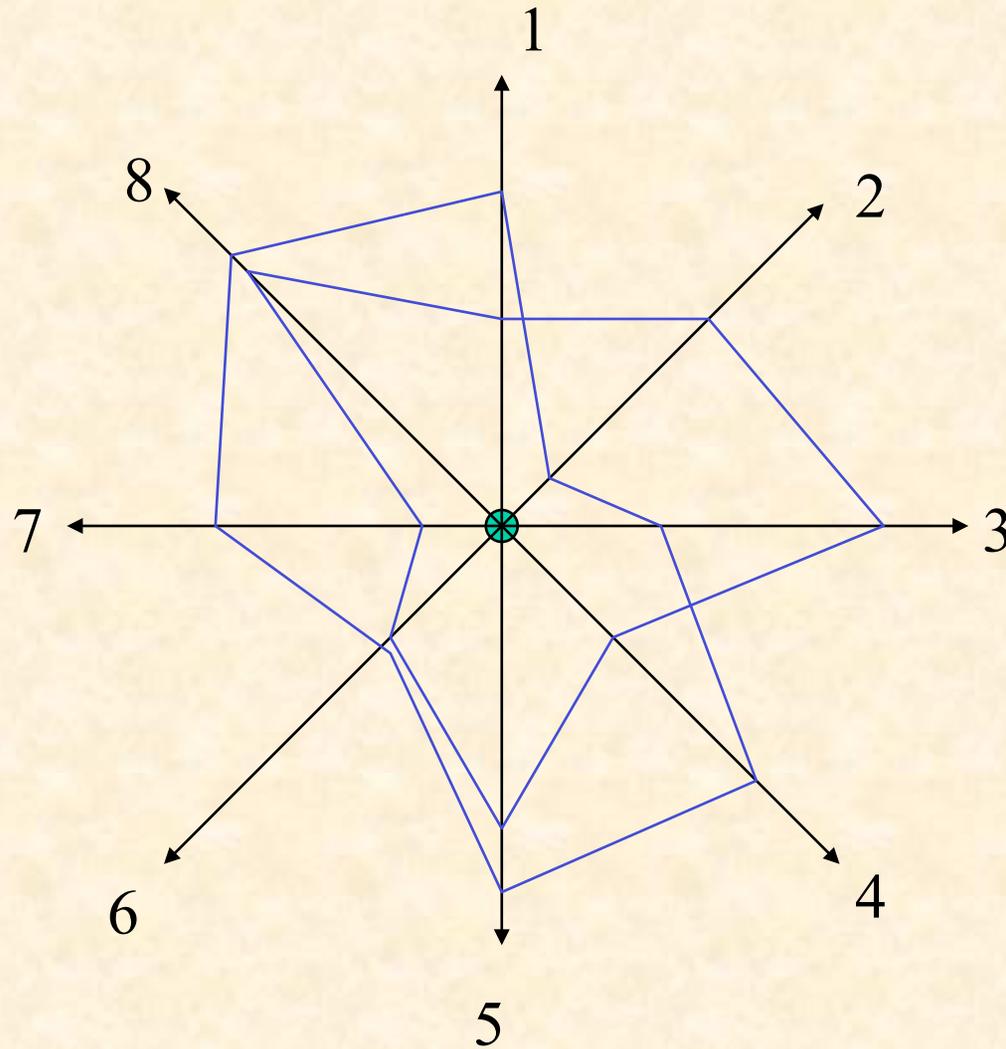


Parallel Coordinates

- Forget about Cartesian orthogonal axes
- $(0,1,-1,2)=$



Star Plot

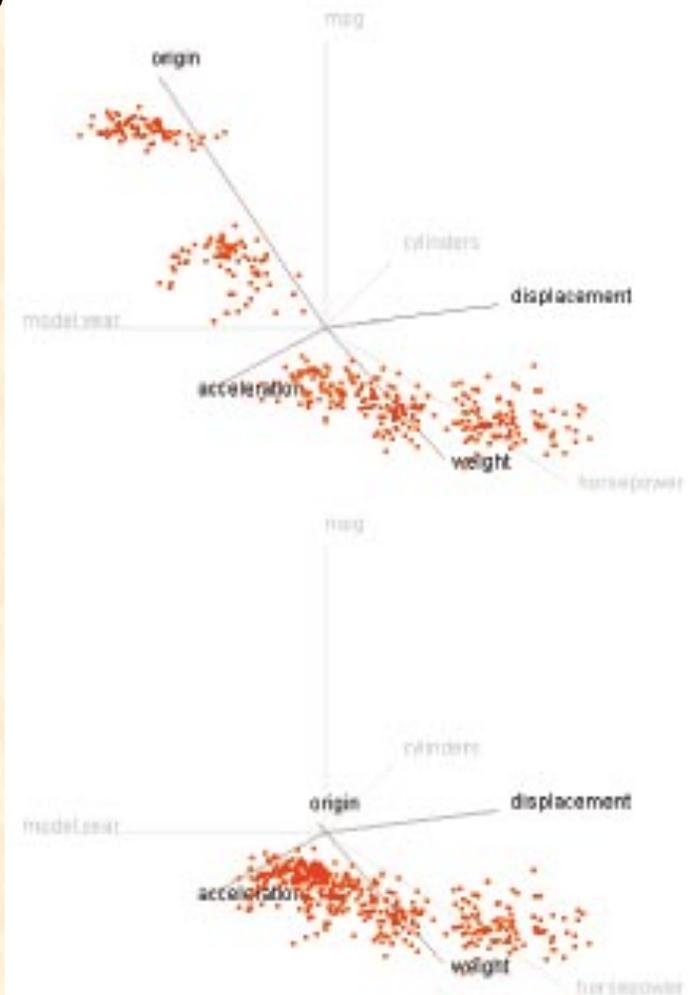


Parallel Coordinates with axes arranged radially

Star Coordinates

- Kandogan, “Star Coordinates”

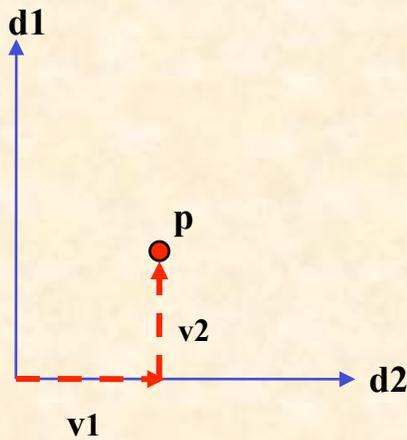
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Star Coordinates

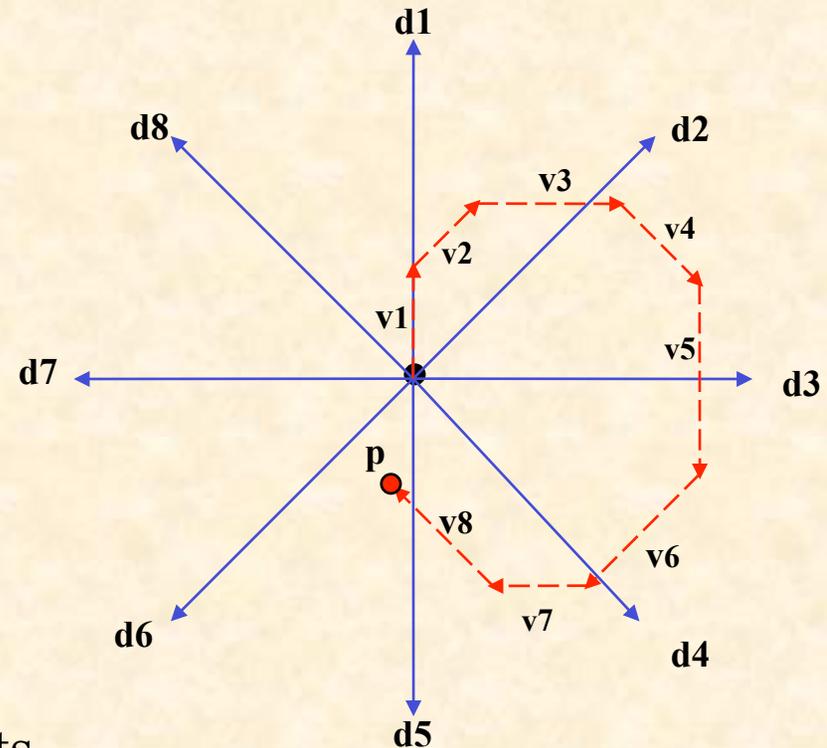
Cartesian

$$P=(v_1, v_2)$$



Star Coordinates

$$P=(v_1, v_2, v_3, v_4, v_5, v_6, v_7, v_8)$$



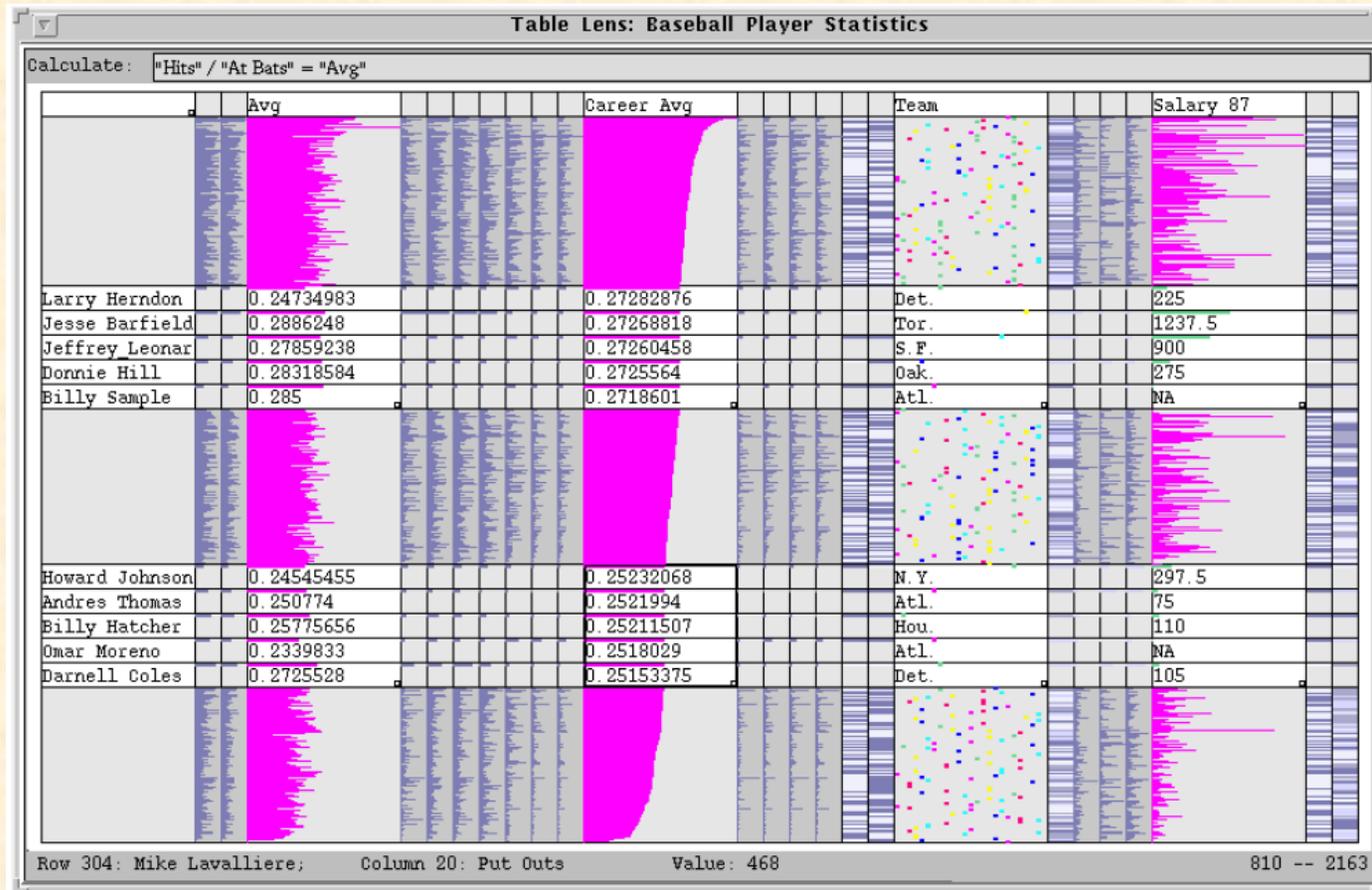
Mapping:

- Items \rightarrow dots
- Σ attribute vectors \rightarrow (x,y)

Analysis

Table Lens

- Rao, “Table Lens” <http://www.ramanarao.com/papers/tablelens-chi94.pdf>



FOCUS / InfoZoom

- Spenke, “FOCUS”
 - Finding correlations between the measurements and the occurrence of a thrombosis

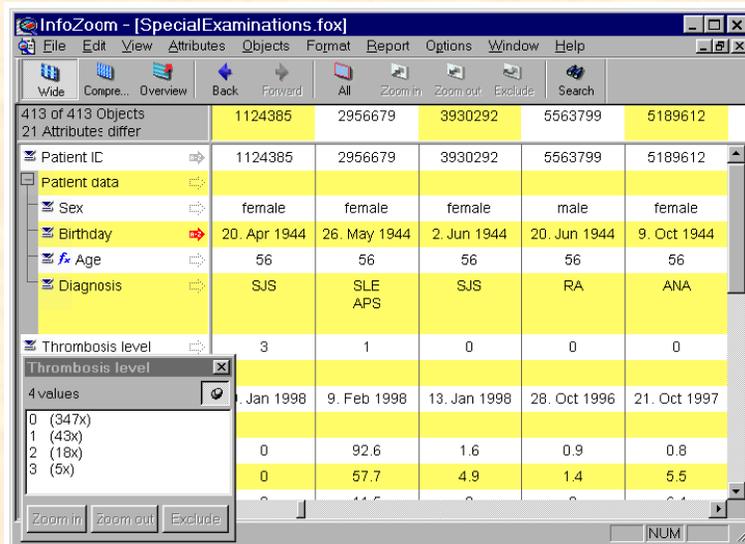
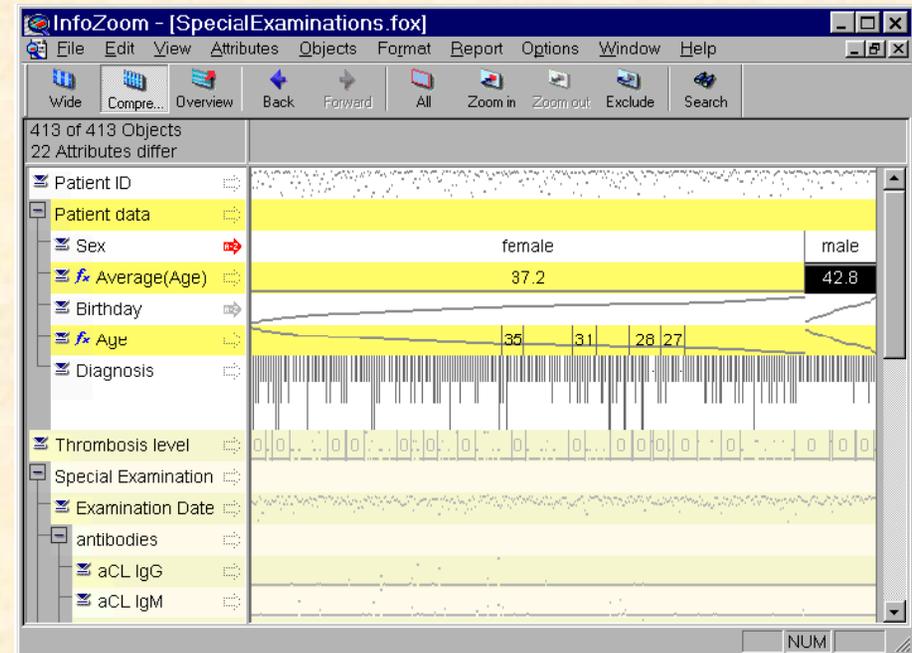


Figure 1: Wide Table Mode



Visualization and Interactive Analysis of Blood Parameters with InfoZoom

Michael Spenke

GMD — German National Research Center for Information Technology
FIT — Institute for Applied Information Technology, <http://www.gmd.de/fit>

VisDB & Pixel Bar Charts

- Keim, “VisDB”

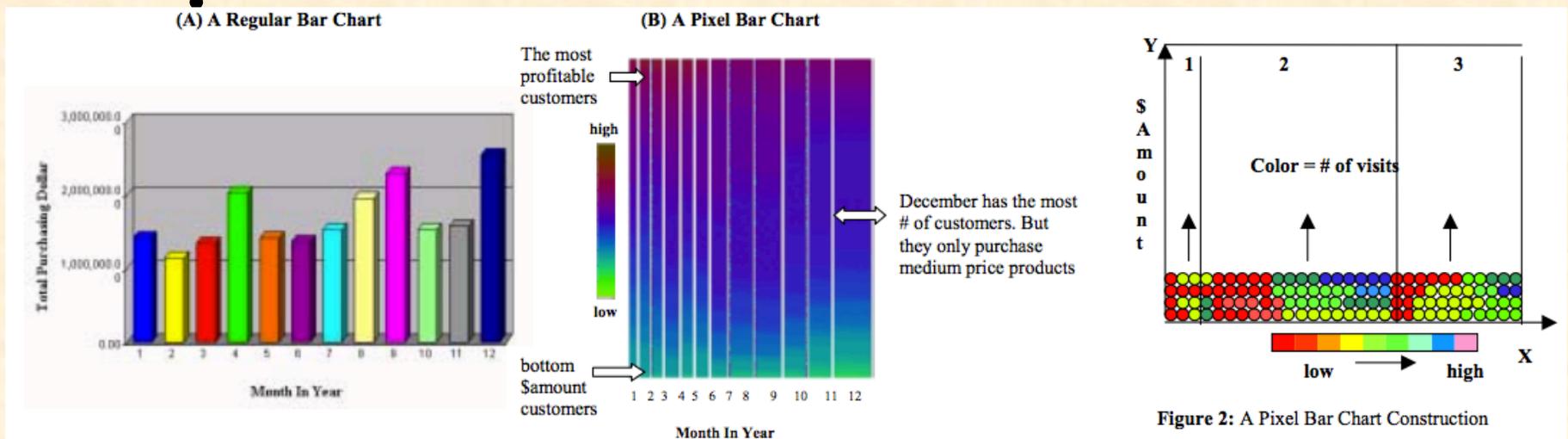
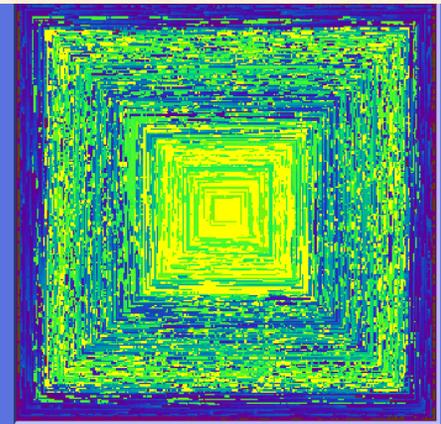
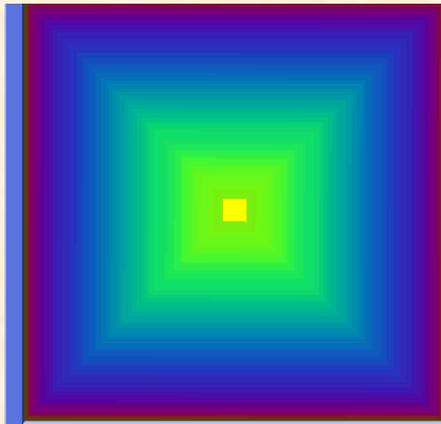


Figure 1: An Example of Mining 44,401 Sales Transactions By Months In A Year

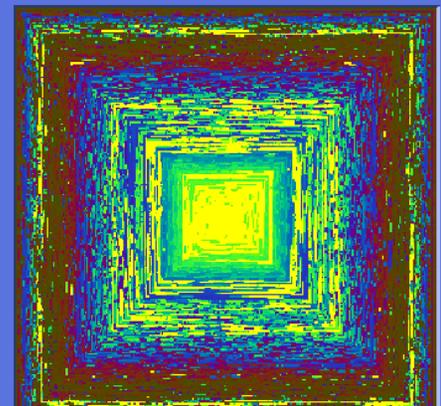
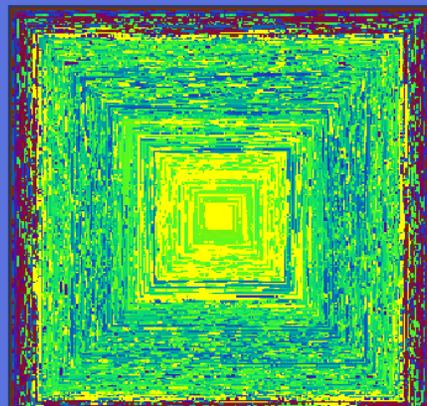
<pixel object,
dividing attribute,
Y-ordering attribute,
X-ordering attribute,
coloring attribute>

<customer,
month,
dollar amount ,
number of visits,
dollar amount >



Solar-Radiation

Humidity



Comparison of Techniques

Comparison of Techniques

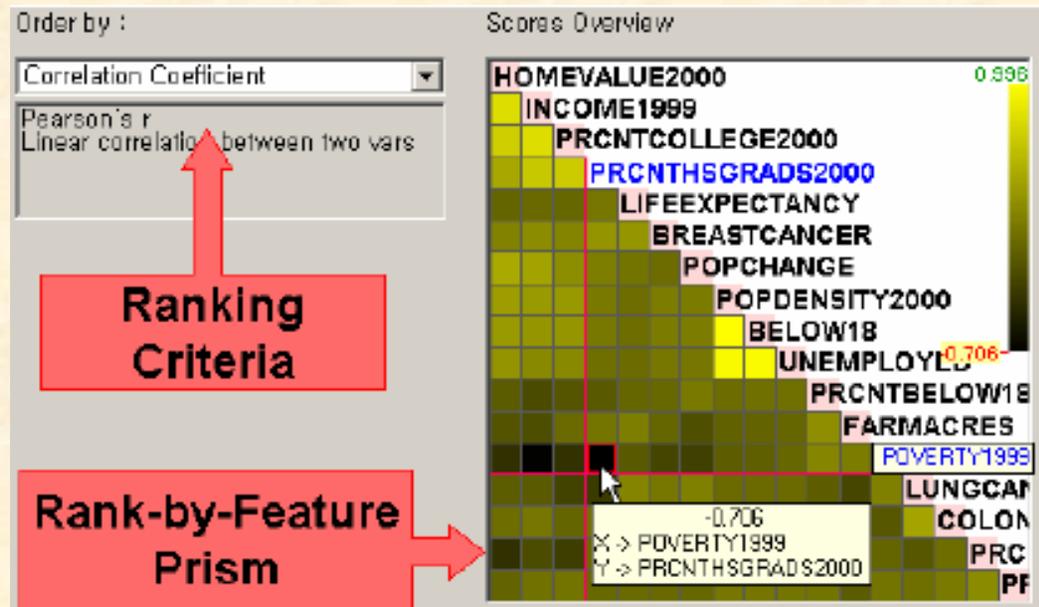
- ParCood: <1000 items, <20 attrs
 - » Relate between adjacent attr pairs
- StarCoord: <1,000,000 items, <20 attrs
 - » Interaction intensive
- TableLens: similar to par-coords
 - » more items with aggregation
 - » Relate 1:m attrs (sorting), short learn time
- Visdb: 100,000 items with 10 attrs
 - » Items*attrs = screenspace, long learn time, must query
- Spotfire : <1,000,000 items, <10 attrs (DQ many)
 - » Filtering, short learn time

Scaling up further

- Beyond 20 dimensions?
 1. Interaction
 - E.g. Offload some dims to Dynamic Query sliders, ...
 2. Reduce dimensionality of the data
 - E.g. Multi-dimensional scaling (MDS) ...later
 3. Visualize features of the dimensions, instead of the data
 - E.g. rank-by-feature
- Tableau

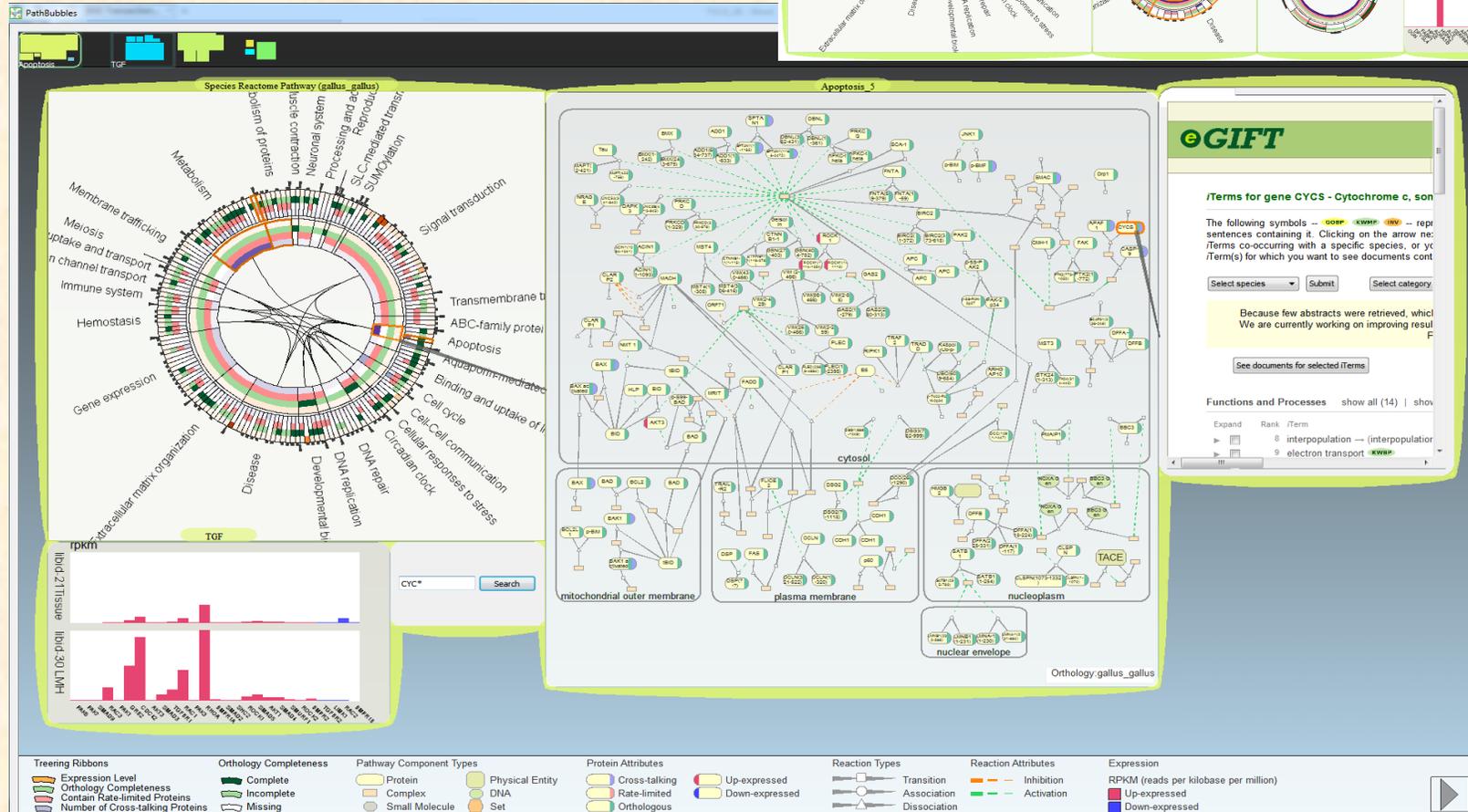
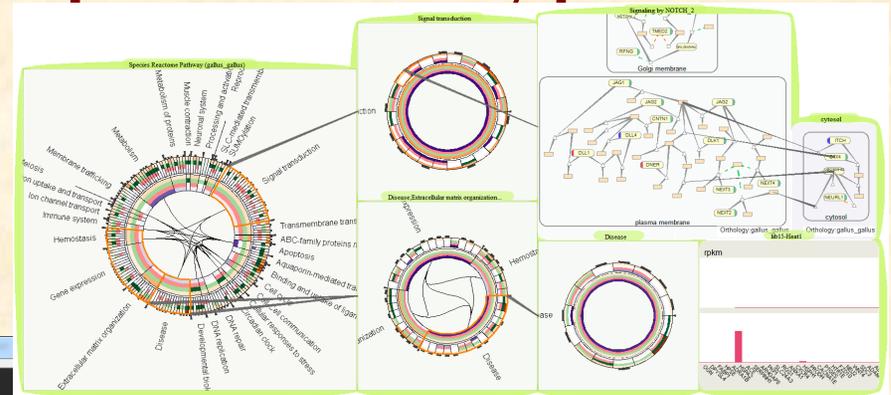
Rank-by-Feature

- Seo, et al.



Combining multiple data types

- Multi-Dimensional:
- PathBubbles: UMBC



Treeing Ribbons Expression Level Orthology Completeness Contain Rate-limited Proteins Number of Cross-talking Proteins	Orthology Completeness Complete Incomplete Missing	Pathway Component Types Protein Complex Small Molecule	Physical Entity DNA Set	Protein Attributes Cross-talking Rate-limited Orthologous	Reaction Types Transition Association Dissociation	Reaction Attributes Inhibition Activation	Expression RPKM (reads per kilobase per million) Up-expressed Down-expressed
---	--	--	--------------------------------------	---	--	--	--

Table - StateData ()			
		Load	Snap
State	College Degree %	Per Capita Income	
Alabama	20.6%	11486	
Alaska	30.3%	17610	
Arizona	27.1%	13461	
Arkansas	17.0%	10520	
California	31.3%	16409	
Colorado	33.9%	14821	
Connecticut	33.8%	20189	
Delaware	27.9%	15854	
District of Columbia	36.4%	18881	
Florida	24.9%	14698	
Georgia	24.3%	13631	
Hawaii	31.2%	15770	
Idaho	25.2%	11457	
Illinois	26.8%	15201	
Indiana	20.9%	13149	
Iowa	24.5%	12422	
Kansas	26.5%	13300	
Kentucky	17.7%	11153	
Louisiana	19.4%	10635	
Maine	25.7%	12957	
Maryland	31.7%	17730	
Massachusetts	34.5%	17224	
Michigan	24.1%	14154	
Minnesota	30.4%	14389	

- I
- S
- I

n
(spatial)

Your solutions

1. Small Multiples

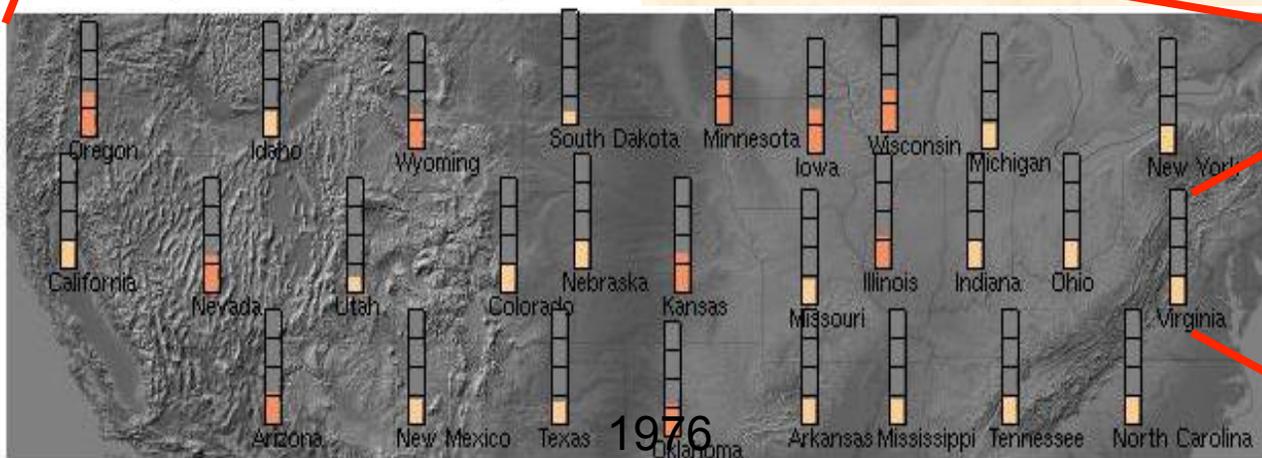
JNLS ON VISUALIZATION AND COMPUTER GRAPHICS, VOL. 12, NO. 5, SEPTEMBER/OCTOBER 2006

The Perceptual Scalability of Visualization

Beth Yost. *Student Member, IEEE* and Chris North

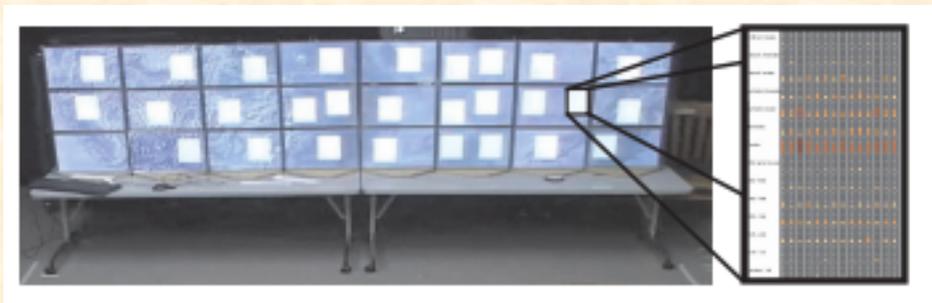
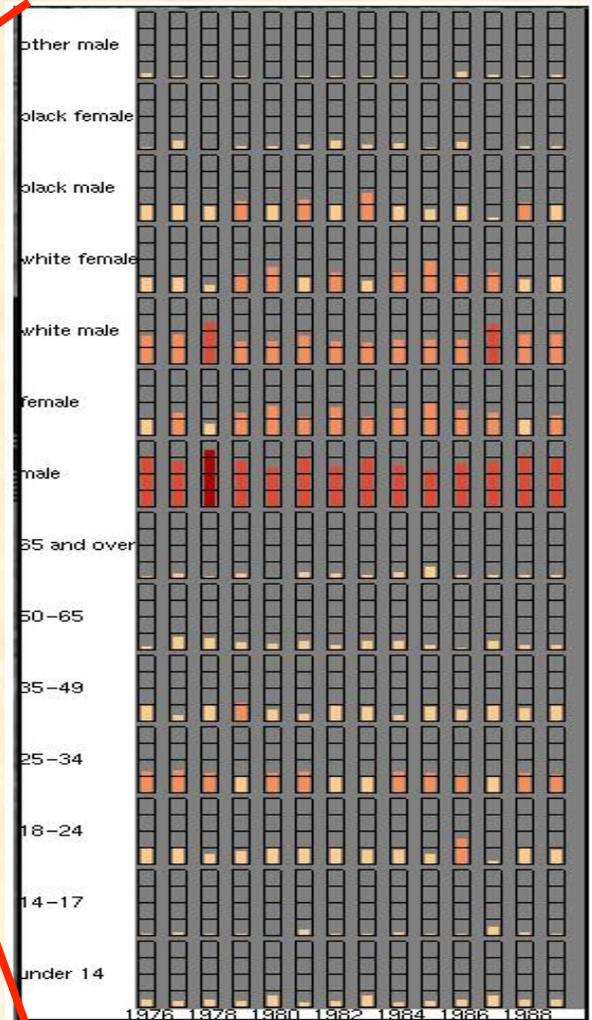
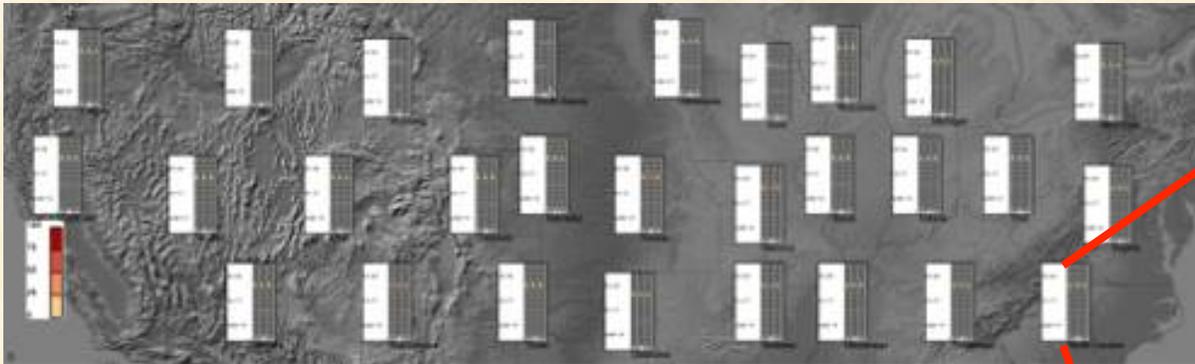
Multiple views: 1 or more attribute / map

Scalability issues: perception | display



2. Embedded Visualizations

Complex glyphs: For each location, show vis of all attributes



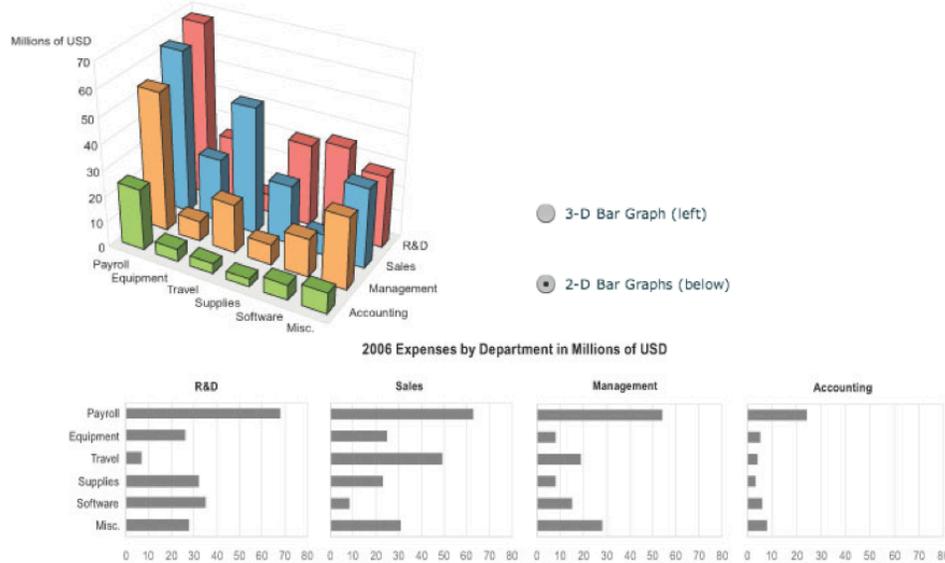
2D vs. 3D

3. 2D vs. 3D

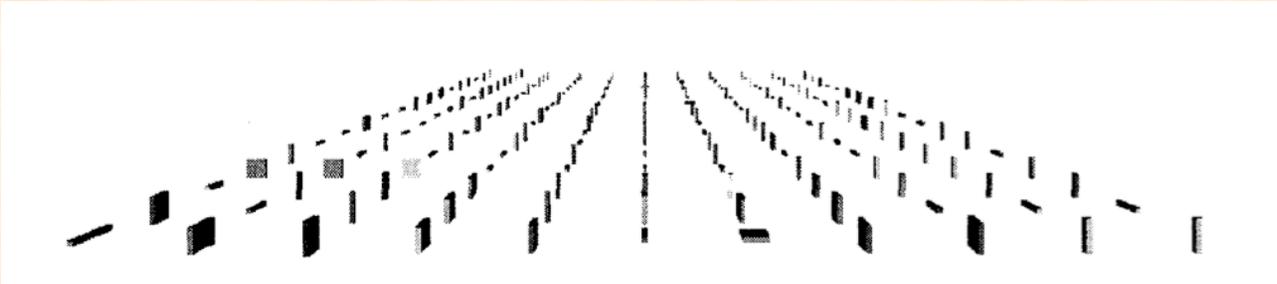
Graph Design I.Q. Test

Question 7: Which graph makes it easier to determine R&D's travel expense?

2006 Expenses by Department

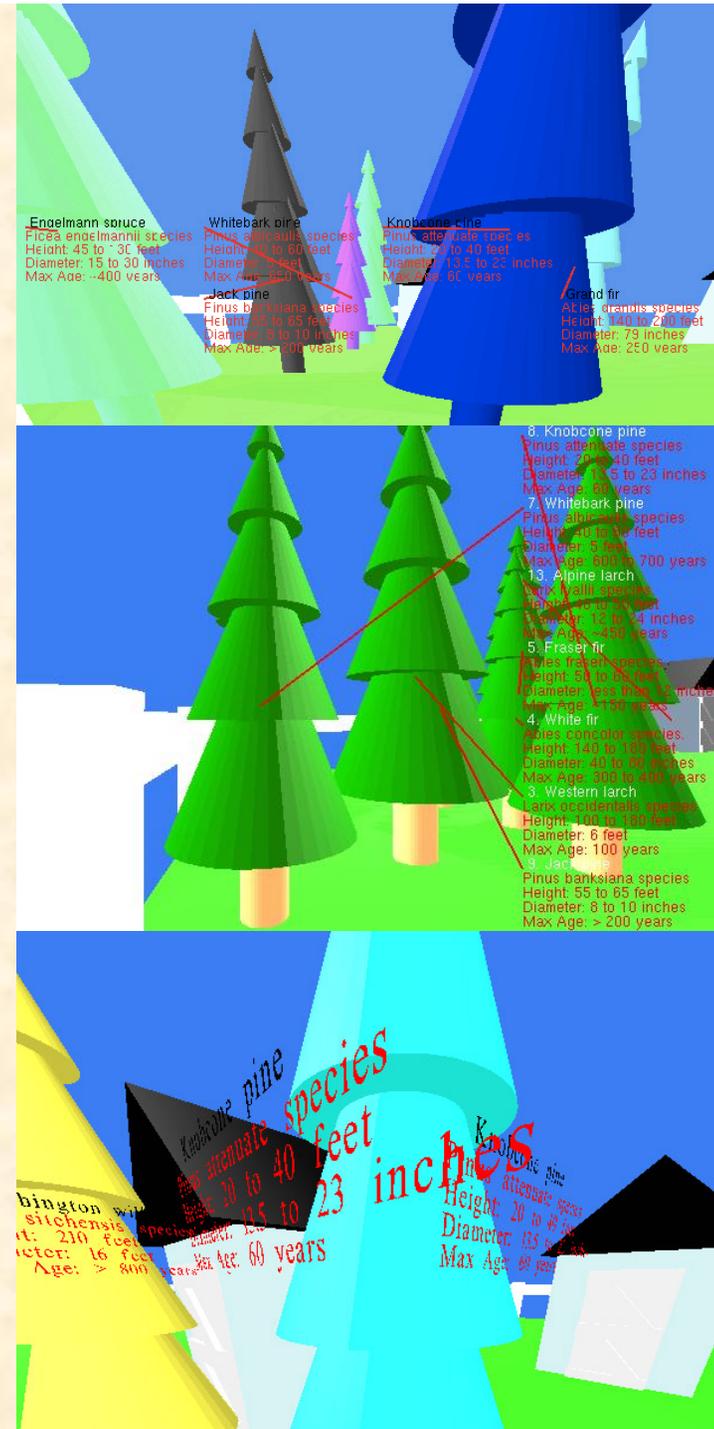


Occlusion
shadow changes the colors?
Chart junk
Patterns -> area;
perspectives



2D vs. 3D: text?

- Texts?
- Feiner, Augmented reality



Mental modal vs. Features

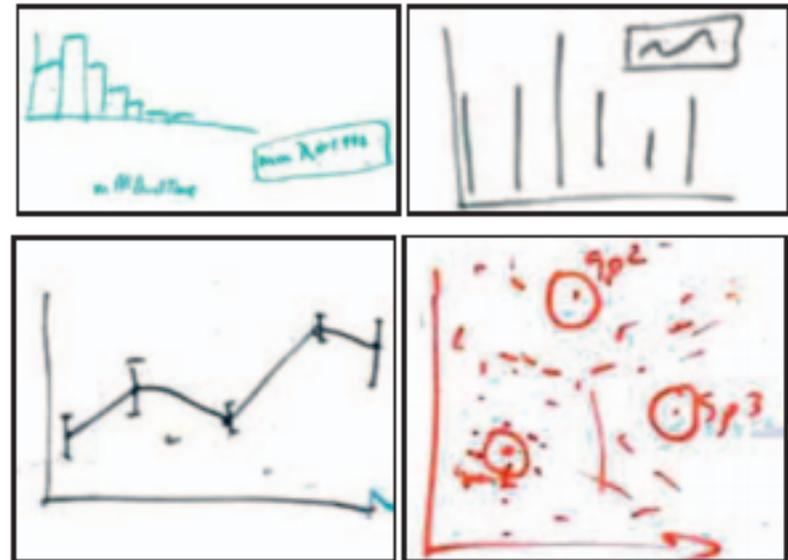
VIS externalization media

Foundations of Science (2005) 10: 89–106

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J. GREGORY TRAFTON, SUSAN B. TRICKETT and FARILEE E. MINTZ

CONNECTING INTERNAL AND EXTERNAL
REPRESENTATIONS: SPATIAL TRANSFORMATIONS OF
SCIENTIFIC VISUALIZATIONS



2508

IEEE TRANSACTIONS ON VISUALIZATION AND COMPUTER GRAPHICS, VOL. 17, NO. 12, DECEMBER 2011

Visual Thinking In Action: Visualizations As Used On Whiteboards

Jagoda Walny, Sheelagh Carpendale, Nathalie Henry Riche, Gina Venolia, and Philip Fawcett

Stereo, tracking, larger FOV?

<http://www.youtube.com/watch?v=I1x4-g6wbtU#t=29>

Linsen group, the effect of stereoscopic immersive environment on projection-based multi-dimensional data visualization. IV 2013.

Tasks: 1. count the cluster; 2/3. find closest cluster to a specific point/cluster; 4. detect the densest cluster; 5. find the most distant cluster pair; 6. count the outliers; 7. find the closest cluster to select group of points; 8. name all of the pairs of overlapping clusters

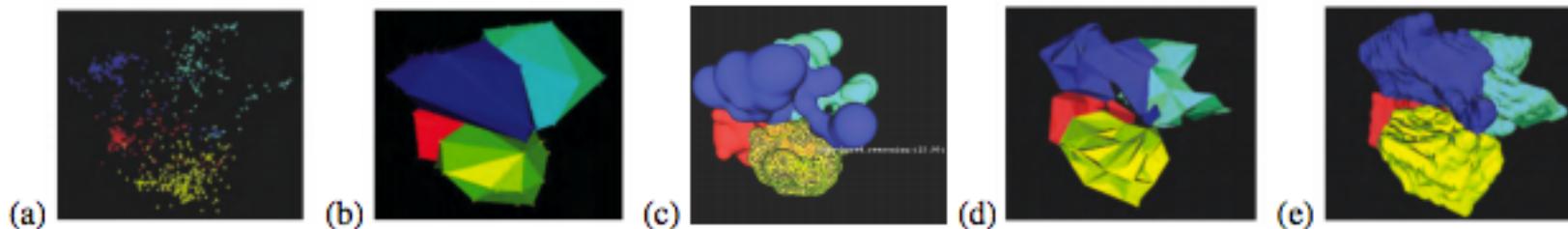
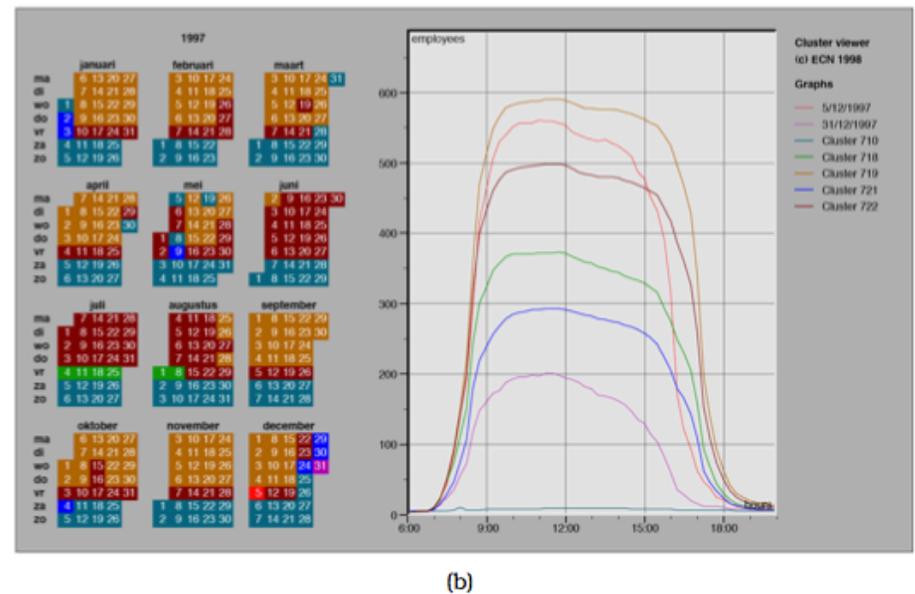
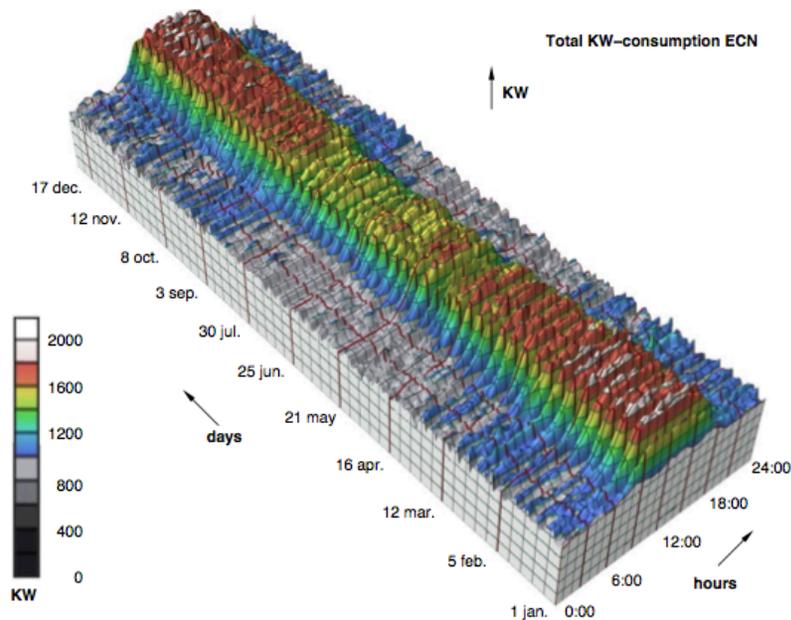
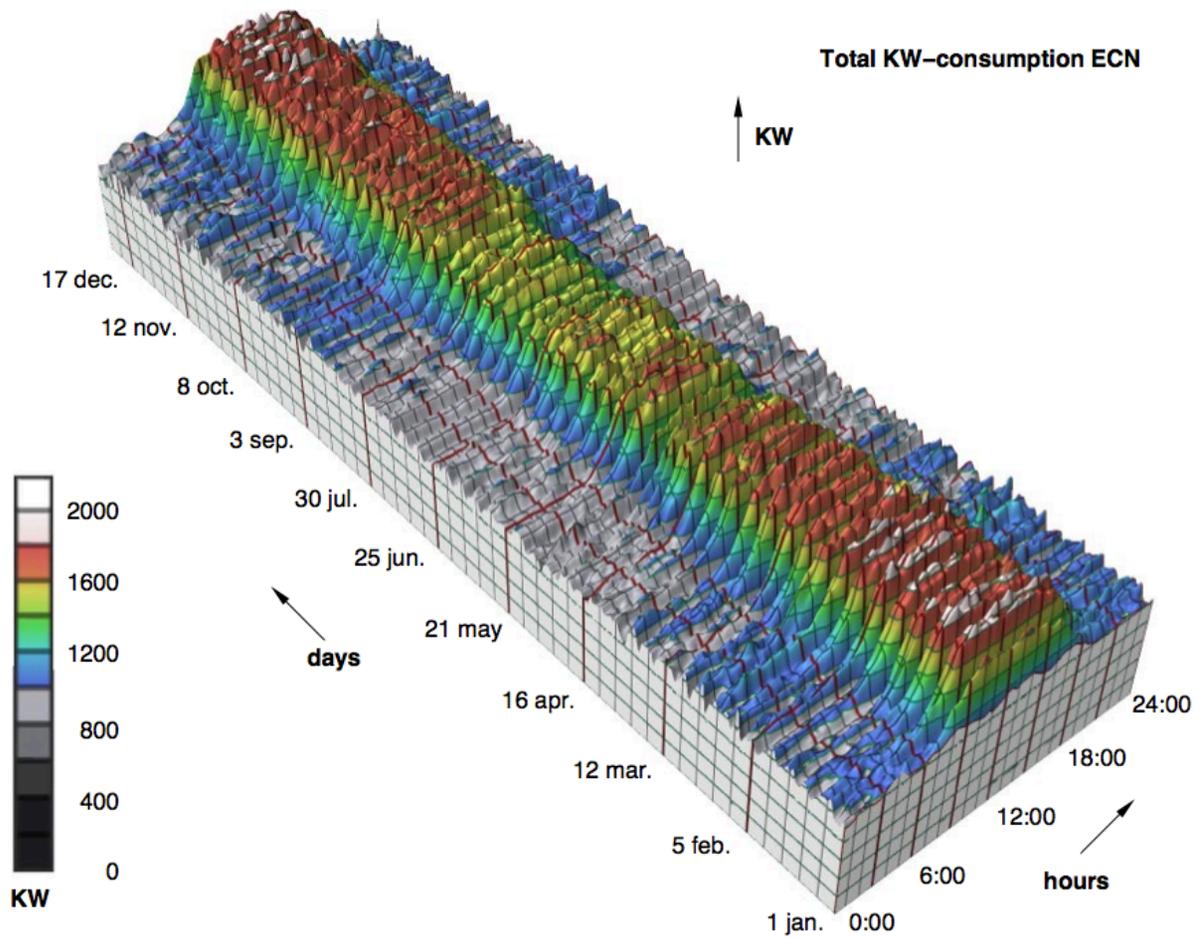


Fig. 1. Visual encoding of the clusters in 3D visual space using (a) Points, a 3D scatterplot with clusters encoded by color., (b) ConvHull, (c) PointsEncSurf, (d) NonconvHull, and (e) HullEncSurf.

Time series

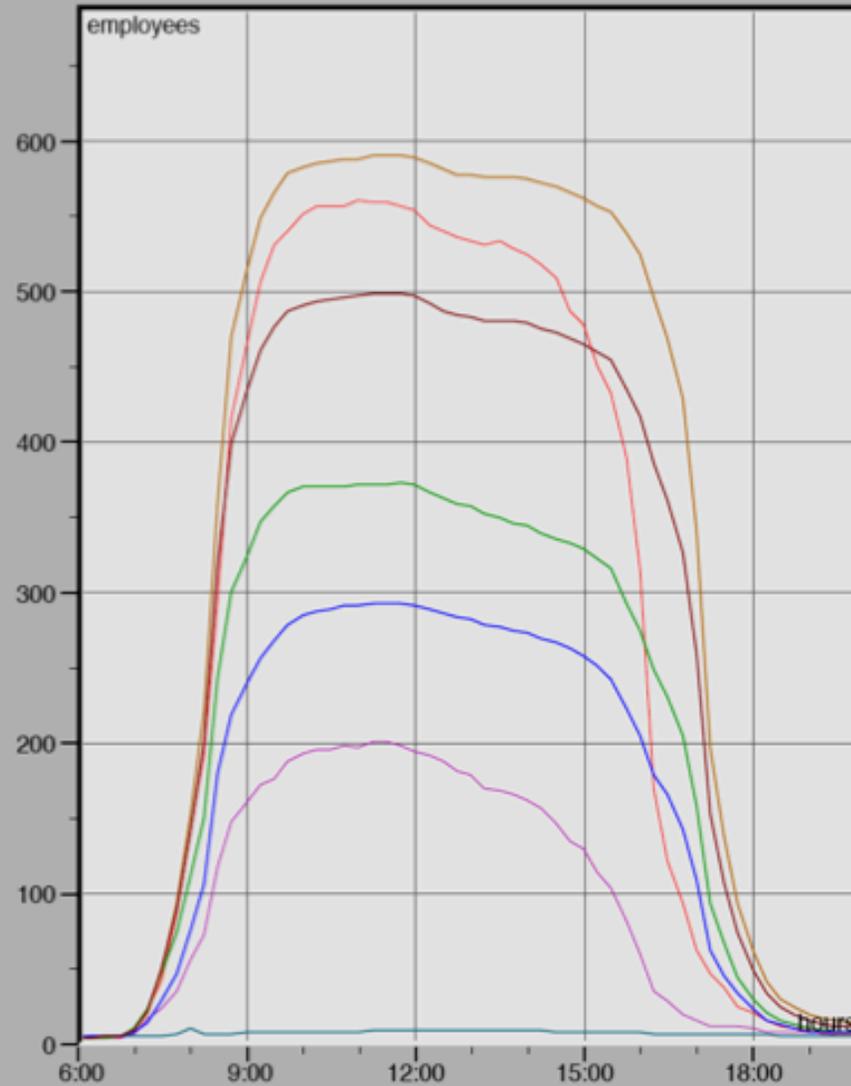
- Van wijk and van Selow 99,
 - # of people inside and amount of power used over the course of each day for one full year.





(a)

1997



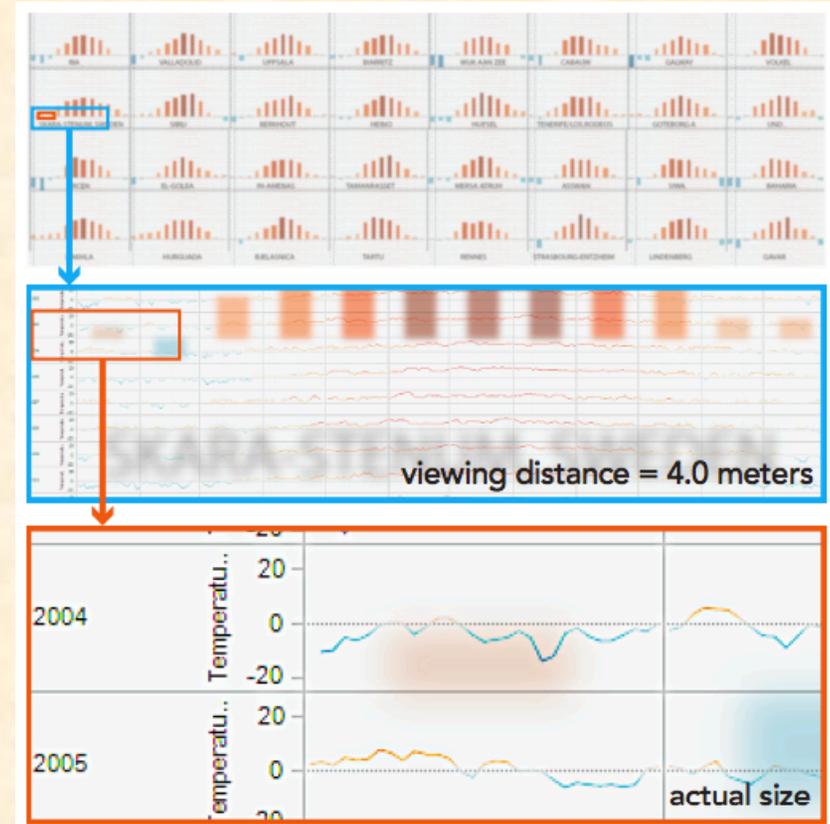
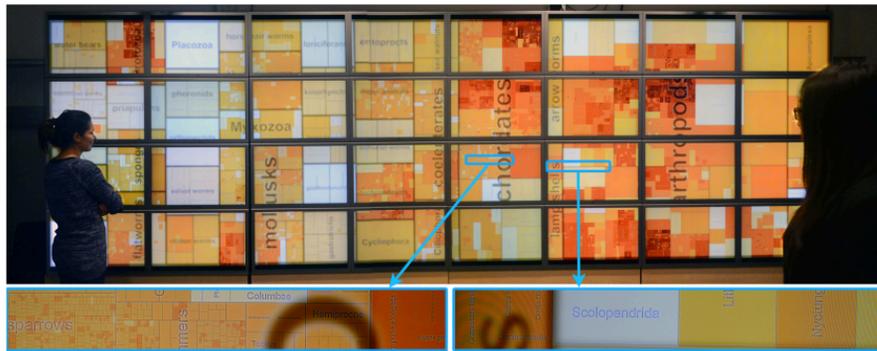
Cluster viewer
(c) ECN 1998

Graphs

- 5/12/1997
- 31/12/1997
- Cluster 710
- Cluster 718
- Cluster 719
- Cluster 721
- Cluster 722

2.5D

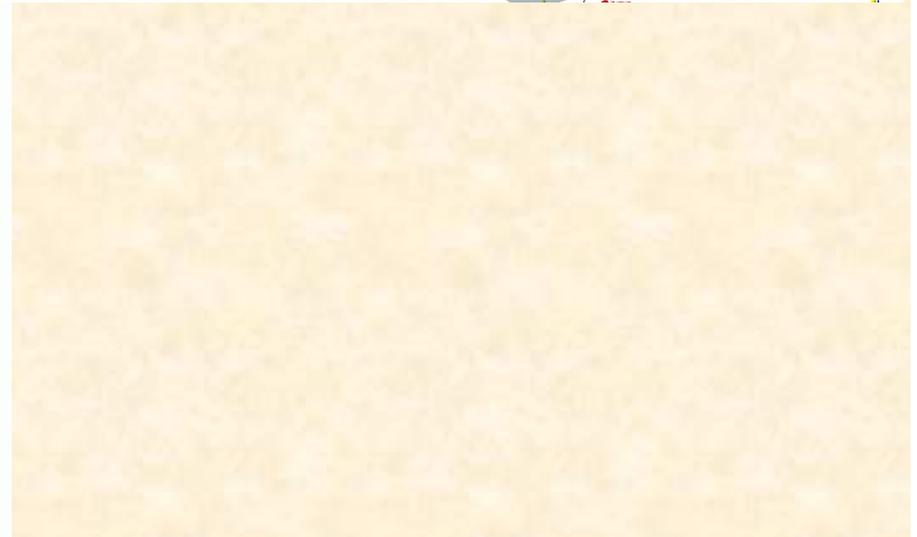
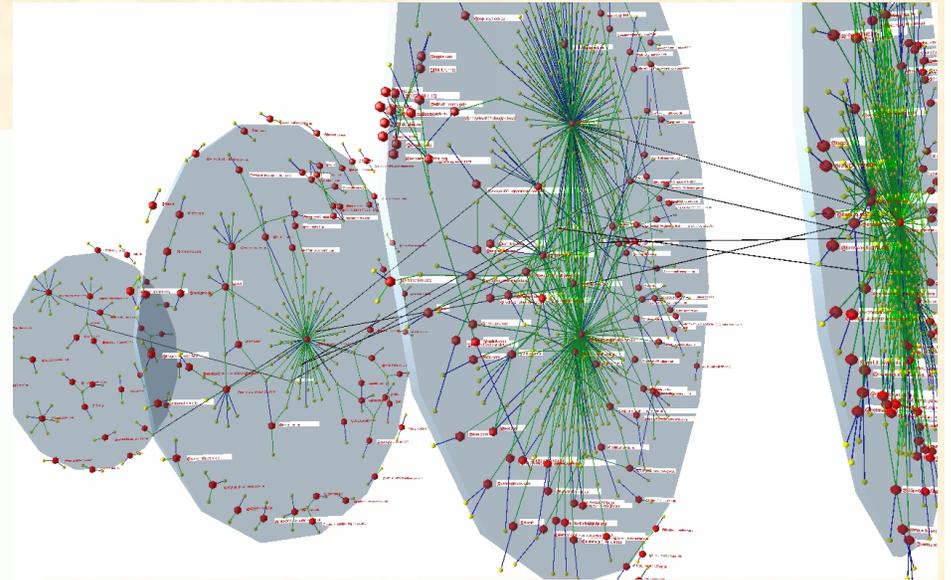
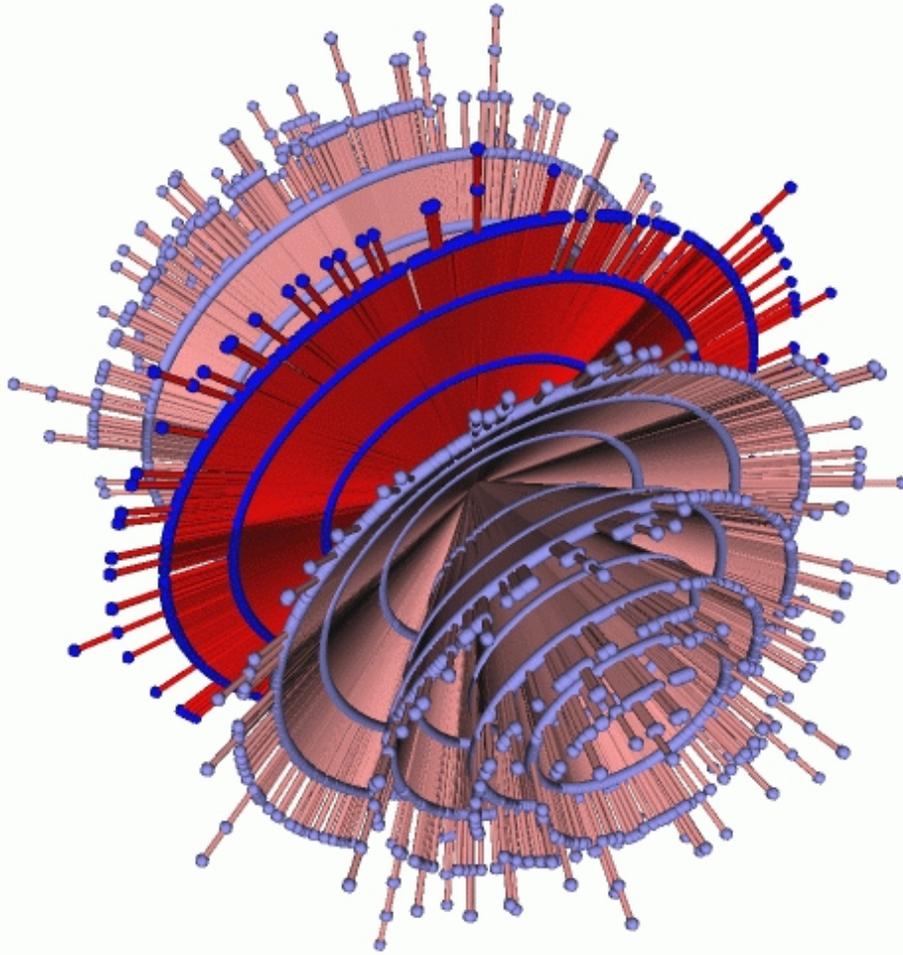
- Petra Isenberg, Hybrid-image vis (2013)



- Today: Alex Garbarino (pathway analysis)

2.5D

- Seokhee Hong



Multi-Dimensional Functions

Multi-Dimensional Functions

- $y = f(x_1, x_2, x_3, \dots, x_n)$
- Continuous:
 - E.g. $y = x_1^3 + 2x_2^2 - 9x_3$
- Discrete:
 - x_i are uniformly sampled in a bounded region
 - E.g. $x_i = [0, 1, 2, \dots, 100]$
 - E.g. measured density in a 3D material under range of pressures and room temperatures.

Variables

- Independent variables
- Dependent variables

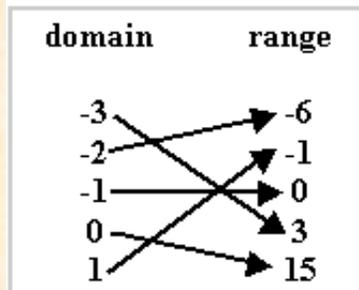


State	College Degree %	Per Capita Income
Alabama	20.6%	11486
Alaska	30.3%	17610
Arizona	27.1%	13461
Arkansas	17.0%	10520
California	31.3%	16409
Colorado	33.9%	14821
Connecticut	33.8%	20189
Delaware	27.9%	15854
District of Columbia	36.4%	18881
Florida	24.9%	14698
Georgia	24.3%	13631
Hawaii	31.2%	15770
Idaho	25.2%	11457
Illinois	26.8%	15201
Indiana	20.9%	13149
Iowa	24.5%	12422
Kansas	26.5%	13300
Kentucky	17.7%	11153
Louisiana	19.4%	10635
Maine	25.7%	12957
Maryland	31.7%	17730
Massachusetts	34.5%	17224
Michigan	24.1%	14154
Minnesota	30.4%	14389

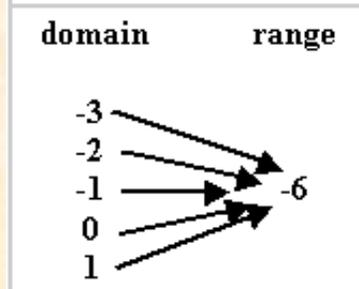
Relations vs. Functions

- Relations:
 - $R(A, B, C, D, E, F)$
 - All dependent variables (1 ind.var.?)
 - Sparse points in multi-d dep.var. space
- Functions: well behaved relations
 - $R(A, B, C, D, E, F, Y) : Y=f(A, B, C, D, E, F)$
 - Many independent variables
 - Defined at every point in multi-d ind.var. space (“onto”)
 - Huge scale: 6D with 10 samples/D = 1,000,000 data points

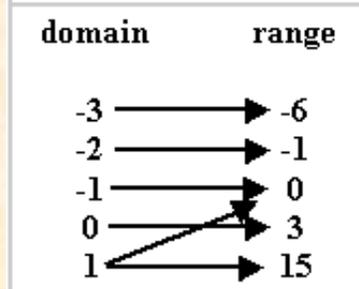
Relation or function?



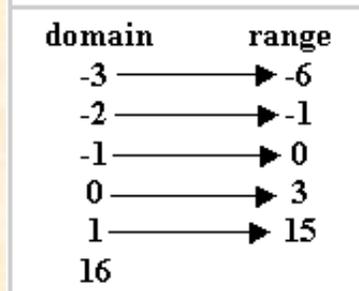
Function



Function



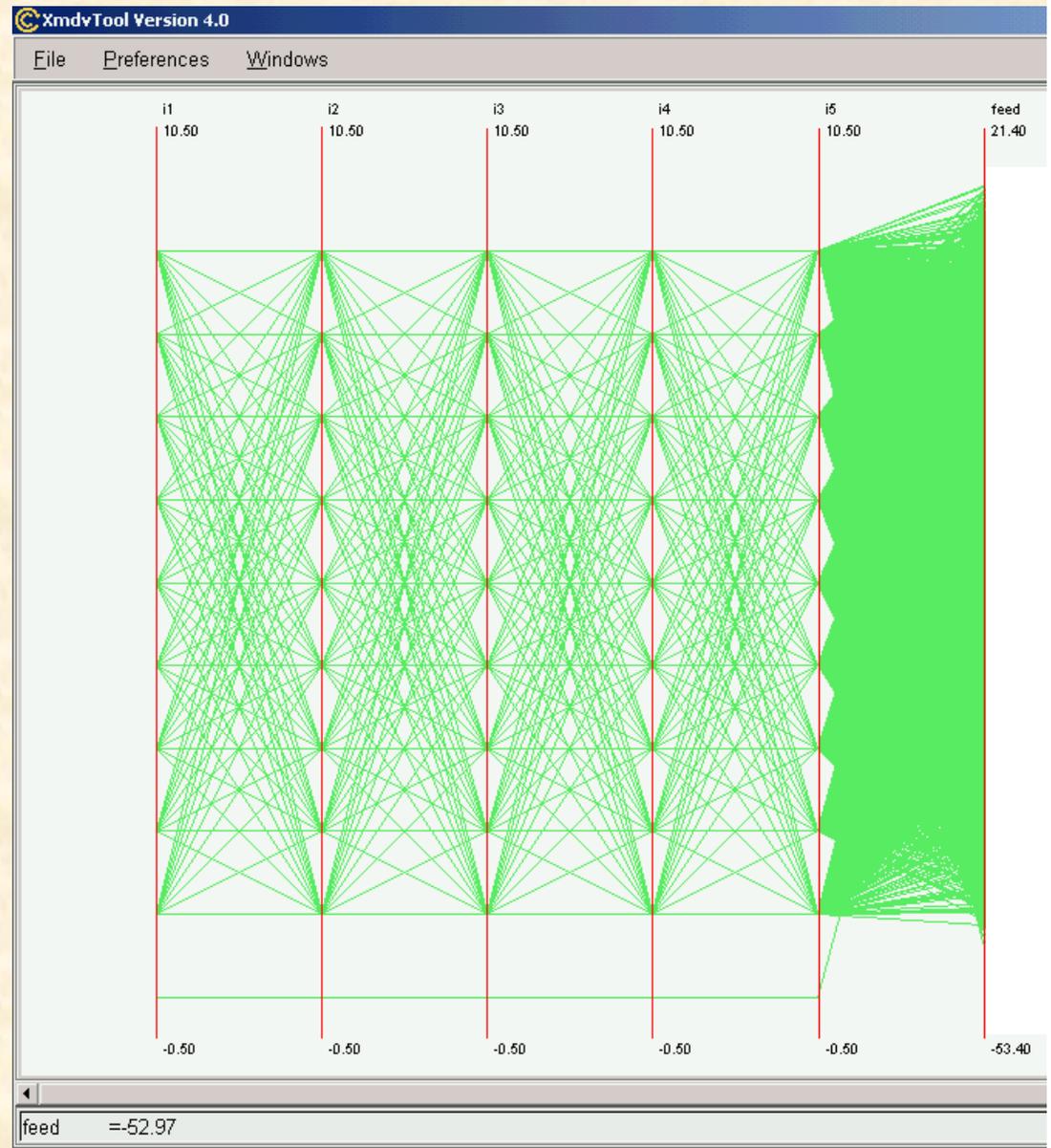
Relation



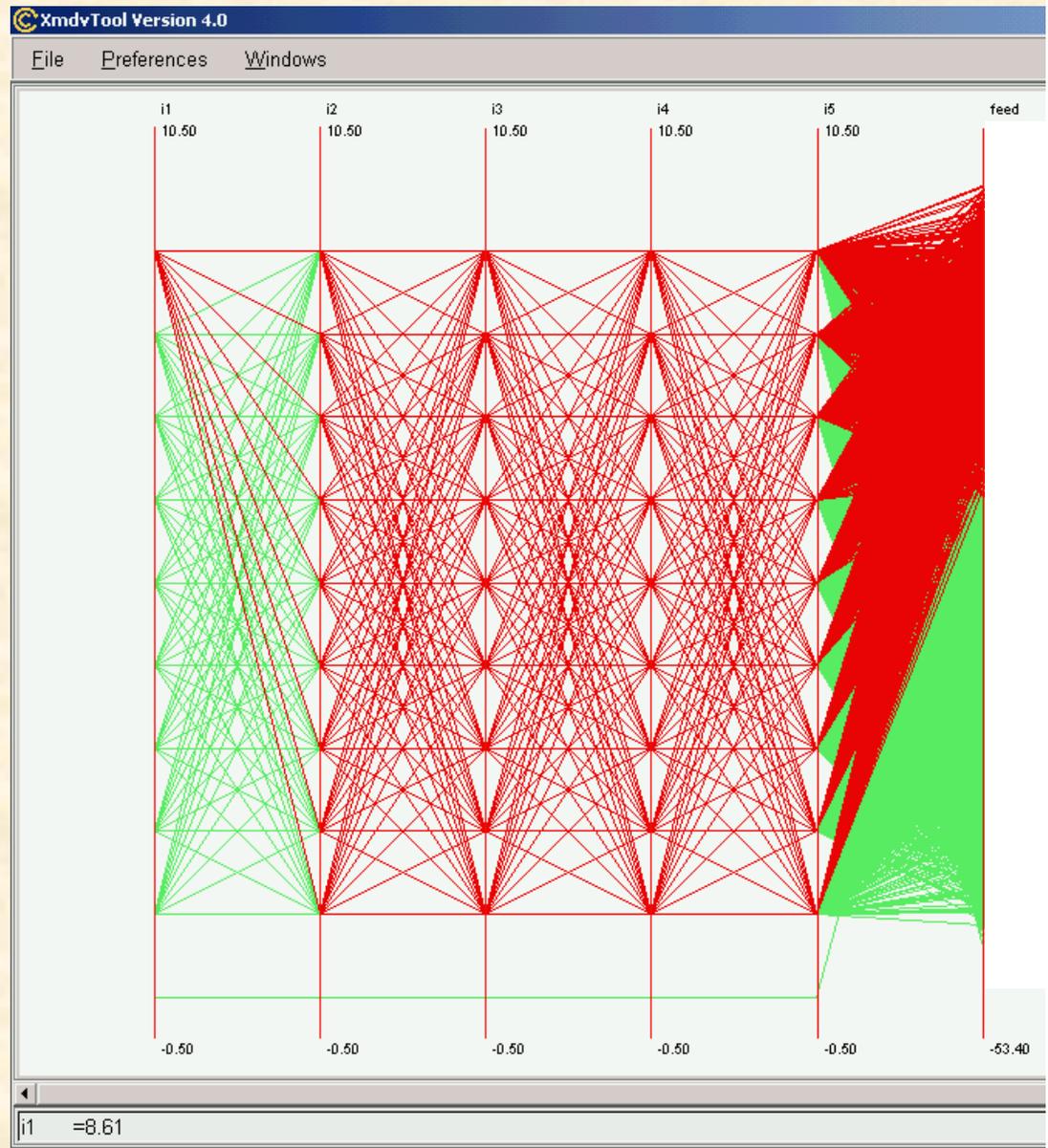
Neither Function nor Relation?

Multi-D Relation Visualizations...

- Don't work well for multi-D functions
- Example:
 - Parallel coords
 - 5D func sampled on 1-9 for all ind.vars.



- Typically want to encode ind.vars. as spatial attrs

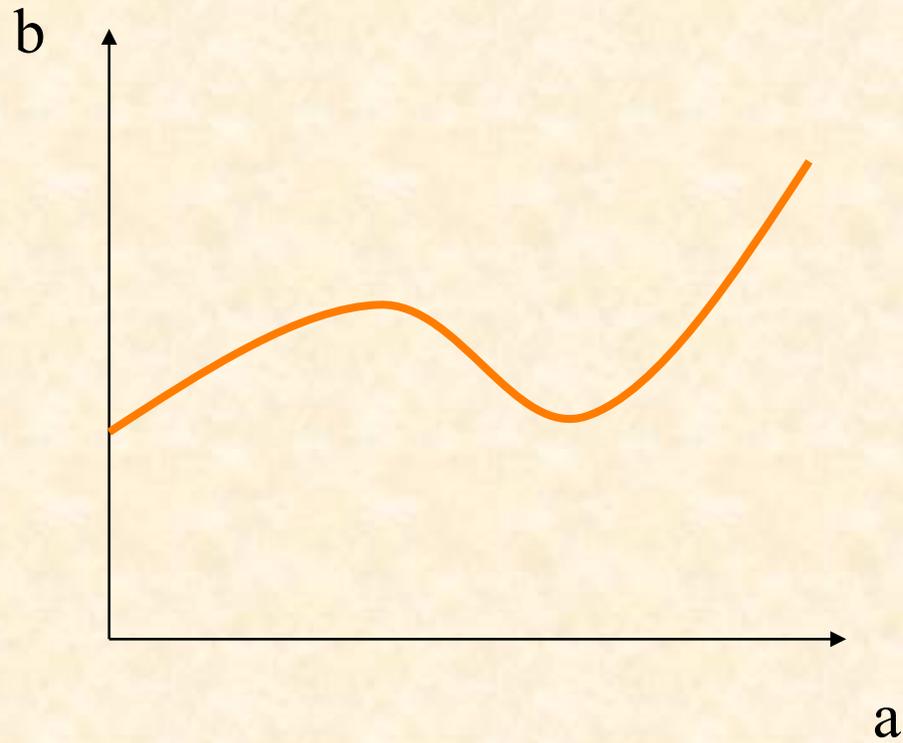


1-D: Easy

- $b = f(a)$

- $a \rightarrow x$

- $b \rightarrow y$



2-D: Easy

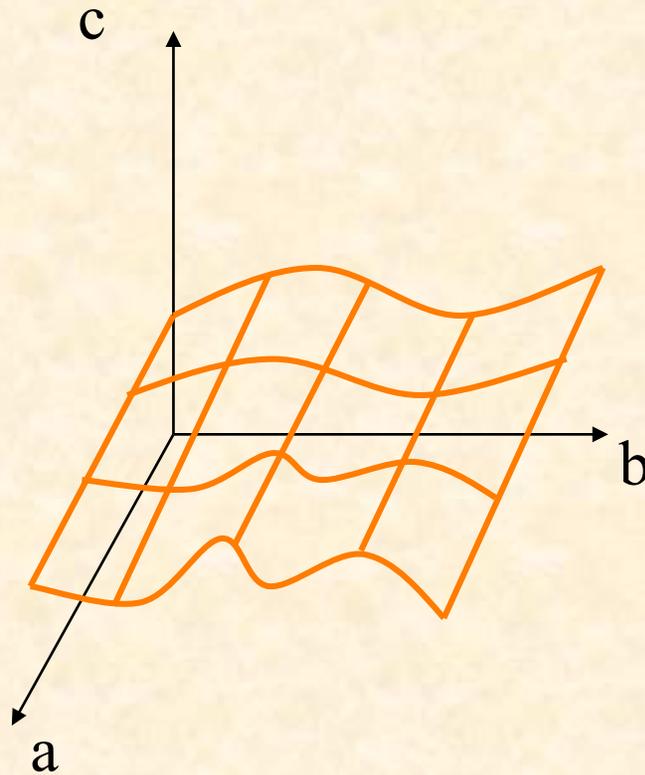
- $c = f(a, b)$

- Height field:

- $a \rightarrow x$

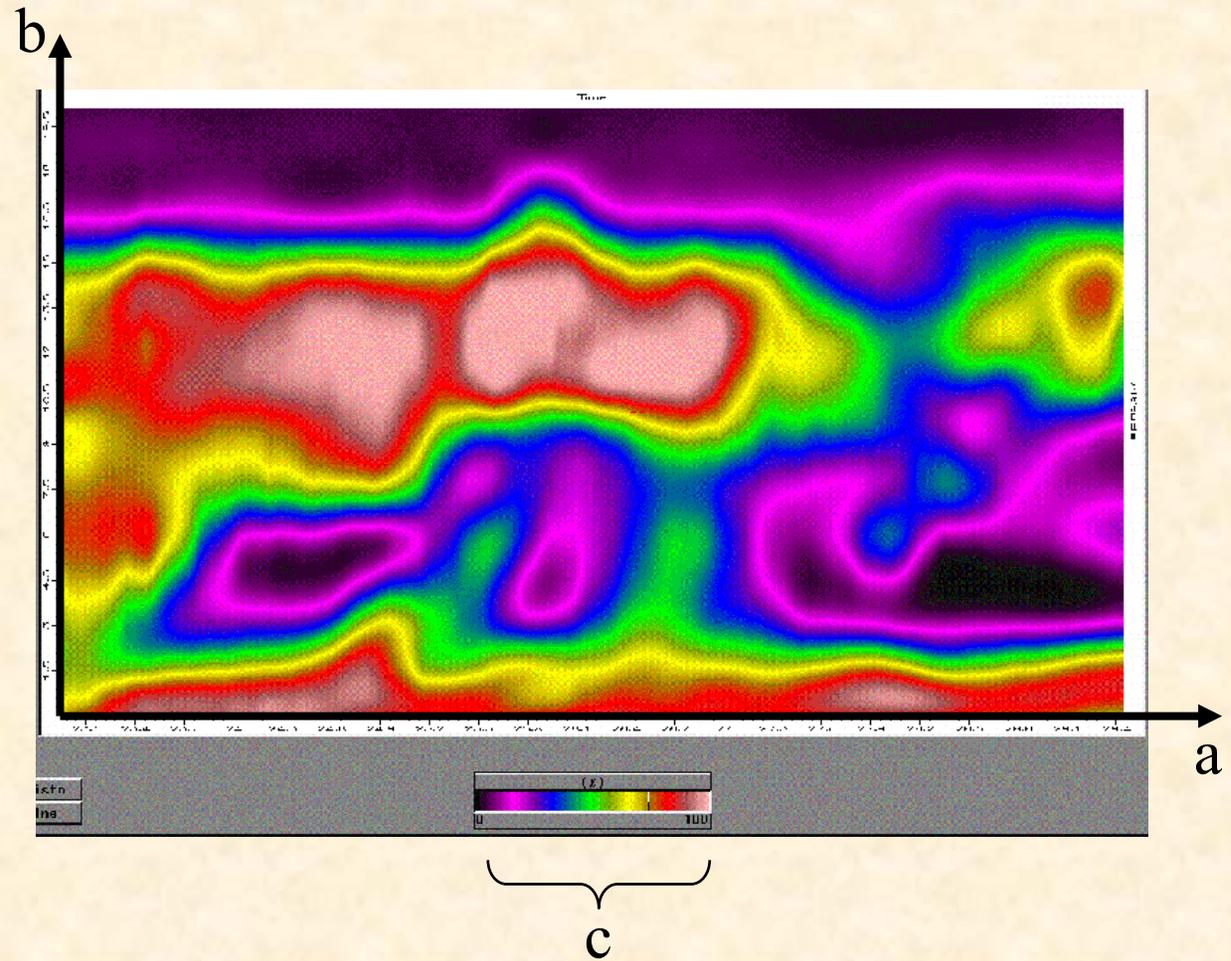
- $b \rightarrow y$

- $c \rightarrow z$



2-D: Easy

- $c = f(a, b)$
- Heat map:
- $a \rightarrow x$
- $b \rightarrow y$
- $c \rightarrow \text{color}$



3-D: Hard

- $d = f(a, b, c)$

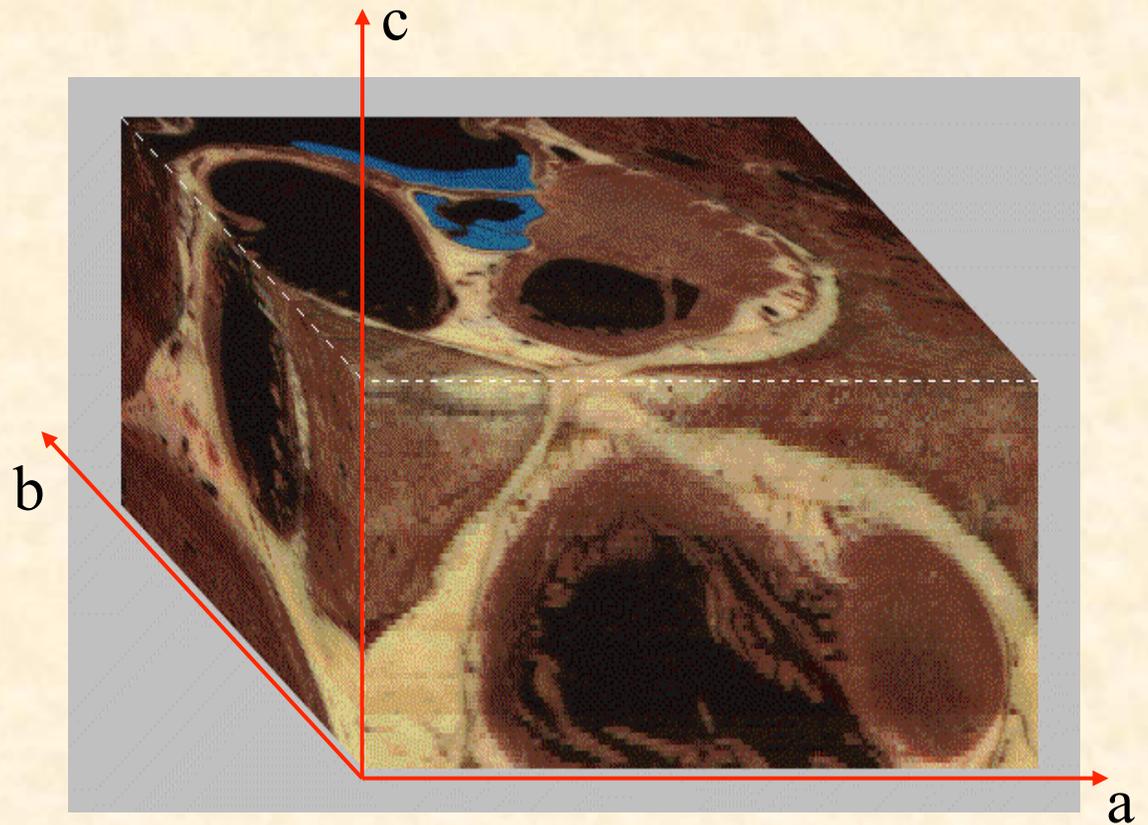
- Color volume:

- $a \rightarrow x$

- $b \rightarrow y$

- $c \rightarrow z$

- $d \rightarrow \text{color}$



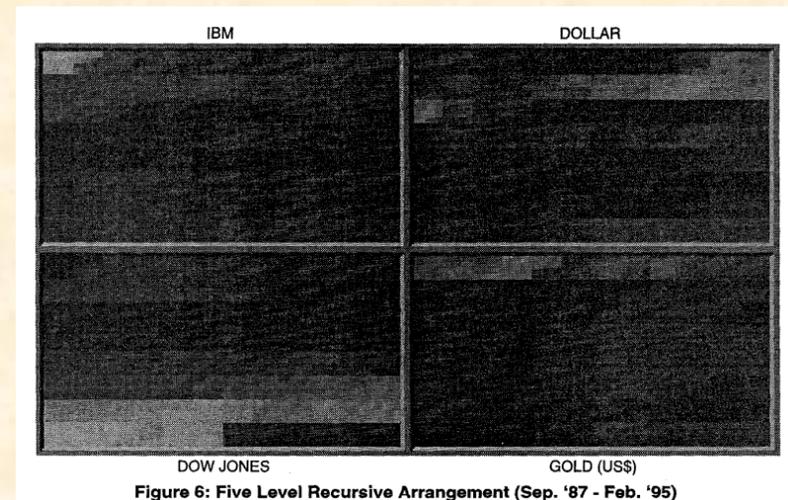
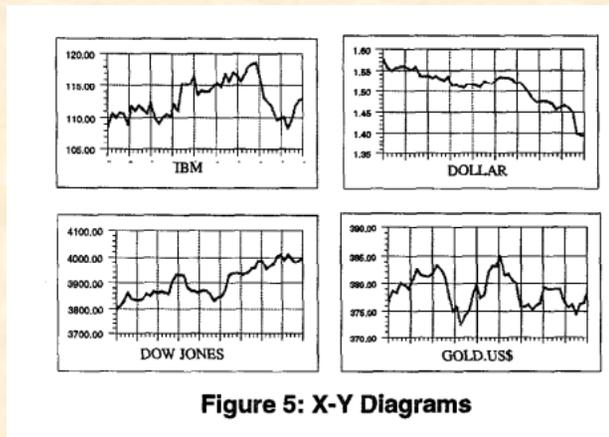
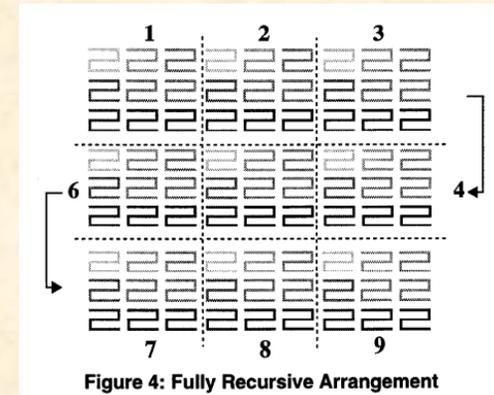
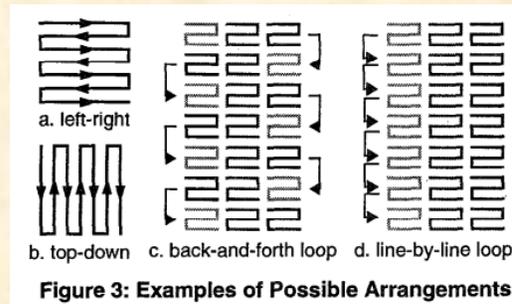
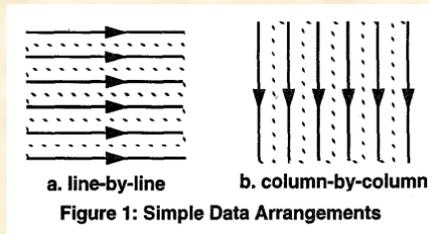
- What's inside?

≥4D: Really Hard

- $y = f(x_1, x_2, x_3, x_4, \dots, x_n)$
- What does a 5D space look like?
- Approaches:
 - Positioning: Recursive pattern (Keim)
 - Scalable aggregation: imMens (Liu)
 - Nested coordinate frames (Worlds within Worlds)
 - Slicing (HyperSlice)
 - Radial Focus+Context (PolarEyez, Sanjini)
- What we talked about before: filtering | overview

Position on paper

- Keim, Recursive pattern: a technique for visualization very large amounts of data



Aggregation: Binned plots

- Liu, Jiang and Heer, imMens: Real-time visual querying of big data
 - ‘big’: one million or more data cases
 - Bin: adjacent intervals over a continuous range
 - Scalability issues: perception | interaction.
 - Novelty: scalability should be limited by the chosen resolution of the visualized data, not the number of records.

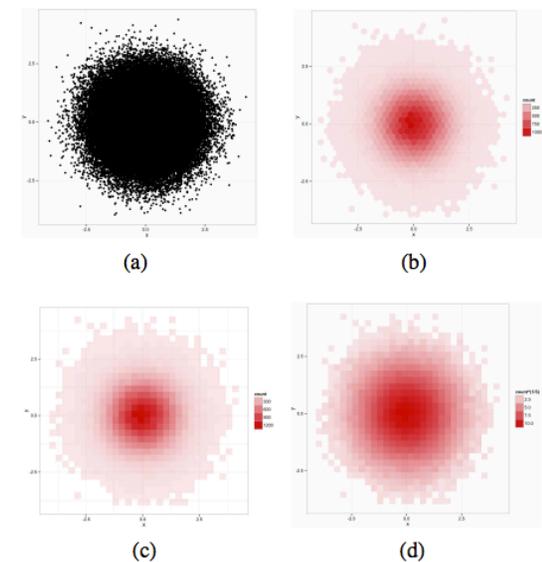
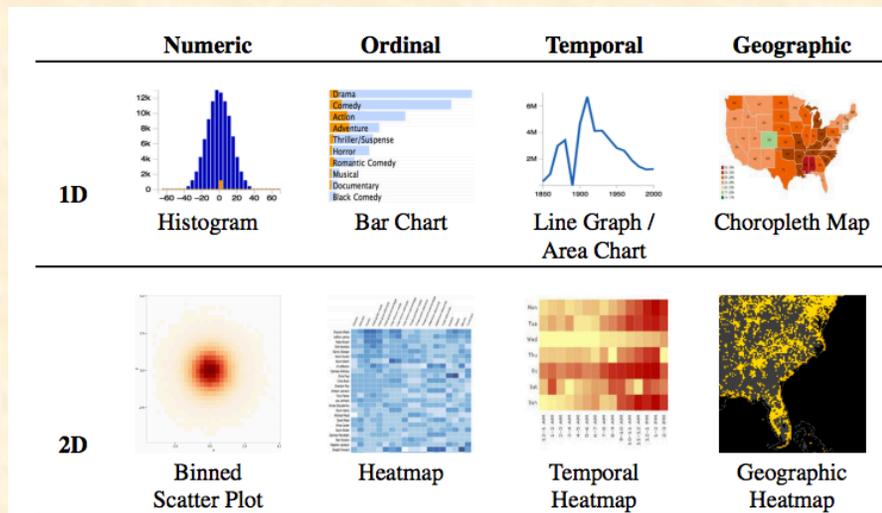


Figure 2: Scatter plots with 100,000 data points: (a) traditional, (b) hexagonal bins, (c) rectangular bins and (d) rectangular bins with perceptual (cube root) color adjustment.

Interactive Visualization of Streaming Data with Kernel Density Estimation

Ove Daae Lampe*
University of Bergen, Norway and
Chr. Michelsen Research AS

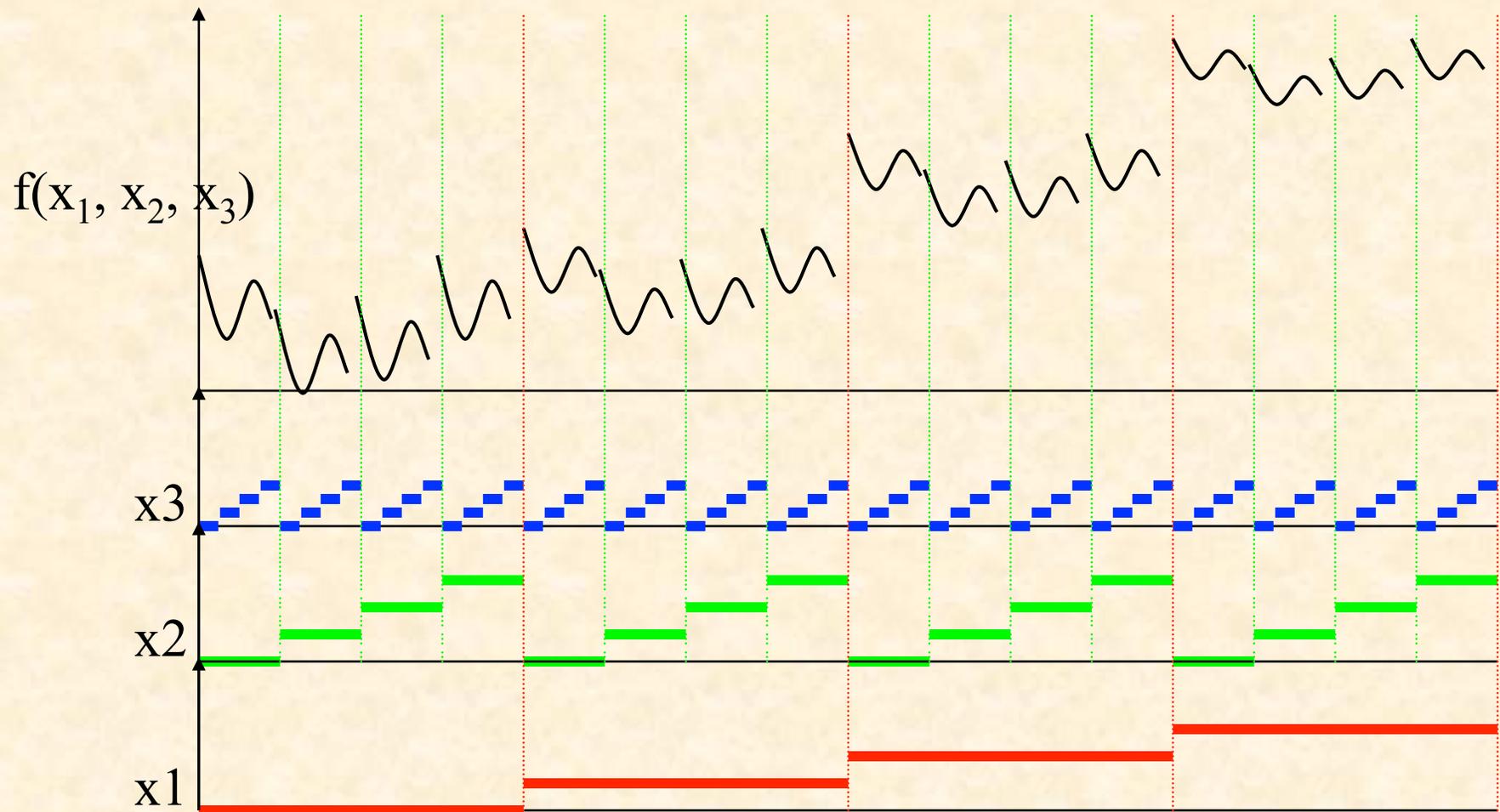
Helwig Hauser†
University of Bergen, Norway
www.ii.UiB.no/vis



Figure 1: Interactive zooming towards SF Bay, where at first all the traffic from the Bay Area is aggregated, to a view where we can separate traffic from the three major airports, and even the distribution of traffic in each airports' cardinal direction. This interaction is enabled by automatically updating the bandwidth of the KDE when the viewport changes.

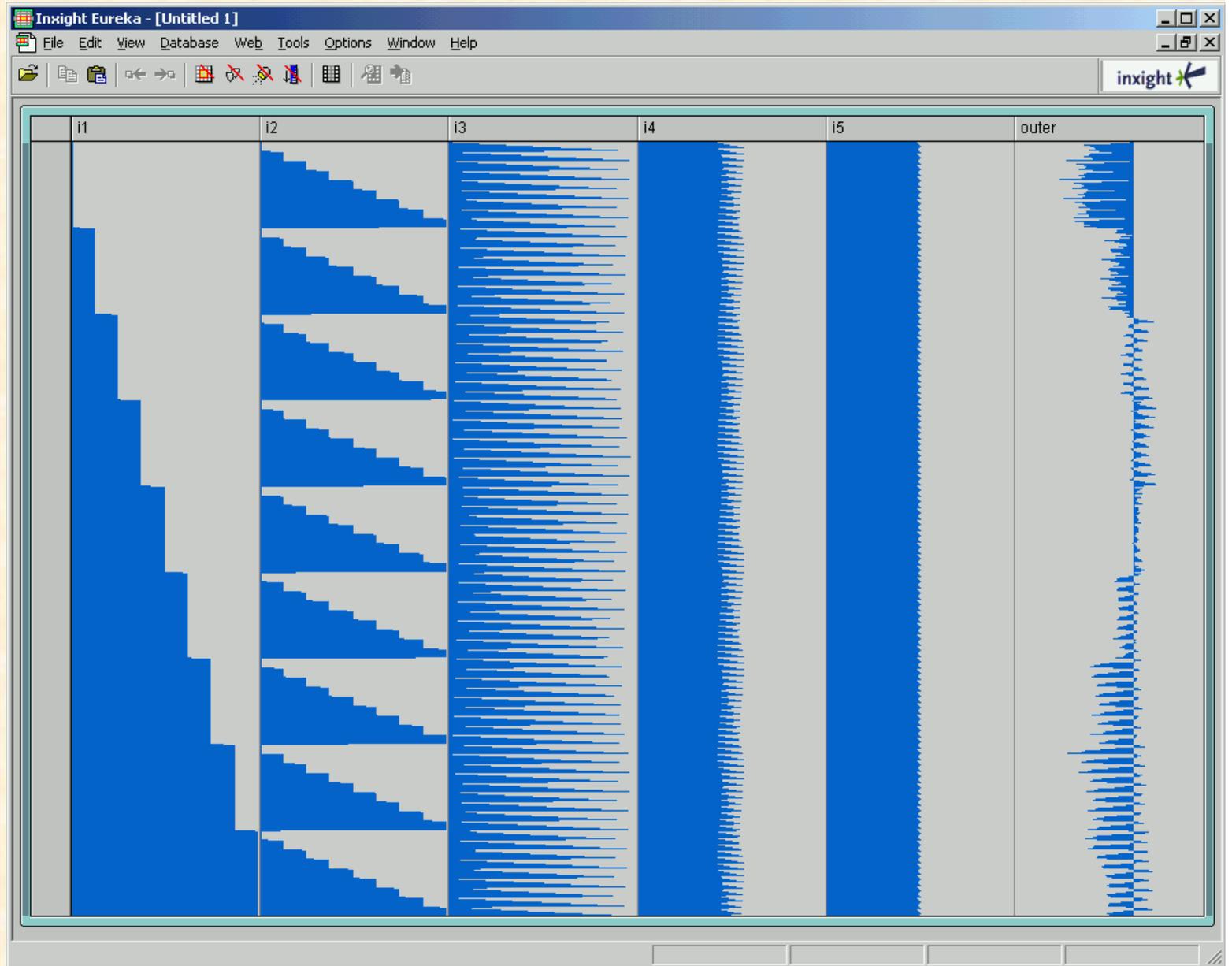
Hierarchical Axes

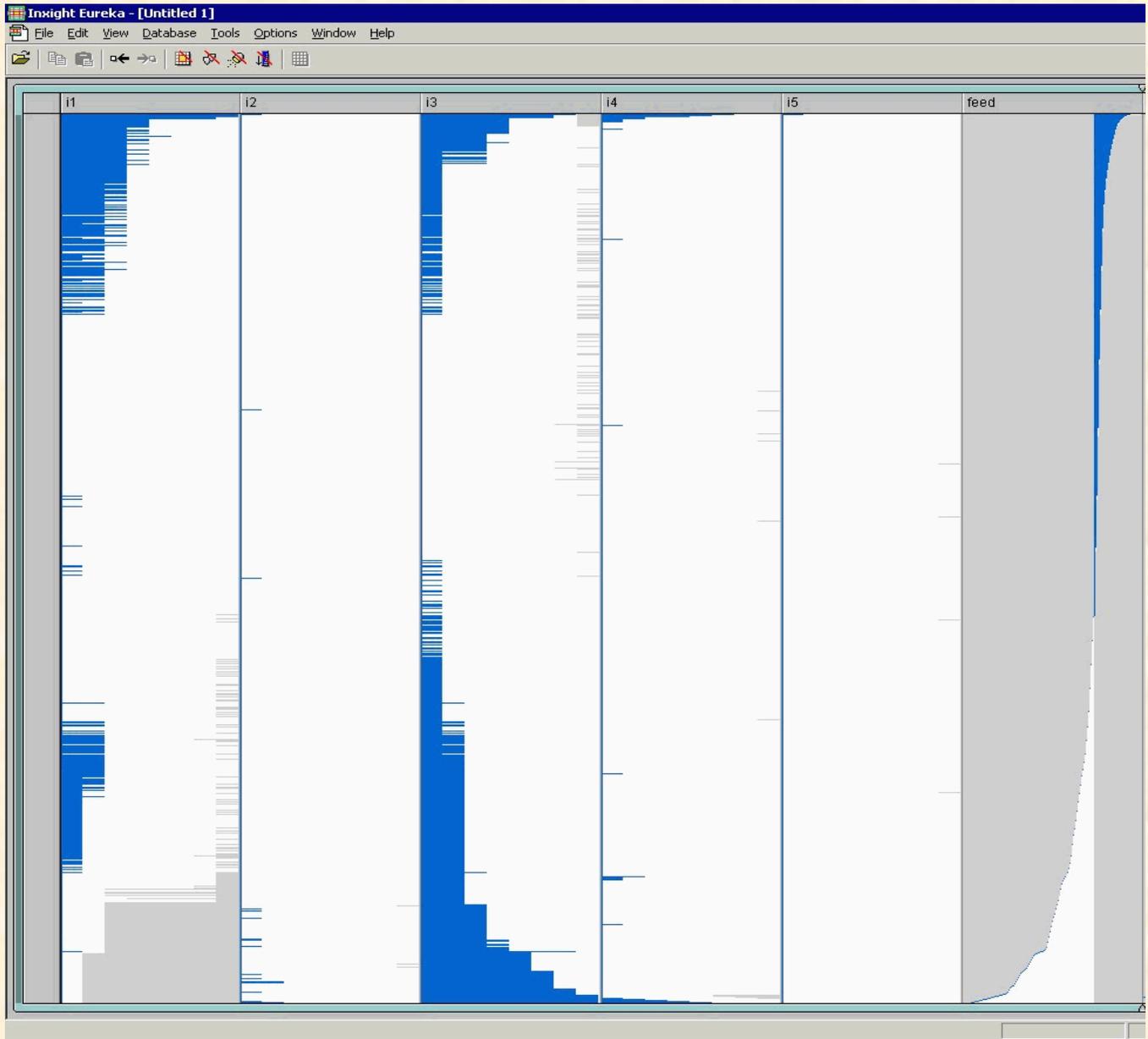
- 1D view of 3D function: (Mihalisin *et al.*)



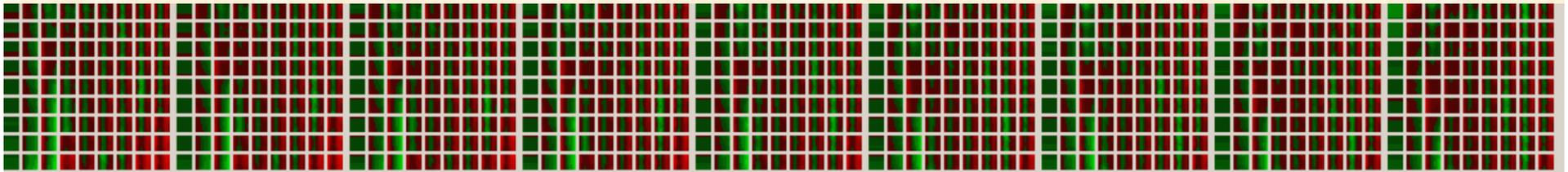
as in TableLens

5D
9 samp/D





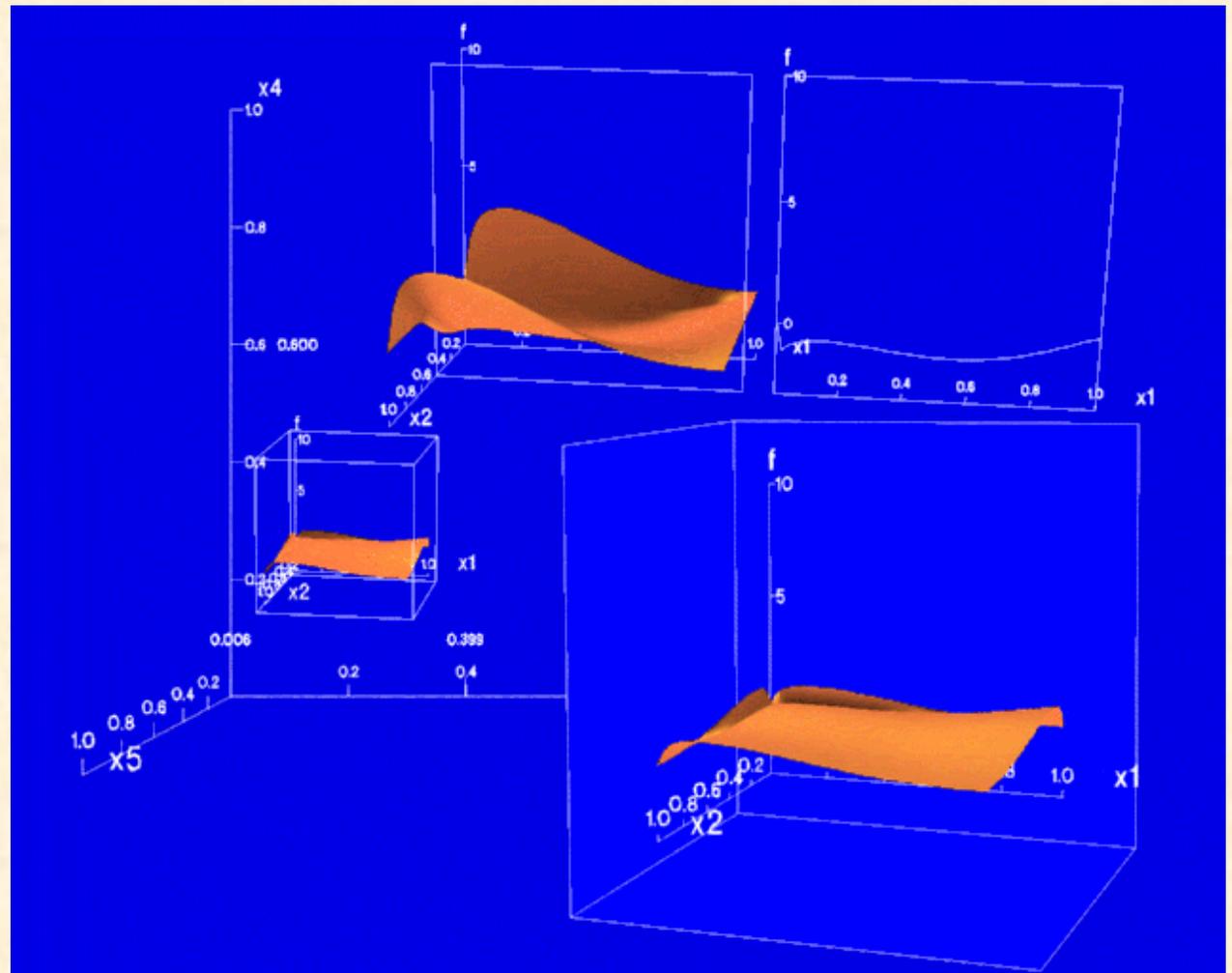
- 5D
9 sample/D



Nested Coordinate Frames

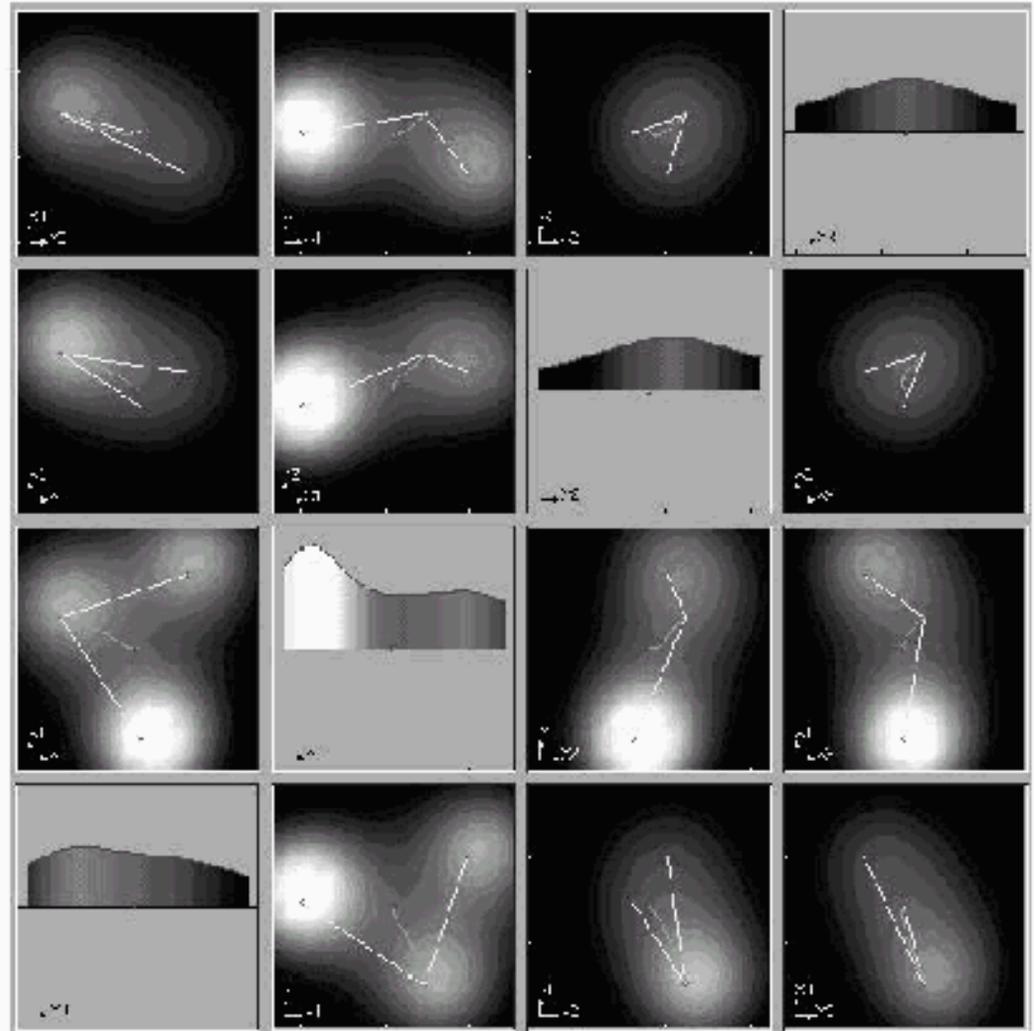
- Feiner, “Worlds within Worlds”

-

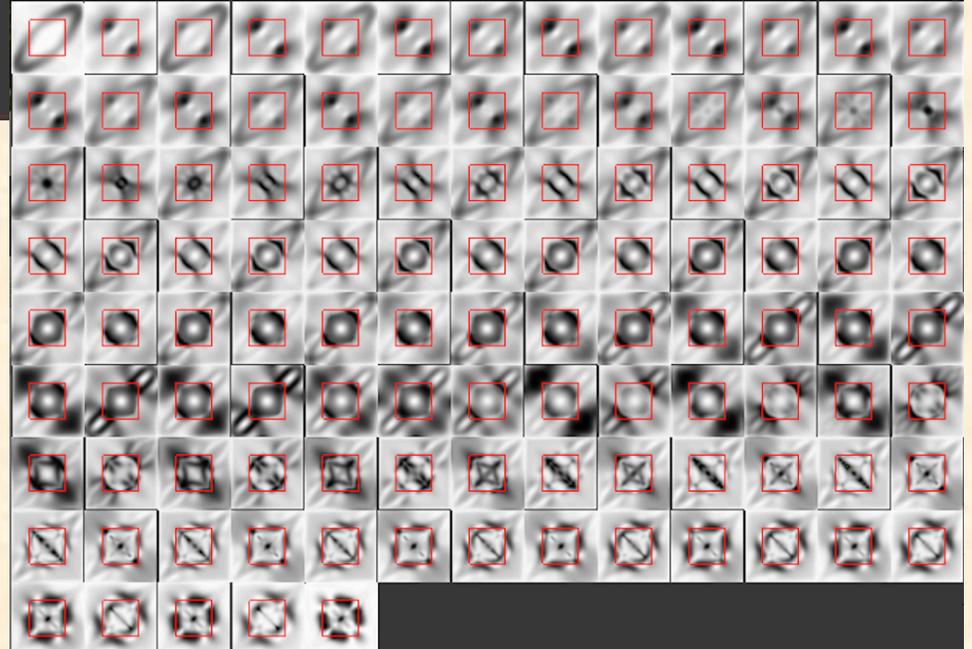
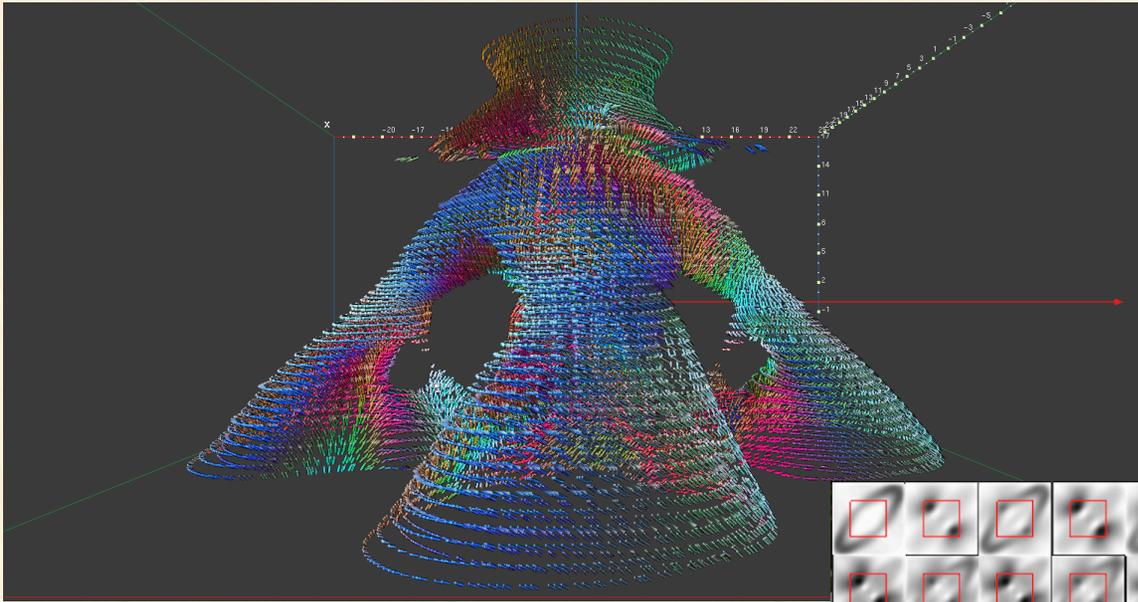


Slicing

- Van Wijk, “HyperSlice”



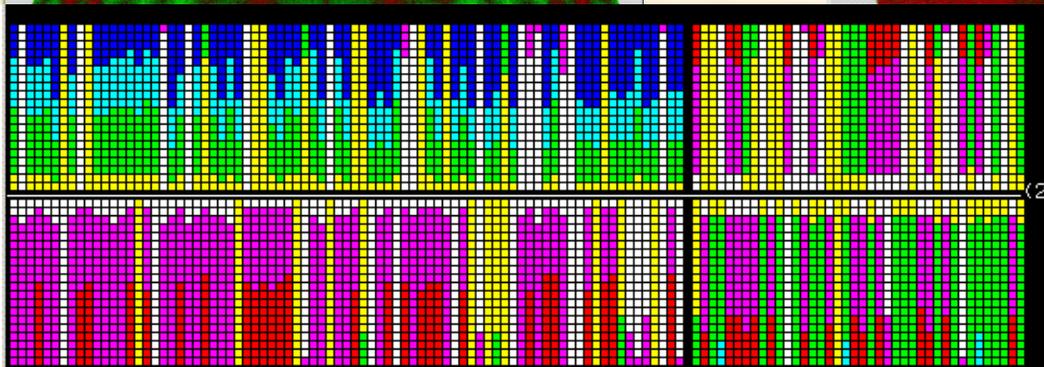
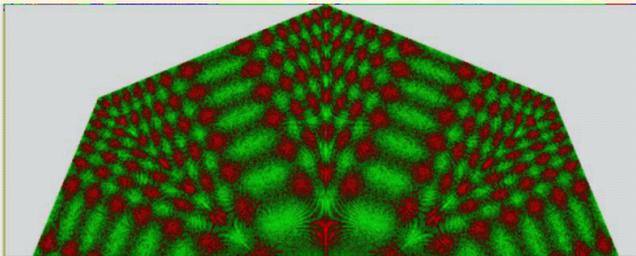
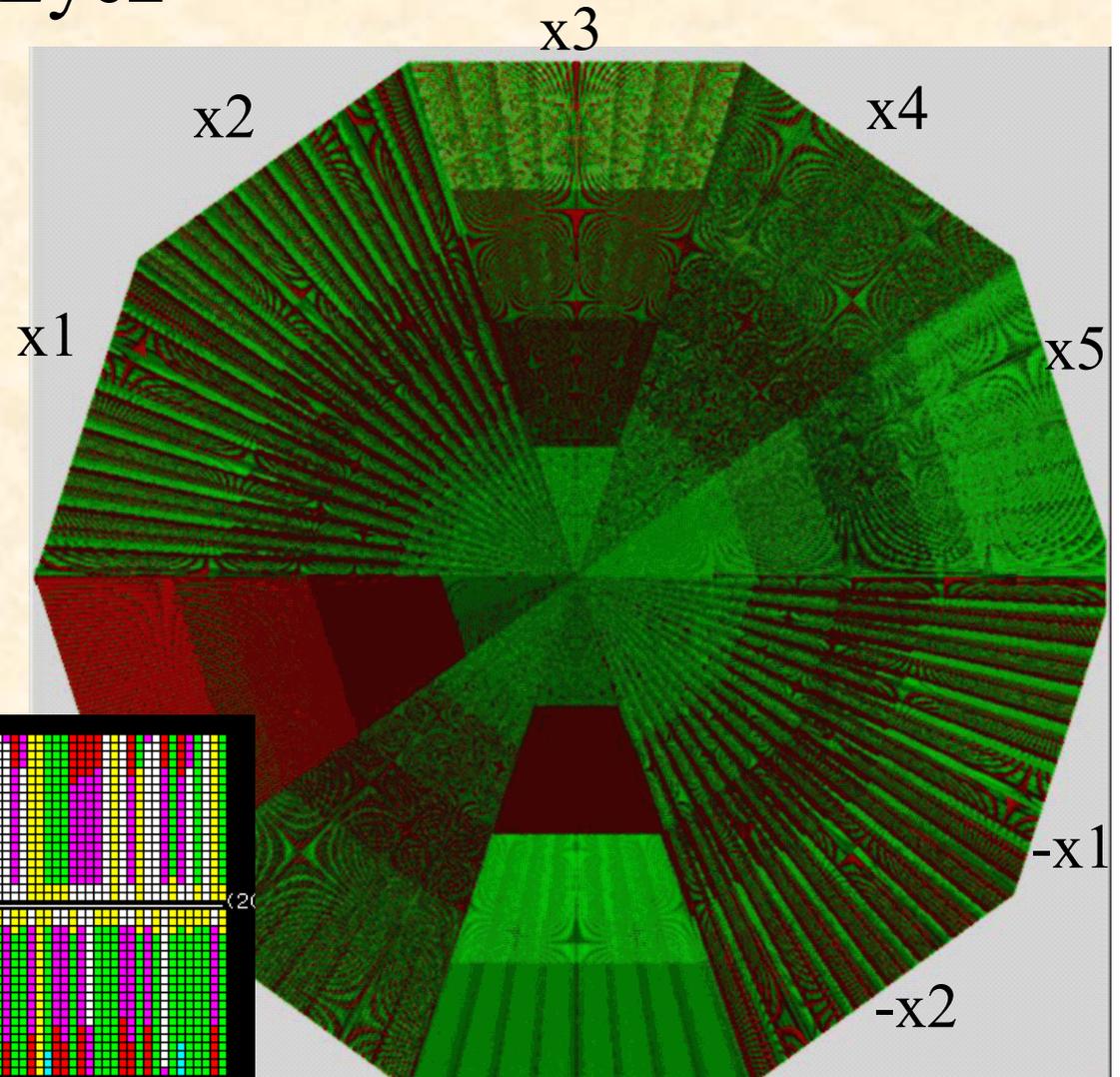
Slicing



Radial Focus+Context

- Jayaraman, “PolarEyez”

- infovis.cs.vt.edu



Comparison

- Hierarchical axes (Mihalisin):
 -
- Nested coordinate frames (Worlds in Worlds)
 -
- Slicing (HyperSlice):
 -
- Radial Focus+Context (PolarEyez)
 -

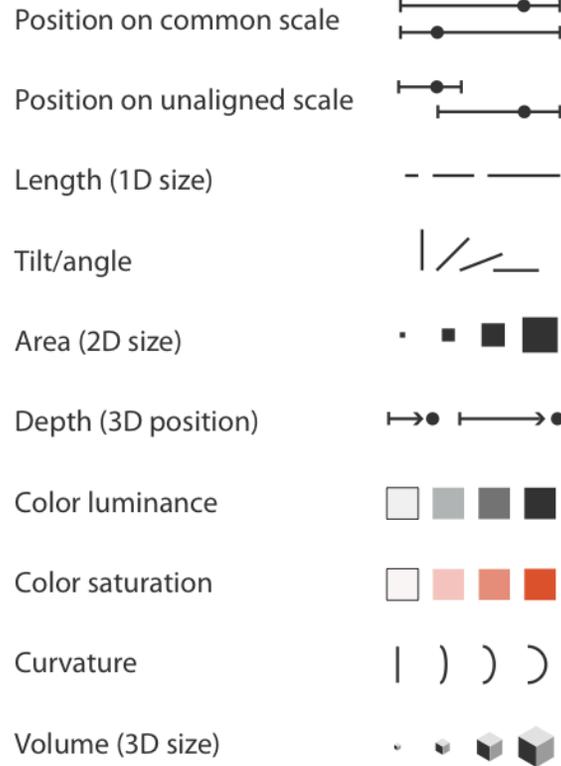
Comparison

- Hierarchical axes (Mihalisin):
 - < 6d by 10 samples, ALL slices, view 2d at a time
- Nested coordinate frames (Worlds in Worlds)
 - < 5-8d, continuous, no overview, 3d hardware
- Slicing (HyperSlice):
 - < 10d by 100 samples, 2d slices
- Radial Focus+Context (PolarEyes)
 - < 10d by 1000 samples, overview, all D uniform, rays

Review (9/17)

Channels: Expressiveness Types and Effectiveness Ranks

➔ **Magnitude Channels: Ordered Attributes**



➔ **Identity Channels: Categorical Attributes**



Most
Effectiveness
Least

Figure 5.6. Channels ranked by effectiveness according to data and channel type. Ordered data should be shown with the magnitude channels, and categorical data with the identity channels.

Review (9/17)

- Many ways to look at tables; multi-D data; what are they?
 - Glyph (face; star glyphs;)
 - Coordinates (star coordinates; parallel coordinates)
 - Table lens

Upcoming (9/17)

- Homework 2 (out tonight, due 9/29)
- Proposal due (10/20)
 - Title of your final report (begin with the title of the project first)
 - Meeting with the client / advisors
 - Data abstraction
 - Task abstraction
 - Initial design

Mandatory: talk to Jian about your project topic next Monday / Wednesday after class 2:30-3:30pm. You **MUST** have a client.