

1

Today's Class

- Useful terminology
 - Degrees of Freedom
 - Compliance and back-drive
 - Actuator saturation
 - Slip
- Mechanics: 3 most common mobility actuators
 - Legs, wheels (we leave wings for future)
- If we have time:
 - Other mobile actuators
 - Wings, walking wheels, passive flight, swimming, ...

© Cynthia Matuszek 2020, except for third-party content

2

Locomotion in Nature

Type of motion	Resistance to motion	Basic kinematics of motion
Flow in a Channel 	Hydrodynamic forces	Eddies
Crawl 	Friction forces	Longitudinal vibration
Sliding 	Friction forces	Transverse vibration
Running 	Loss of kinetic energy	Oscillatory movement of a multi-link pendulum
Jumping 	Loss of kinetic energy	Oscillatory movement of a multi-link pendulum
Walking 	Gravitational forces	Rolling of a polygon (see figure 2.2)

© Cynthia Matuszek

3

Locomotion in Nature

- Concepts found in nature
 - Difficult to imitate technically
 - Why?
- Most technical systems use wheels or caterpillars
 - Rolling is most efficient, but not found in nature
 - Nature never invented the wheel!
- However, a walking biped is close to rolling

© Cynthia Matuszek 2020, except for third-party content

4

Walking or Rolling?

	Walking	Rolling
Number of Actuators	More	Fewer
Structural Complexity	Higher	Lower
Control Expense	Higher <i>(walking = complicated)</i>	Lower <i>(wheels = simple)</i>
Energy Efficiency (depends on terrain)	Worse <i>(depends)</i>	Better <i>(depends)</i>
Movement of masses (walking adds up-down)	More movement	Less movement

© Cynthia Matuszek 2020, except for third-party content

5

Walking or Rolling? (II)

1. Number of actuators
2. Structural complexity
3. Control expense
4. Energy efficient
 - Terrain (flat ground, soft ground, climbing, rubble, stairs...)
5. Movement of physical masses
 - Walking / running includes up and down movement
 - Some extra losses

© Cynthia Matuszek 2020, except for third-party content

6

Passive Dynamic Walking

- Gravity-powered walking with bipedal gait



We saw this last time – now we're looking at similarity to rolling

Nagoya Inst. Tech. June 2005. About 4000 steps (about 35 minutes). Yoshito Ikemata, Akihito Sano & Hideo Fujimoto

© Cynthia Matuszek 2020, except for third-party content. <https://www.youtube.com/watch?v=CK8lFFGmi7Y>

7

Characterizing Locomotion

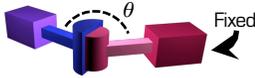
- Locomotion is:
 - Physical interaction between robot and environment
 - Concerned with **interaction forces** and the **mechanisms and actuators** that generate them
- The most important issues in locomotion are:
 - Stability**
 - Center of gravity
 - Static/dynamic stabilization
 - Inclination of terrain
 - Type of environment**
 - Water, air, soft or hard ground
 - Characteristics of contact**
 - Contact point(s)
 - Contact area
 - Angle of Contact
 - Friction

© Cynthia Matuszek 2020, except for third-party content. Adapted from © P. Stegeman, ETH Zurich, ASI

8

Degrees of Freedom

- DoFs: Number of independent parameters that define the **state** (not location) of a physical system
- How many numbers define how parts can move with respect to each other?



- This arm can be straight, or bent some amount
- To know its state, you need to know **1** thing: θ

© Cynthia Matuszek 2020, except for third-party content. en.wikipedia.org/wiki/Degrees_of_freedom_%28mechanics%29

9

Degrees of Freedom

- DoFs
 - Number of independent parameters that define the **state** (not location!) of a physical system.



© Cynthia Matuszek 2020, except for third-party content. https://en.wikipedia.org/wiki/Degrees_of_freedom_%28mechanics%29

10

Compliance / Back-drive

- Motion of a DoF in response to external force
 - High compliance: moves a lot when stressed (pushed)
 - Low compliance: stiff when stressed
- Active compliance: software recognizes motion
- Passive compliance: mechanical structure
- Back-driveable means that you can physically move it (without breaking it) – passive compliance
 - If you grab my arm and bend it, the elbow joint moves
 - When I'm asleep, anyway...
 - Mostly a product of motor and gear type

© Cynthia Matuszek 2020, except for third-party content

11

Saturation

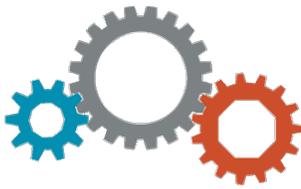
- Actuator saturation: physical performance limit
 - Saturation is (generally) a nonlinear response
 - Example: The more power you push into a motor, the less extra motion you get per unit
 - Eventually you get none – it's **saturated**
- Example: electric motor
 - Driving circuit has amp limit
 - Result: torque or speed limit
 - When limit is exceeded, parts start to burn out
 - It's a hard, nonlinear limit

© Cynthia Matuszek 2020, except for third-party content

12

Slip

- Slip: some interface fails to catch
 - Gears, wheels, belts...
 - Examples: tires on snow; overdriven motor
- More power in \neq more movement out



© Cynthia Matusek 2020, except for third-party content

13

Legged Motion

- Fewer legs \rightarrow more complicated mechanically
 - Static stability
 - With point contact – at least three legs for static stability
 - With surface contact – at least one leg required
- During walking some legs are lifted
 - Usually half
 - Losing stability?
- For static walking 4+ legs are required
 - Animals usually move two legs at a time
 - Humans require more than a year to learn to do this!

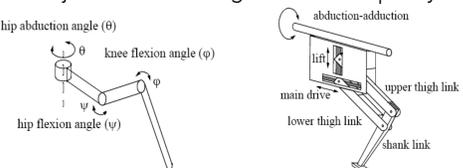


© Cynthia Matusek 2020, except for third-party content Adapted from © R. Siegwart, ETH Zürich – AT16

14

Leg Joints (DoFs)

- 2+ DoFs to move a leg forward: **lift** and **swing**
- Three DoFs for each leg in most cases
 - 4th DOF for the ankle joint
 - Might improve walking and stability
 - More joints increase design / control complexity



© Cynthia Matusek 2020, except for third-party content Adapted from © R. Siegwart, ETH Zürich – AT16

15

Gait Options

- Gait: the number of distinct event sequences
 - Distinct sequence of lift and release events of individual legs**
 - Depends on number of legs
- Number of possible events N with k legs:

$$N = (2k - 1)!$$
- For a biped (k=2), number of possible events N:

$$N = (2k-1)! = 3! = 3 \cdot 2 \cdot 1 = 6$$
- For a robot with 6 legs (hexapod):

$$N = 11! = 39,916,800$$

© Cynthia Matusek 2020, except for third-party content Adapted from © R. Siegwart, ETH Zürich – AT16

16

Gait Options

- Two legs (biped) can have four different states:
 - Both legs down
 - Right leg down, left leg up
 - Right leg up, left leg down
 - Both legs up
- Event sequence:** one state to another and back

● Leg down
○ Leg up

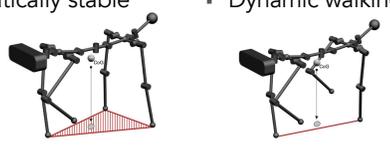
1 \rightarrow 2 \rightarrow 1 ● ● ● \rightarrow turning on right leg	2 \rightarrow 3 \rightarrow 2 ● ○ ● \rightarrow walking running
1 \rightarrow 3 \rightarrow 1 ● ● ● \rightarrow turning on left leg	2 \rightarrow 4 \rightarrow 2 ● ○ ○ \rightarrow hopping right leg
1 \rightarrow 4 \rightarrow 1 ● ○ ● \rightarrow hopping with two legs	3 \rightarrow 4 \rightarrow 3 ● ○ ○ \rightarrow hopping left leg

© Cynthia Matusek 2020, except for third-party content Adapted from © R. Siegwart, ETH Zürich – AT17

17

Static vs. Dynamic Walking

- Statically stable
 - Bodyweight supported by at least three legs
 - Even if all joints freeze, the robot will not fall
 - Safe \blacklozenge slow and inefficient
- Dynamic walking
 - Robot will fall if not continuously moving
 - Fewer than three legs in ground contact
 - Fast, efficient \blacklozenge harder actuation and control



© Cynthia Matusek 2020, except for third-party content

18

Adapted from © R. Siegwart, ETH Zürich – 2011

Static vs. Dynamic Gait

- Whether robot is stable at all times during walking (static)

6-legged, Static
4-legged, Dynamic

© Cynthia Matuszek 2020, except for third-party content

19

Dynamic Quadruped

- Boston Dynamics Spot

Boston Dynamics

© Cynthia Matuszek 2020, except for third-party content <https://www.youtube.com/watch?v=kqaO45SvaO4>

20

Dynamic Quadruped (II)

- Boston Dynamics Spot

Boston Dynamics

© Cynthia Matuszek 2020, except for third-party content <https://www.youtube.com/watch?v=fUvU3Kzoio>

21

Dynamic Quadruped (III)

- Boston Dynamics BigDog

Boston Dynamics

© Cynthia Matuszek 2020, except for third-party content <https://www.youtube.com/watch?v=cNZPRsvwuzQ>

22

Dynamic Quadruped

- Boston Dynamics BigDog

Adapted from © R. Siegwart, ETH Zürich – 2011

© Cynthia Matuszek 2020, except for third-party content

23

All About Wheels

- Most appropriate solution for many applications
- Three wheels guarantee stability
- With more than three wheels an appropriate **suspension** is required
- Selection of wheels depends on the application

Adapted from © R. Siegwart, ETH Zürich – 2011

© Cynthia Matuszek 2020, except for third-party content

24

Mountings and Axles

Mounting axis
Axle

Direction of rotation
Direction of translation

© Cynthia Matuszek 2020, except for third-party content

25

4 Basic Wheel Types

- Standard wheel
 - Two degrees of freedom
 - Rotation around the (motorized) wheel axle and the contact point
- Castor wheel
 - Three degrees of freedom
 - Rotation around the wheel axle, the contact point and the castor axle

© Cynthia Matuszek 2020, except for third-party content Adapted from © R. Siegwart, ETH Zürich – /26

26

Basic Wheel Types

- Swedish (Mecanum, Ilon) wheel
 - Three degrees of freedom
 - Rotation around the (motorized) wheel axle, rollers, contact point

© Cynthia Matuszek 2020, except for third-party content Adapted from © R. Siegwart, ETH Zürich – /27

27

Omni Wheels

© Cynthia Matuszek 2020, except for third-party content https://www.youtube.com/watch?v=8sH1a511_28

28

Basic Wheel Types

- Ball or spherical wheel
 - Suspension not solved

© Cynthia Matuszek 2020, except for third-party content <https://en.wikipedia.org/wiki/Bal29>

29

Characterization: Stability

- Stability of a vehicle is guaranteed with 3 wheels
 - If center of gravity is within the contact triangle
- Stability is improved by 4+ wheels
 - However, requires a flexible suspension
 - It's hyperstatic (see later)

© Cynthia Matuszek 2020, except for third-party content Adapted from © R. Siegwart, ETH Zürich – /30

30

Characterization: Stability (II)



- **Bigger wheels** overcome **higher obstacles**
 - But require higher torque or reductions in the gear box
- Most wheel arrangements require high control effort
 - Non-holonomic – we'll get into that in Ch. 3
- Combining actuation and steering on a single wheel
 - Makes the design complex
 - Adds errors for **odometry**
 - Data from motion sensors used to estimate position



Adapted from © R. Siegwart, ETH Zürich – ASI

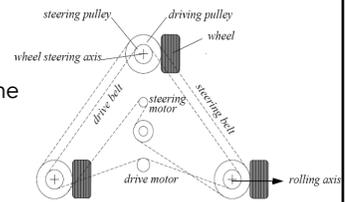
31

31

Synchro Drive



- All wheels are actuated by one motor
 - Defines the speed of the vehicle
- All wheels steered synchronously by second motor
 - Sets the heading of the vehicle
- Orientation in space of robot frame always the same
- Not possible to control orientation of robot frame



© 2009 Marcell, 2020, except for third-party content

Adapted from © R. Siegwart, ETH Zürich – ASI

32