

Adversarial Search Aka Games

Chapter 5

Some material adopted from notes by Charles R. Dyer, U of Wisconsin-Madison

Overview

- Game playing
 - -State of the art and resources
 - -Framework
- Game trees
 - -Minimax
 - -Alpha-beta pruning
 - -Adding randomness

Why study games?

- Interesting, hard problems that require minimal "initial structure"
- Clear criteria for success
- A way to study problems involving {hostile, adversarial, competing} agents and the uncertainty of interacting with the natural world
- People have used them to assess their intelligence
- Fun, good, easy to understand, PR potential
- Games often define very large search spaces
 –chess 35¹⁰⁰ nodes in search tree, 10⁴⁰ legal states

State of the art

• Chess:

- Deep Blue beat Gary Kasparov in 1997
- Garry Kasparav vs. Deep Junior (Feb 2003): tie!
- Kasparov vs. X3D Fritz (November 2003): tie!
- Checkers: Chinook is the world champion
- Checkers: has been solved exactly it's a draw!
- Go: Computers starting to achieve expert level
- **Bridge**: Expert computer players exist, but no world champions yet
- Poker: Poki regularly beats human experts
- Check out the <u>U. Alberta Games Group</u>

Chinook

- Chinook is the World Man-Machine Checkers Champion, developed by researchers at the University of Alberta
- It earned this title by competing in human tournaments, winning the right to play for the (human) world championship, and eventually defeating the best players in the world
- Play <u>Chinook</u> online
- <u>One Jump Ahead</u>: Challenging Human Supremacy in Checkers, Jonathan Schaeffer, 1998
- See <u>Checkers Is Solved</u>, J. Schaeffer, et al., Science, v317, n5844, pp1518-22, AAAS, 2007.

The board set for play



Red to play



Chess early days



- **1948**: Norbert Wiener's <u>*Cybernetics*</u> describes how a chess program could be developed using a depth-limited minimax search with an evaluation function
- 1950: Claude Shannon publishes <u>Programming a</u> <u>Computer for Playing Chess</u>
- **1951**: Alan Turing develops on paper the first program capable of playing a full game of chess
- **1962**: Kotok and McCarthy (MIT) develop first program to play credibly
- 1967: <u>Mac Hack Six</u>, by Richard Greenblatt et al. (MIT) defeats a person in regular tournament play

Ratings of human & computer chess champions







Chess Grand Master Garry Kasparov, left, comtemplates his next move against IBM's Deep Blue chess computer while Chung-Jen Tan, manager of the Deep Blue project looks on iduring the first game of a six-game rematch between Kasparov and Deep Blue in this file photo from 1997. The computer program made history by becoming the first to beat a world chess champion, Kasparov, at a serious game. Photo: Adam Nadel/Associated Press

Othello: Murakami vs. Logistello





open sourced

Takeshi Murakami World Othello Champion

- 1997: The Logistello software crushed Murakami, 6 to 0
- Humans can not win against it
- Othello, with 10²⁸ states, is still not solved



Google DeepMind Challenge Match 8-15 March 2016



2016

AlphaGo

02:00

Google DeepMind Challenge Match 8 - 15 March 2016

Lee Sedol

CARNEGIE MELLON ARTIFICIAL INTELLIGENCE BEATS TOP POKER PROS

2017

Historic win at Rivers Casino is first against best human players

By <u>Byron Spice</u>



Tuomas Sandholm (center) and Ph.D. student Noam Brown developed Libratus.

How can we do it?

Typical simple case for a game

- 2-person game
- Players alternate moves
- Zero-sum: one player's loss is the other's gain
- **Perfect information**: both players have access to complete information about state of game. No information hidden from either player
- No chance (e.g., using dice) involved
- Examples: Tic-Tac-Toe, Checkers, Chess, Go, Nim, Othello
- But not: Bridge, Solitaire, Backgammon, Poker, Rock-Paper-Scissors, ...

Can we use ...

- Uninformed search?
- Heuristic search?
- Local search?
- Constraint based search?

How to play a game

- A way to play such a game is to:
 - -Consider all the legal moves you can make
 - -Compute new position resulting from each move
 - -Evaluate each to determine which is best
 - -Make that move
 - –Wait for your opponent to move and repeat
- Key problems are:
 - -Representing the "board" (i.e., game state)
 - -Generating all legal next boards
 - -Evaluating a position

Evaluation function

- Evaluation function or static evaluator used to evaluate the "goodness" of a game position
 - Contrast with heuristic search where evaluation function is non-negative estimate of **cost** from start node to goal passing through given node
- <u>Zero-sum</u> assumption permits single function to describe goodness of board for both players
 - -f(n) >> 0: position n good for me; bad for you
 - $-f(n) \ll 0$: position n bad for me; good for you
 - -f(n) near 0: position n is a neutral position
 - $-\mathbf{f}(\mathbf{n}) = +\mathbf{infinity}$: win for me
 - $-\mathbf{f}(\mathbf{n}) = -\mathbf{infinity}$: win for you

Evaluation function examples

• For Tic-Tac-Toe

f(n) = [# my open 3lengths] - [# your open 3lengths]Where 3length is complete row, column, or diagonal and an open one is one that has no opponent marks

• Alan Turing's function for chess

-f(n) = w(n)/b(n) where w(n) = sum of the pointvalue of white's pieces and b(n) = sum of black's

Traditional piece values are: pawn:1; knight:3;bishop:3; rook: 5; queen: 9

Evaluation function examples

- Most evaluation functions specified as a weighted sum of positive features
 f(n) = w₁*feat₁(n) + w₂*feat₂(n) + ... + w_n*feat_k(n)
- Example features for chess are piece count, piece values, piece placement, squares controlled, etc.
- IBM's chess program <u>Deep Blue</u> (circa 1996) had >8K features in its evaluation function

But, that's not how people play

- People use *look ahead*
 - i.e., enumerate actions, consider opponent's possible responses, REPEAT
- Producing a *complete* game tree is only possible for simple games
- So, generate a partial game tree for some number of <u>plys</u>
 - -Move = each player takes a turn
 - -Ply = one player's turn
- What do we do with the game tree?



Game trees



- Problem spaces for typical games are trees
- Root node is current board configuration; player must decide best single move to make next
- Static evaluator function rates board position f(board):real, >0 for me; <0 for opponent
- Arcs represent possible legal moves for a player
- If my turn to move, then root is labeled a "MAX" node; otherwise it's a "MIN" node
- Each tree level's nodes are all MAX or all MIN; nodes at level i are of opposite kind from those at level i+1

Game Tree for Tic-Tac-Toe



Minimax procedure

- Create MAX node with current board configuration
- Expand nodes to some **depth** (a.k.a. **plys**) of lookahead in game
- Apply evaluation function at each leaf node
- *Back up* values for each non-leaf node until value is computed for the root node
 - -At MIN nodes: value is **minimum** of children's values
 - -At MAX nodes: value is **maximum** of children's values
- Choose move to child node whose backed-up value determined value at root

Minimax theorem

• Intuition: assume your opponent is at least as smart as you and play accordingly

-If she's not, you can only do better!

• <u>Von Neumann</u>, J: *Zur Theorie der Gesellschaftsspiele* Math. Annalen. **100** (1928) 295-320

For every 2-person, 0-sum game with finite strategies, there is a value V and a mixed strategy for each player, such that (a) given player 2's strategy, best payoff possible for player 1 is V, and (b) given player 1's strategy, best payoff possible for player 2 is -V.

• You can think of this as:

-Minimizing your maximum possible loss

-Maximizing your minimum possible gain

Minimax Algorithm

Static evaluator value

This is the move selected by minimax



Partial Game Tree for Tic-Tac-Toe



Why use backed-up values?

- Intuition: if evaluation function is good, doing look ahead and backing up values with Minimax should be better
- Non-leaf node N's backed-up value is value of best state that MAX can reach at depth h if MIN plays well
 - "well" : same criterion as MAX applies to itself
- If e is good, then backed-up value is better estimate of STATE(N) goodness than e(STATE(N))
- Use lookup horizon h because time to choose move is limited

Minimax Tree



Is that all there is to simple games?

Alpha-beta pruning

- Improve performance of the minimax algorithm through **alpha-beta pruning**
- *"If you have an idea that is surely bad, don't take the time to see how truly awful it is"* -- Pat Winston



- We don't need to compute the value at this node
- No matter what it is, it can't affect value of the root node

Alpha-beta pruning

- Traverse search tree in depth-first order
- At MAX node n, **alpha(n)** = max value found so far
- At MIN node n, **beta(n)** = min value found so far
 - -Alpha values start at $-\infty$ and only increase, while beta values start at $+\infty$ and only decrease
- Beta cutoff: Given MAX node N, cut off search below N (i.e., don't examine any more of its children) if alpha(N) >= beta(i) for some MIN node ancestor i of N
- Alpha cutoff: stop searching below MIN node N if beta(N)<=alpha(i) for some MAX node ancestor i of N








Alpha-Beta Tic-Tac-Toe Example



Alpha-Beta Tic-Tac-Toe Example



Another alpha-beta example



Alpha-Beta Tic-Tac-Toe Example 2























































```
function MAX-VALUE (state, \alpha, \beta)
;; \alpha = best MAX so far; \beta = best MIN
if TERMINAL-TEST (state) then return
 UTILITY (state)
V := -\infty
for each s in SUCCESSORS (state) do
    v := MAX (v, MIN-VALUE (s, \alpha, \beta))
    if v \geq \beta then return v
                                          Alpha-beta
    \alpha := MAX (\alpha, v)
end
                                            algorithm
return v
function MIN-VALUE (state, \alpha, \beta)
if TERMINAL-TEST (state) then return
 UTILITY (state)
V := \infty
for each s in SUCCESSORS (state) do
    v := MIN (v, MAX-VALUE (s, \alpha, \beta))
    if v \leq \alpha then return v
     \beta := MIN (\beta, v)
end
return v
```

Effectiveness of alpha-beta

- Alpha-beta guaranteed to compute same value for root node as minimax, but with \leq computation
- Worst case: no pruning, examine b^d leaf nodes, where nodes have b children & d-ply search is done
- **Best case:** examine only (2b)^{d/2} leaf nodes
 - You can search twice as deep as minimax!
 - -Occurs if each player's best move is 1st alternative
- In Deep Blue's alpha-beta pruning, average branching factor at node was ~6 instead of ~35!

Other Improvements

- Adaptive horizon + iterative deepening
- Extended search: retain k>1 best paths (not just one) extend tree at greater depth below their leaf nodes to help dealing with "horizon effect"
- **Singular extension**: If move is obviously better than others in node at horizon h, expand it
- Use transposition tables to deal with repeated states
- Null-move search: assume player forfeits move; do a shallow analysis of tree; result must surely be worse than if player had moved. Can be used to recognize moves that should be explored fully.