CMSC 341

Splay Trees

Splay Trees

Concept

- adjust tree in response to accesses to make common operations efficient
- after access node is moved to root by *splaying*

Performance

- amortized such that m operations take O(m lg n) where n is the number of insertions

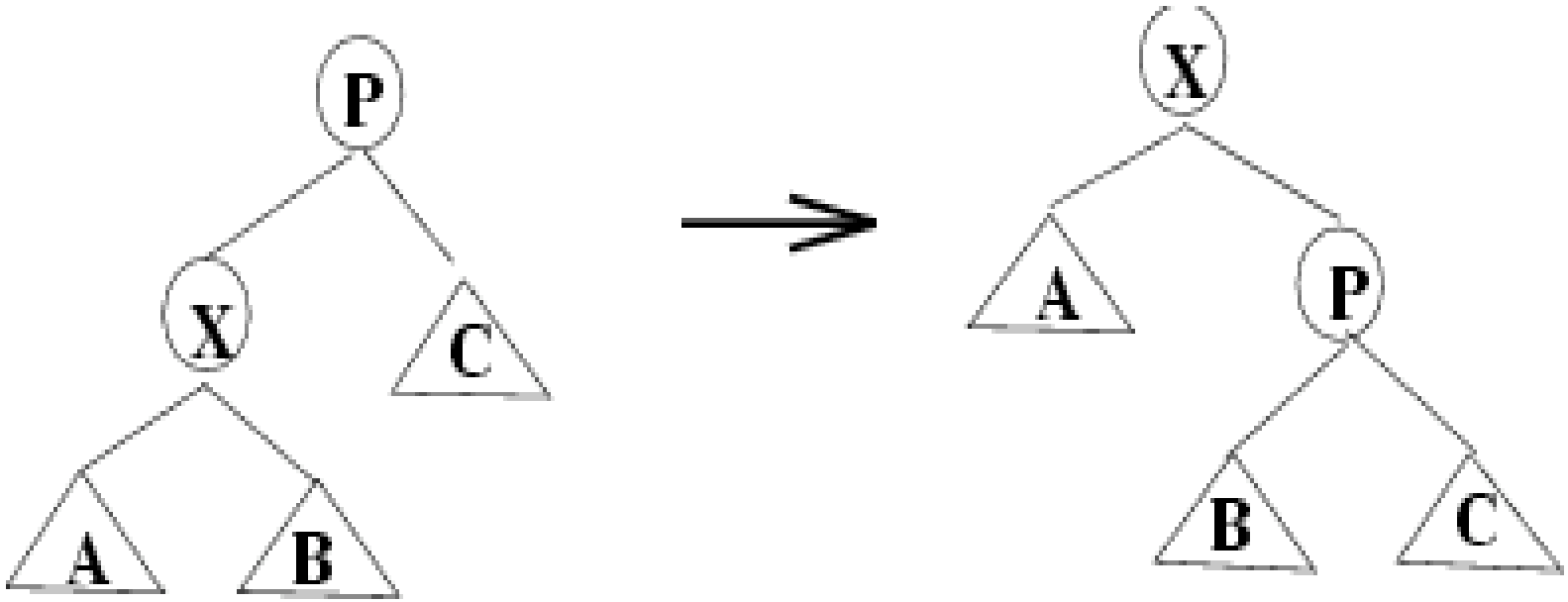
Splay Operation

Traverse tree from node x to root, rotating along the way until x is the root

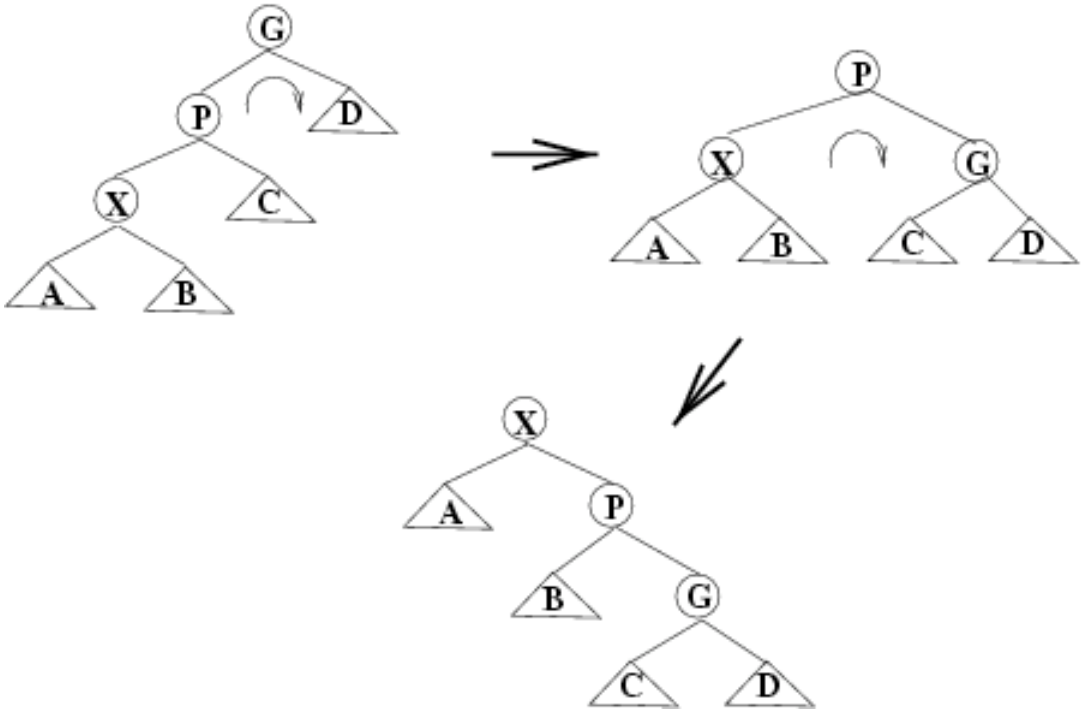
Each rotation

- If x is root, do nothing.
- If x has no grandparent, rotate x about its parent.
- If x has a grandparent,
  - if x and its parent are both left children or both right children, rotate the parent about the grandparent, then rotate x about its parent
  - if x and its parent are opposite type children (one left and the other right), rotate x about its parent, then rotate x about its new parent (former grandparent)

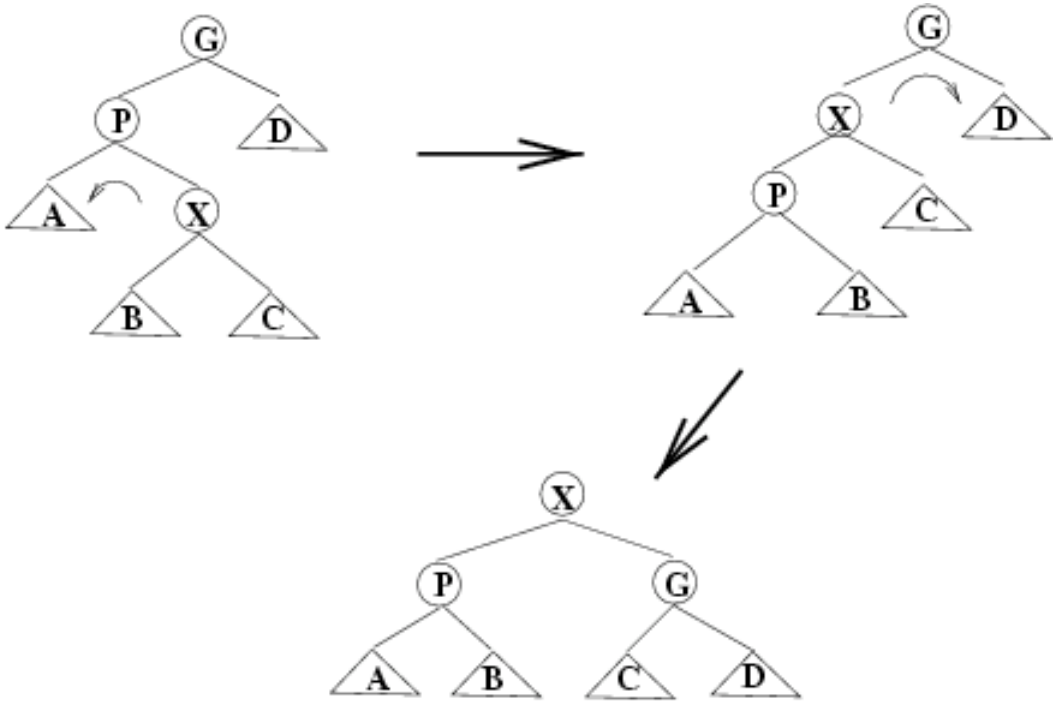
Node has no grandparent



Node and Parent are Same Side
Zig-Zig



Node and Parent are Different Sides
Zig-Zag



Operations in Splay Trees

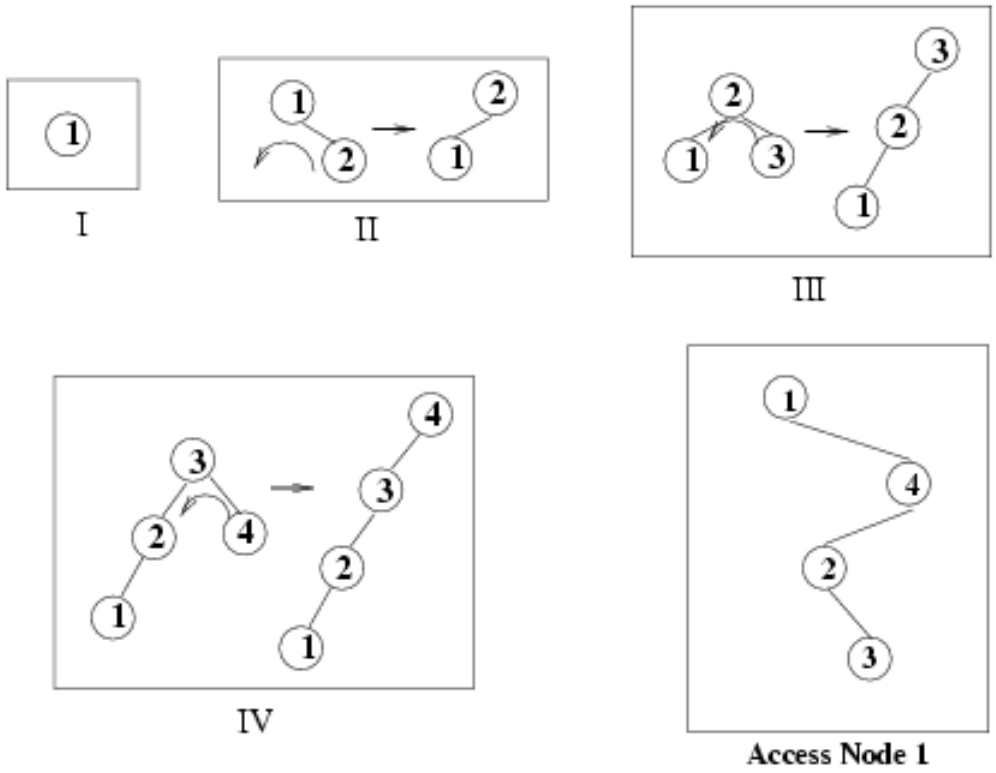
insert

- first insert as in normal binary search tree
- then splay inserted node
- if there is a duplicate, the node holds the duplicate element is splayed

find

- search for node
- if found, splay to root; otherwise splay last node on path

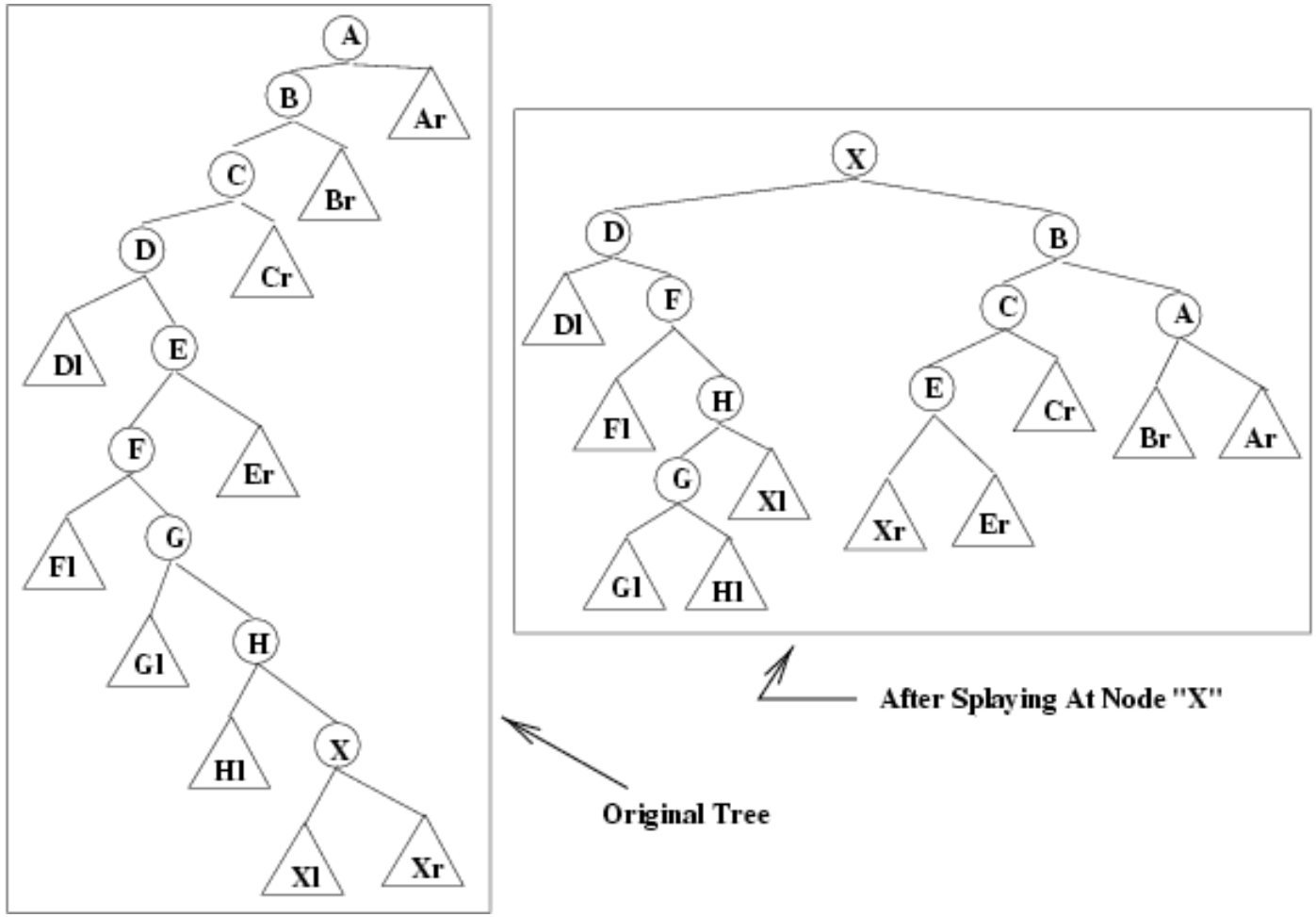
Insertion in order into a Splay Tree



Operations on Splay Trees (cont)

remove

- splay selected element to root
- disconnect left and right subtrees from root
- do one of:
  - splay max item in T_L (then T_L has no right child)
  - splay min item in T_R (then T_R has no left child)
- connect other subtree to empty child
- if the item to be deleted is not in the tree, the node last visited in the search is splayed


A
B
Ar
C
Br
D
Cr
Dl
E
F
Er
Fl
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H
Hl
X
Xl
Xr
X
D
B
Dl
F
C
A
Fl
H
E
Cr
Br
Ar
G
Xl
Xr
Er
Gl
Hl
After Splaying At Node "X"
Original Tree

Performance of Splay Trees

insert

- regular bst insertion -- O(depth)
- splay: O(1) for each rotation, O(depth) rotations