

Class Website



<https://redirect.cs.umbc.edu/courses/graduate/691cv/>

Lecture Slides will be uploaded *after* the lecture
(*usually in 1-2 days*)

Access to Google Chat

We will wait until the Waitlist Deadline (Friday) 😊

After that, the TA will add you.

Sign-Up for Scribing →



- All students are required to scribe **at least twice** during the semester.
 - You can sign-up for a preferred week
- Scribing = high-quality detailed notes during the lectures in that week, typeset using Overleaf/LaTeX
 - Template is on the class website. Hand-drawn figures are allowed.
- *Notes for Monday lectures are due before class next Monday*
- *Notes for Wednesday lectures are due before class next Wednesday*

Email your notes as PDF, with subject: "[Scribing Submission] <lecture-date>" to gokhale@umbc.edu AND ssaha2@umbc.edu													
We may deviate a bit from the planned topics listed below.													
to sign-up, enter your name below in an empty slot -- do not overwrite your classmates' entries!													
Lecture Date	Day	Planned Topic	Notes Due	Scribe 1	Scribe 2	Scribe 3	Lecture Date	Day	Planned Topic	Notes Due	Scribe 1	Scribe 2	Scribe 3
29-Jan	M	Intro	5-Feb	Olivia Amaral			31-Jan	W	Image Formation				
5-Feb	M	Filtering I	12-Feb	Olivia Amaral			7-Feb	W	Filtering II				
12-Feb	M	Features I	19-Feb	Jabril Hall			14-Feb	W	Features II				
19-Feb	M	Features III	26-Feb				21-Feb	W	no scribing				
26-Feb	M	no scribing					28-Feb	W	ML for CV				
4-Mar	M	ML for CV (NN)	11-Mar				6-Mar	W	ML for CV (GD)				
11-Mar	M	Pytorch Tutorial	18-Mar				13-Mar	W	Object Detection				
18-Mar	M	no scribing (Spring Break)					20-Mar	W	no scribing (Spring Break)				
25-Mar	M	Image Transformations	1-Apr				27-Mar	W	Homographies				
1-Apr	M	no scribing (Midterm)					3-Apr	W	Camera Models				
8-Apr	M	Epipolar Geometry	15-Apr				10-Apr	W	Stereo				
15-Apr	M	V&L	22-Apr				17-Apr	W	Image Synthesis				
22-Apr	M	Robustness	29-Apr				24-Apr	W	buffer				
29-Apr	M	no scribing (Guest Lecture I)					1-May	W	no scribing (Guest Lecture II)				
6-May	M	no scribing (Guest Lecture III)					8-May	W	no scribing (Project Presentations)				
13-May	M	no scribing (Project Presentations)											

The LaTeX template has been released on the class website.

Please create an account on <https://overleaf.com> (it is free!)

For a tutorial on how to use LaTeX with Overleaf, visit:

[https://www.overleaf.com/learn/latex/Learn LaTeX in 30 minutes](https://www.overleaf.com/learn/latex/Learn%20LaTeX%20in%2030%20minutes)

(this link is on the website)



PPR Seminar

Advances in Perception, Prediction, and Reasoning



Dr. Yezhou Yang



Associate Professor,
School of Computing & AI, Arizona State University

<https://yezhouyang.engineering.asu.edu/>

**Visual Concept Learning Beyond Appearances:
Modernizing a Couple of Classic Ideas**

February 8, 2024 3:30 – 4:30 PM

ITE 325-B or Webex: <https://umbc.webex.com/meet/gokhale>

Lecture 2

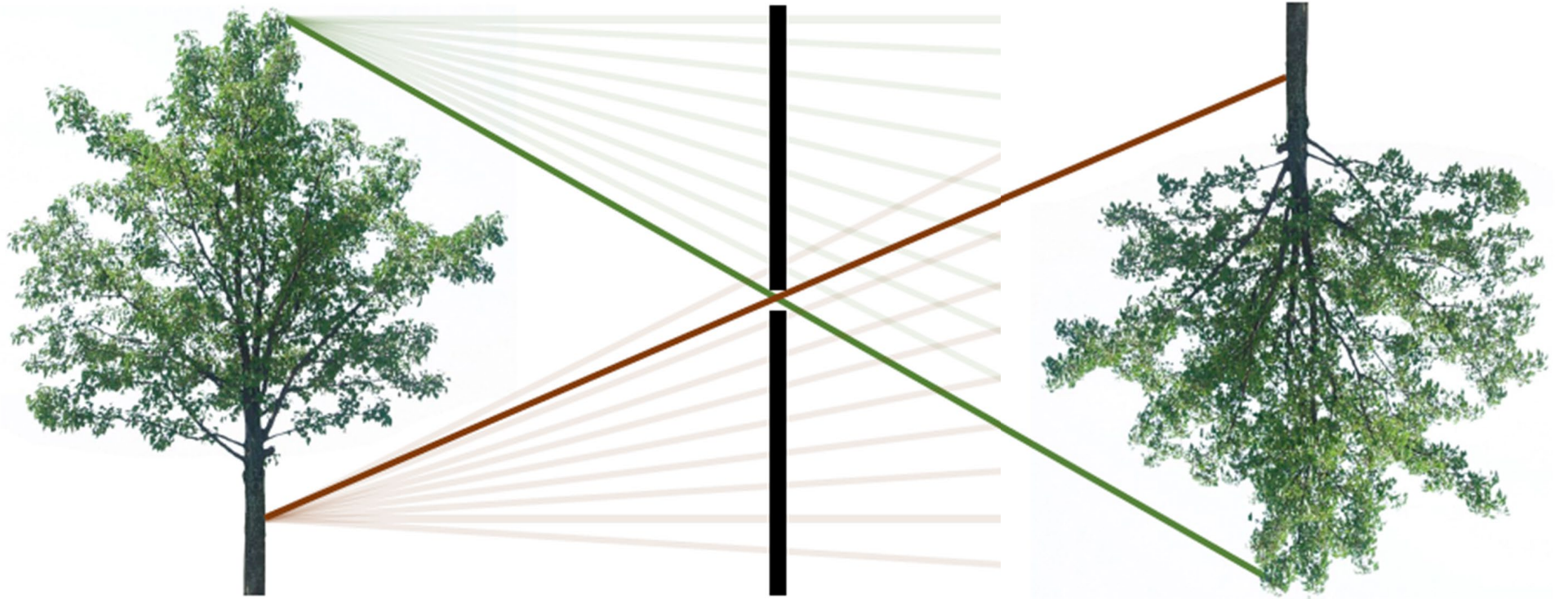
Image Formation



Recap

Pinhole imaging

real-world
object



Each scene point contributes to only one sen

copy of real-world object
(inverted and scaled)

Recap Pinhole camera terms

real-world
object



barrier (diaphragm)



pinhole
(aperture)



camera center
(center of projection)



image plane



digital sensor
(CCD or CMOS)

Pinhole size

What happens as we change the pinhole diameter?

real-world
object



pinhole
diameter

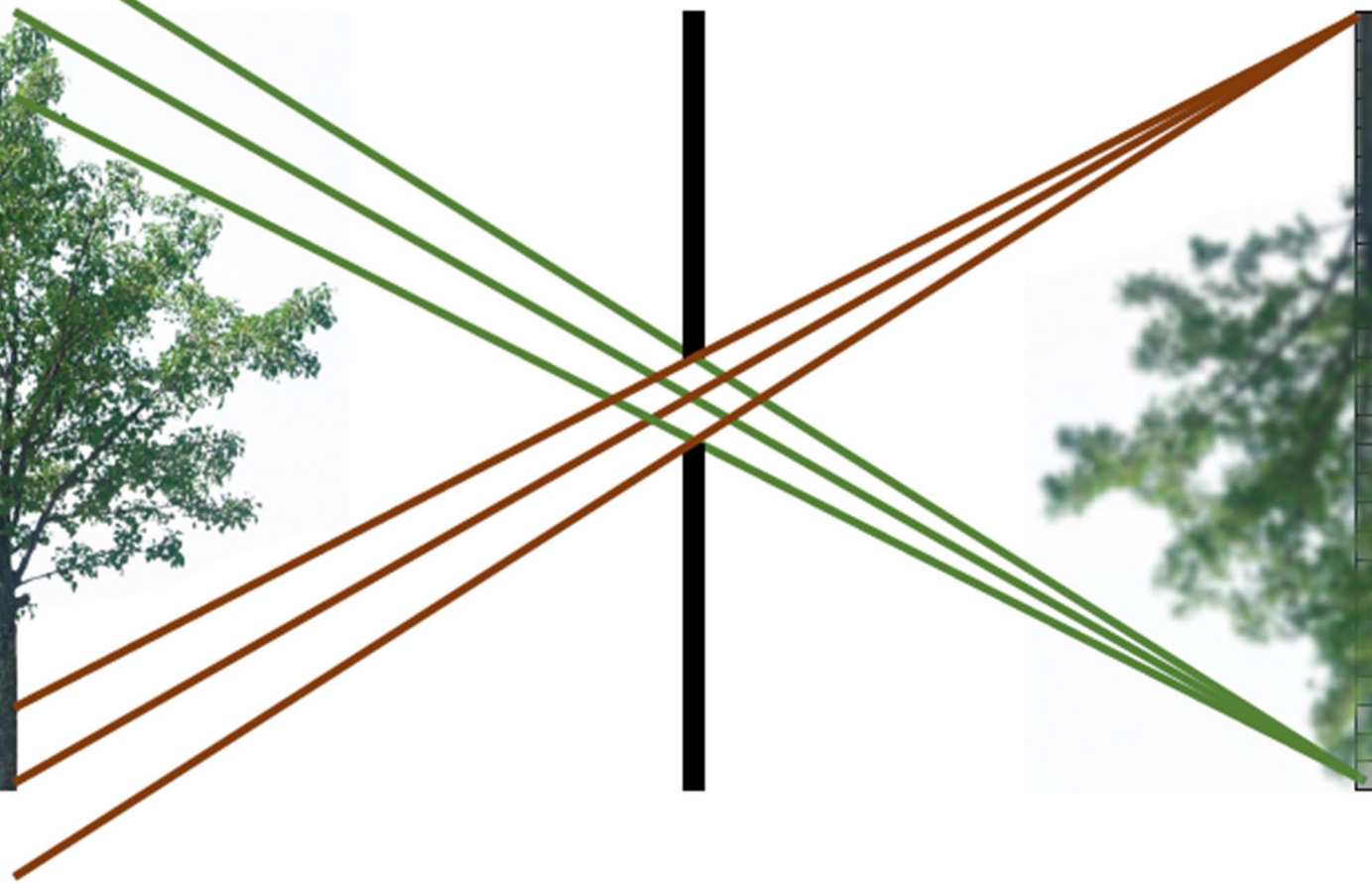
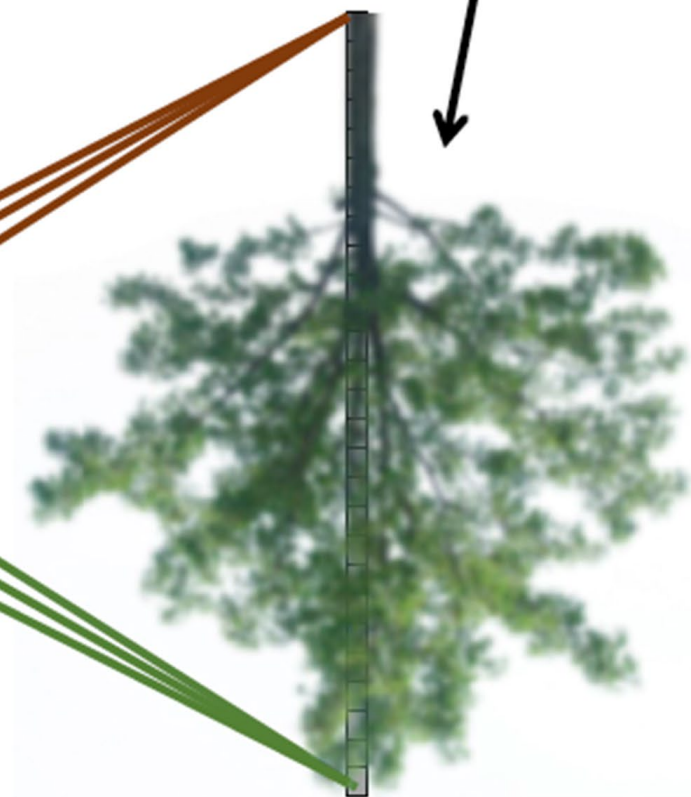
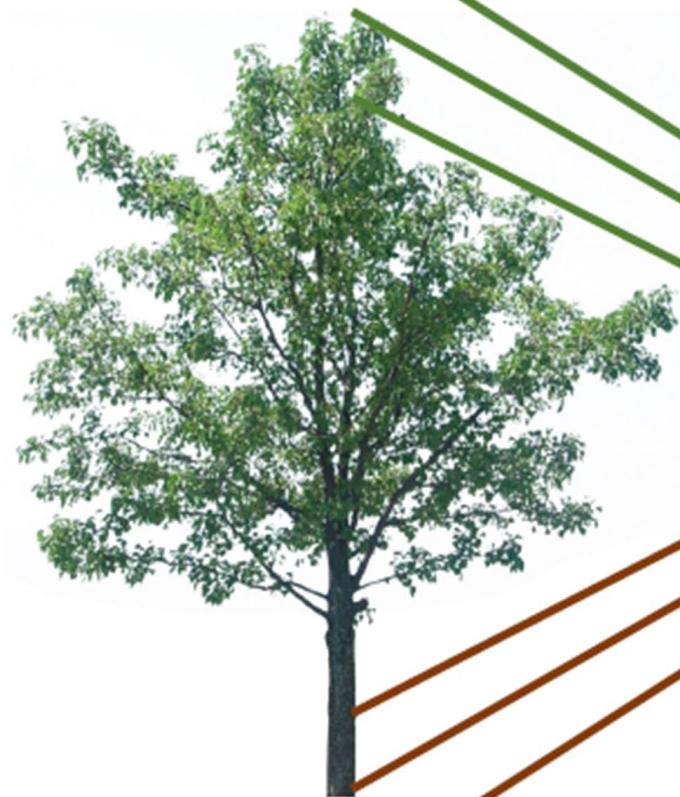


Pinhole size

What happens as we change the pinhole diameter?

object projection becomes blurrier

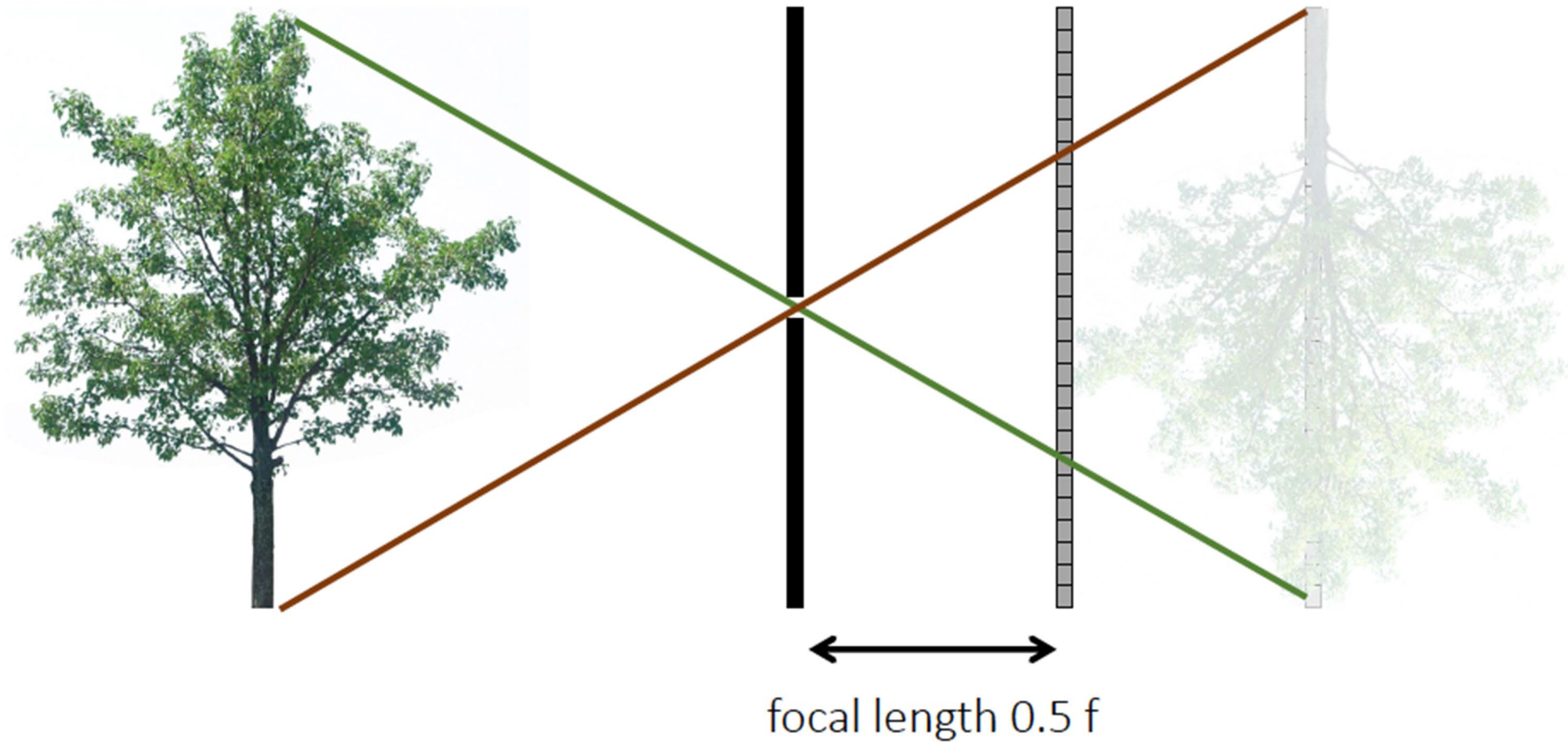
real-world
object



Focal length

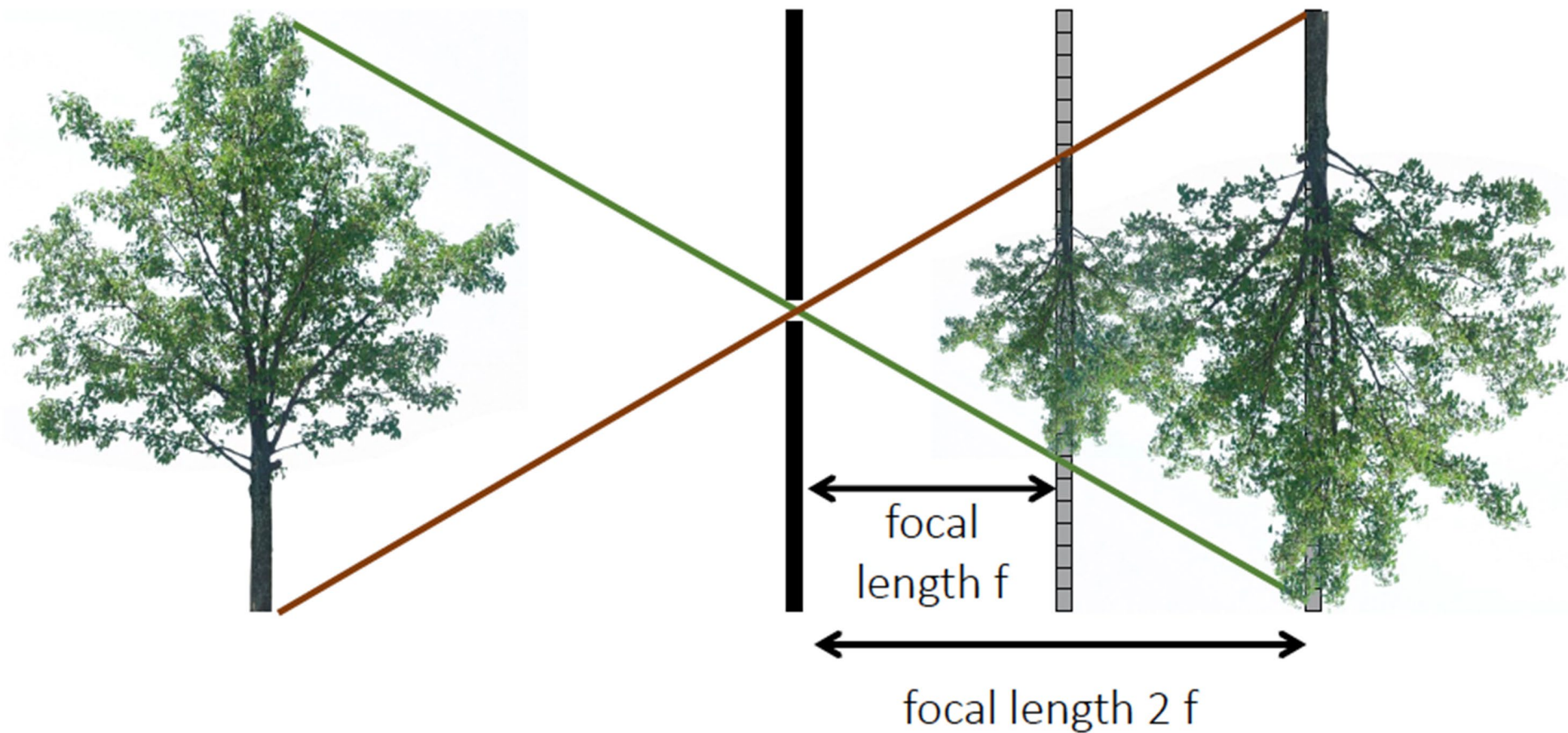
What happens as we change the focal length?

real-world
object

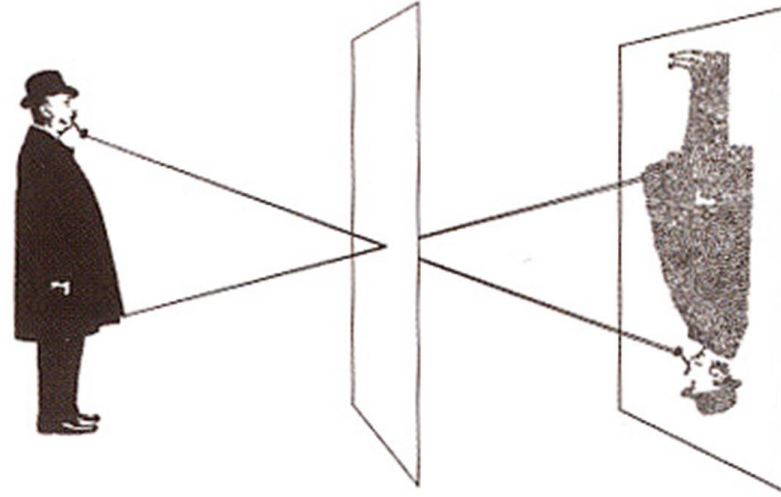


Magnification depends on focal length

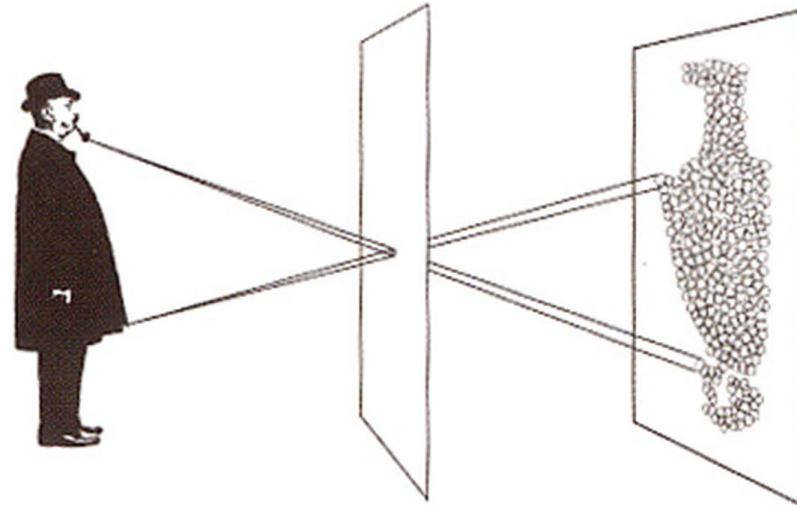
real-world
object



Photograph made with small pinhole



Photograph made with larger pinhole



Problems with Pinholes

Recap

- Pinhole size (aperture) must be “very small” to obtain a clear image.
- However, as pinhole size is made smaller, less light is received by image plane.
- If pinhole is comparable to wavelength λ of incoming light, DIFFRACTION blurs the image!
- Sharpest image is obtained when:

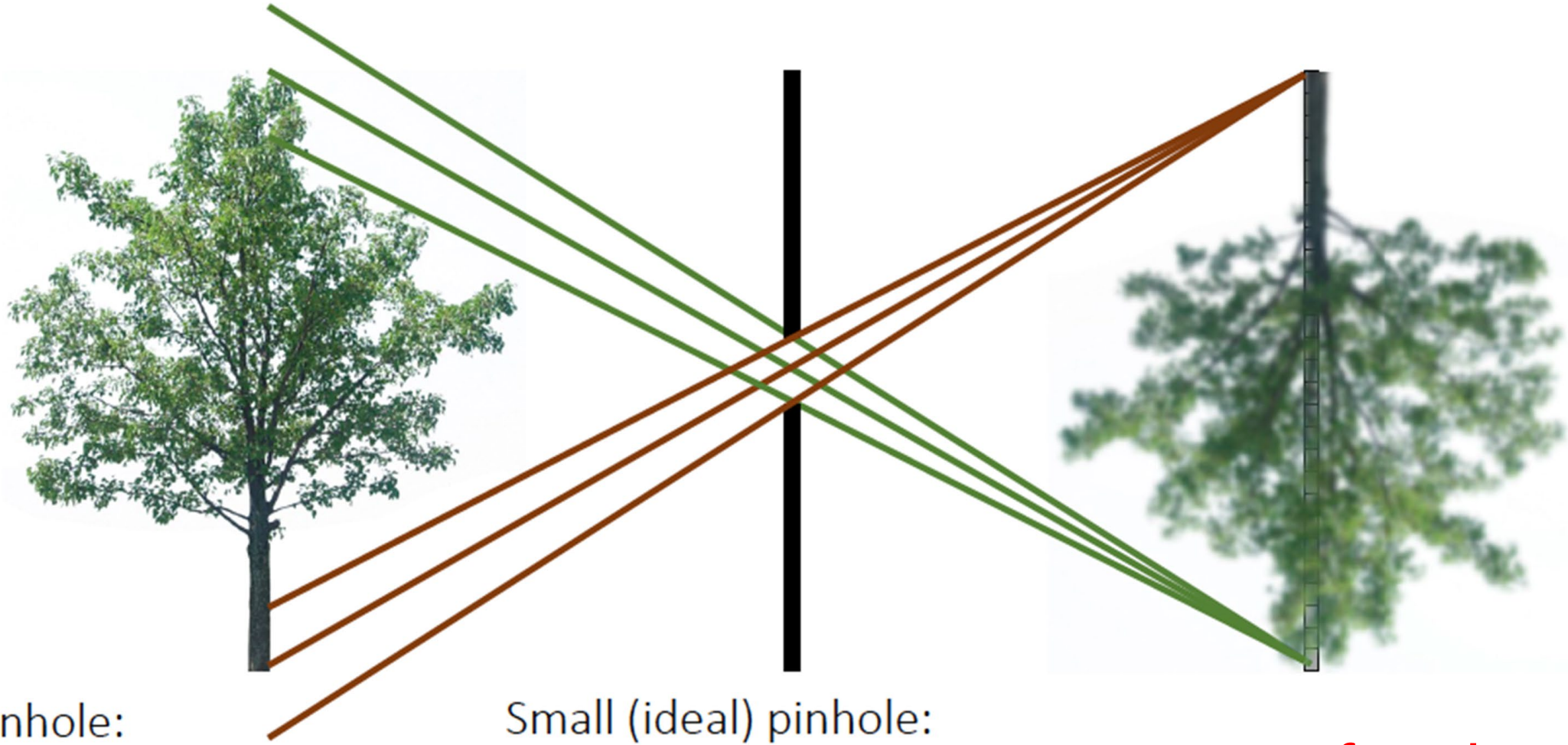
$$\text{pinhole diameter } d = 2 \sqrt{f' \lambda}$$

Example: If $f' = 50\text{mm}$,
= 600nm (red),
 $d = 0.36\text{mm}$



Fig. 5.96 The pinhole camera. Note the variation in image clarity as the hole diameter decreases. [Photos courtesy Dr. N. Joel, UNESCO.]

Pinhole camera



Large pinhole:

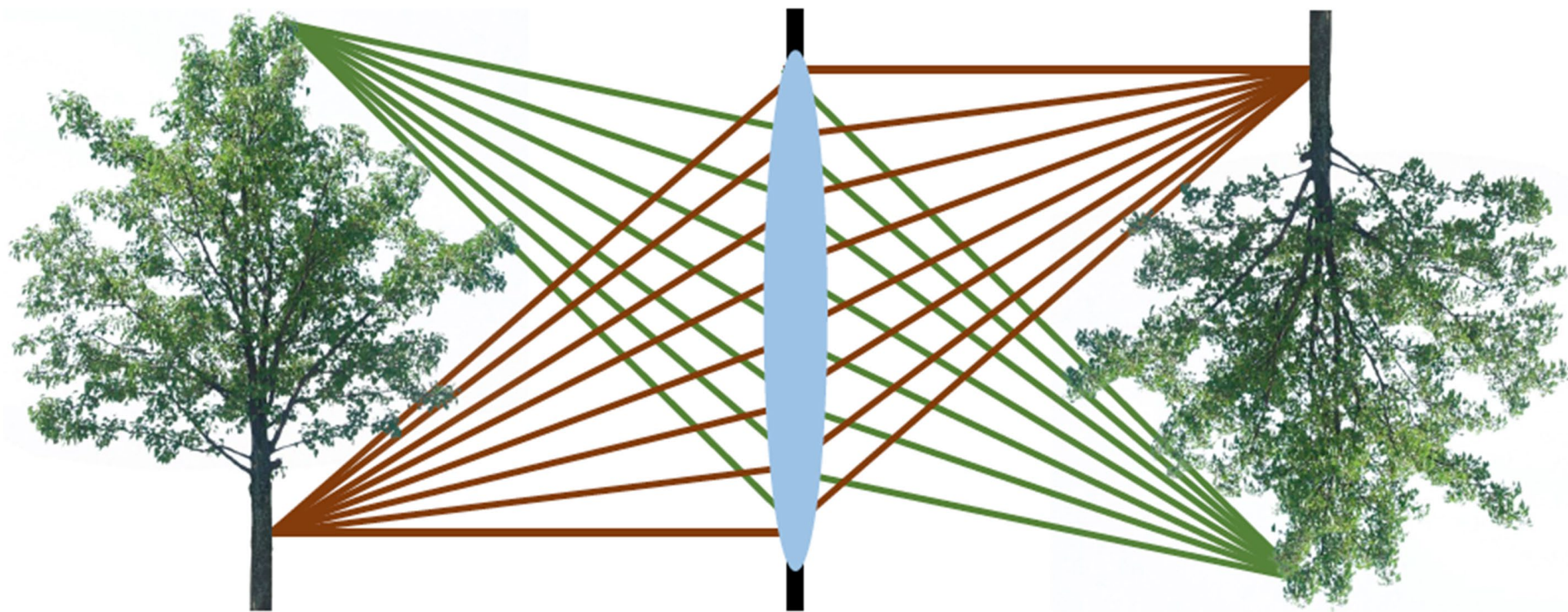
1. Image is blurry.
2. Signal-to-noise ratio is high.

Small (ideal) pinhole:

1. Image is sharp.
2. Signal-to-noise ratio is low.

Best of Both Worlds?

Almost, by using lenses

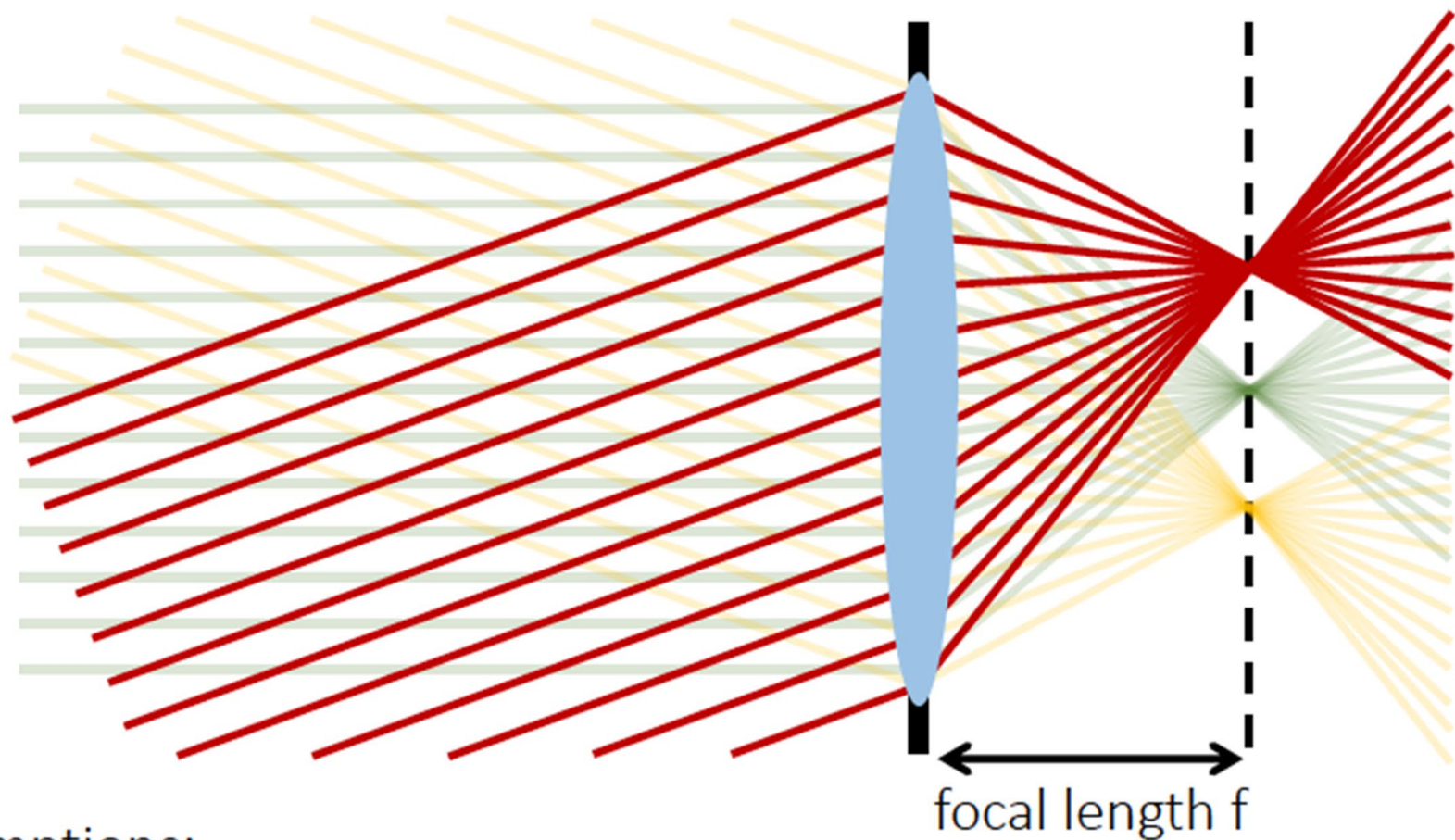


Lenses map “bundles” of rays from points on the scene to the sensor.

How does this mapping work exactly?

Thin lens model

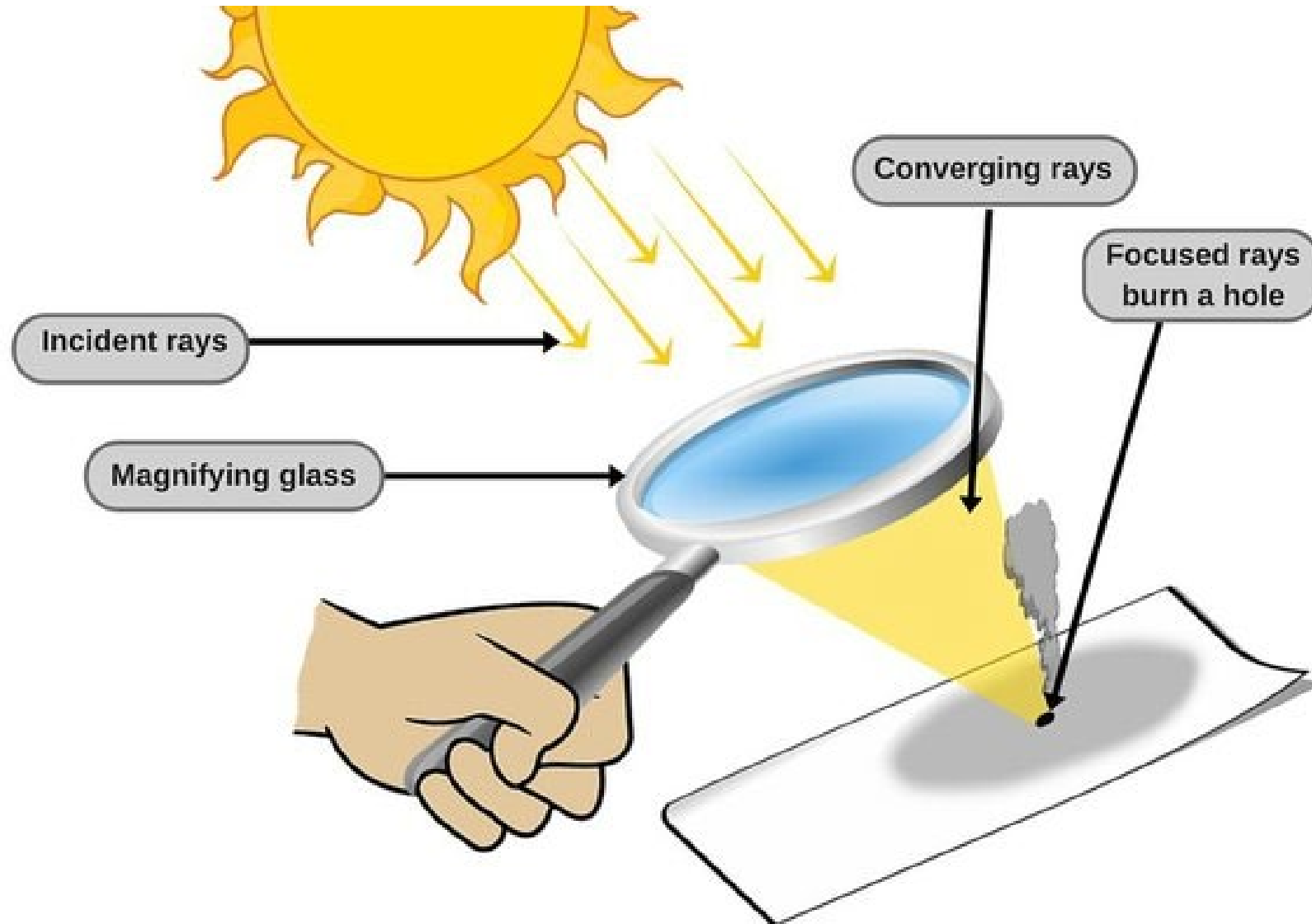
Simplification of geometric optics for well-designed lenses.

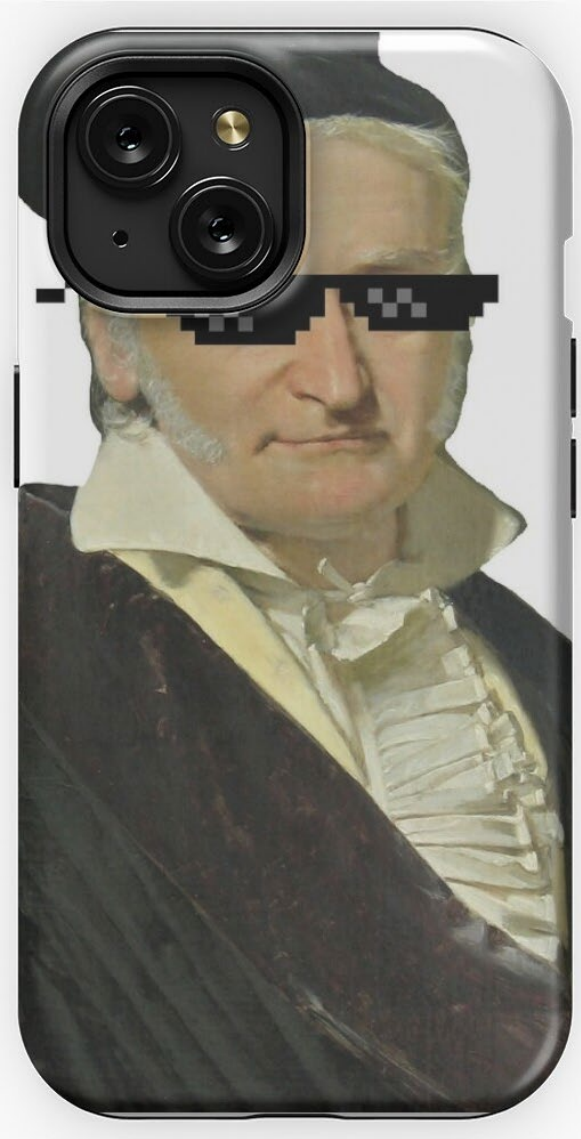


Two assumptions:

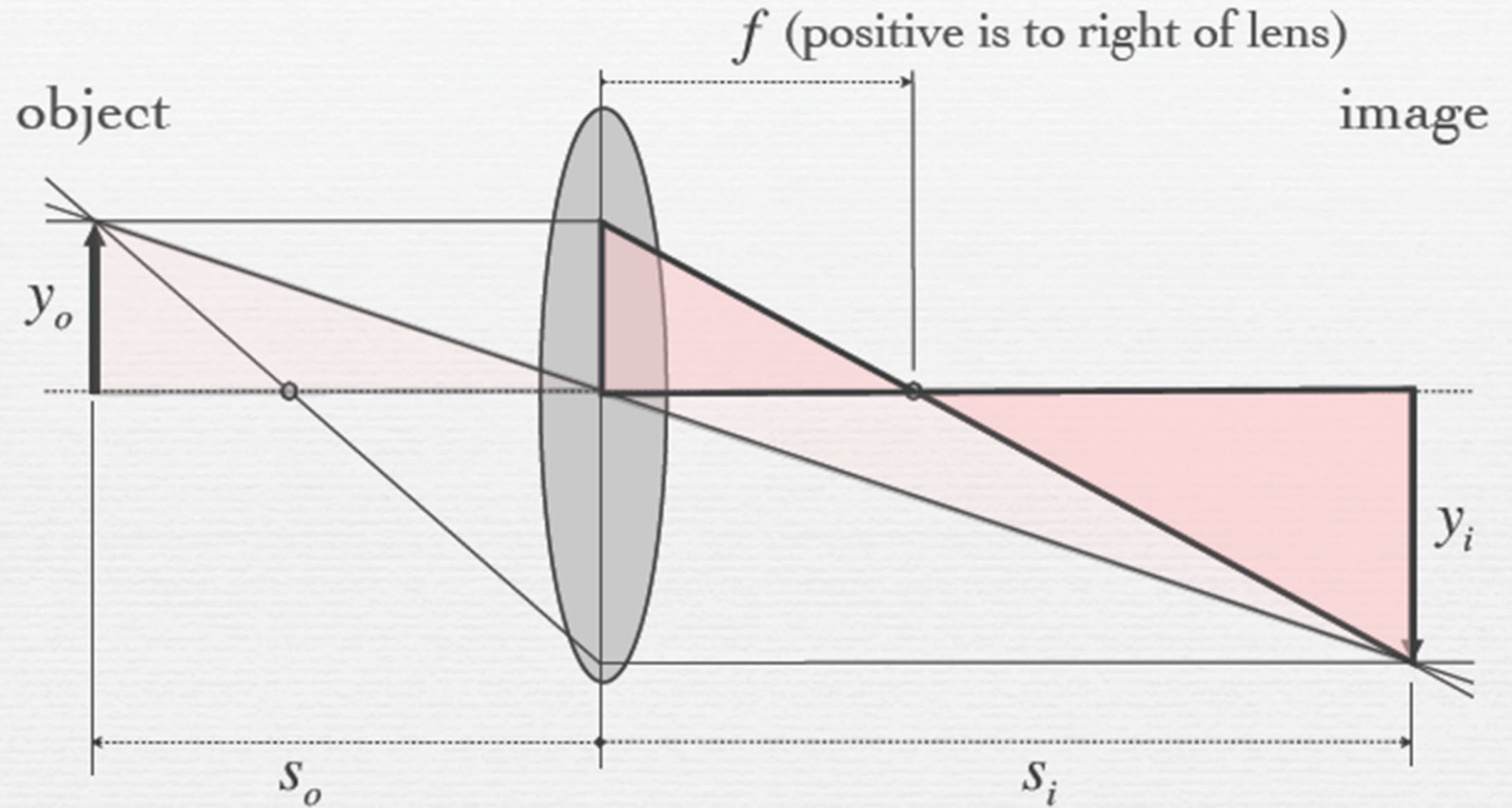
1. Rays passing through lens center are unaffected.
2. Parallel rays converge to a single point located on focal plane.

Can we verify the thin lens model?



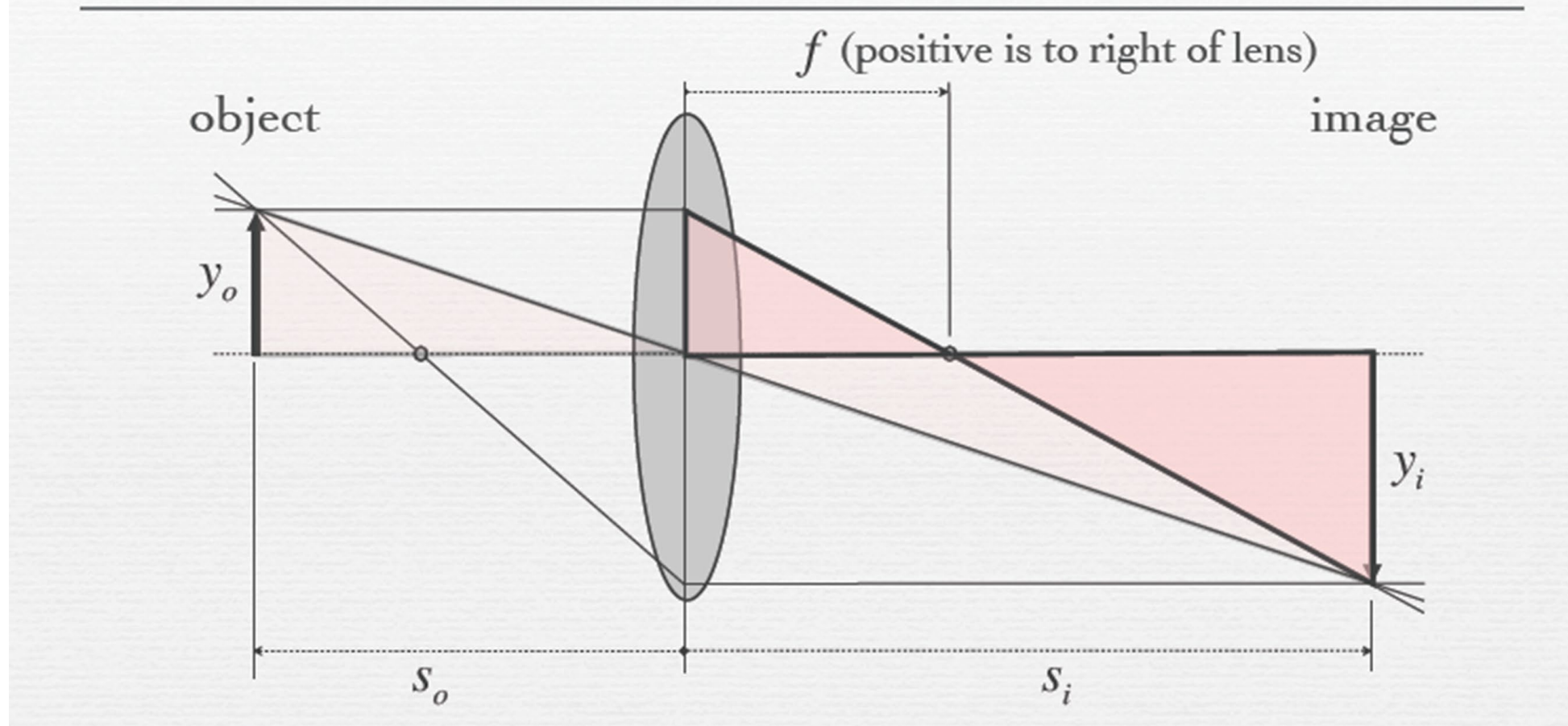


From Gauss's ray construction to the Gaussian lens formula



Exercise: Derive Relationship between s_o , s_i , f

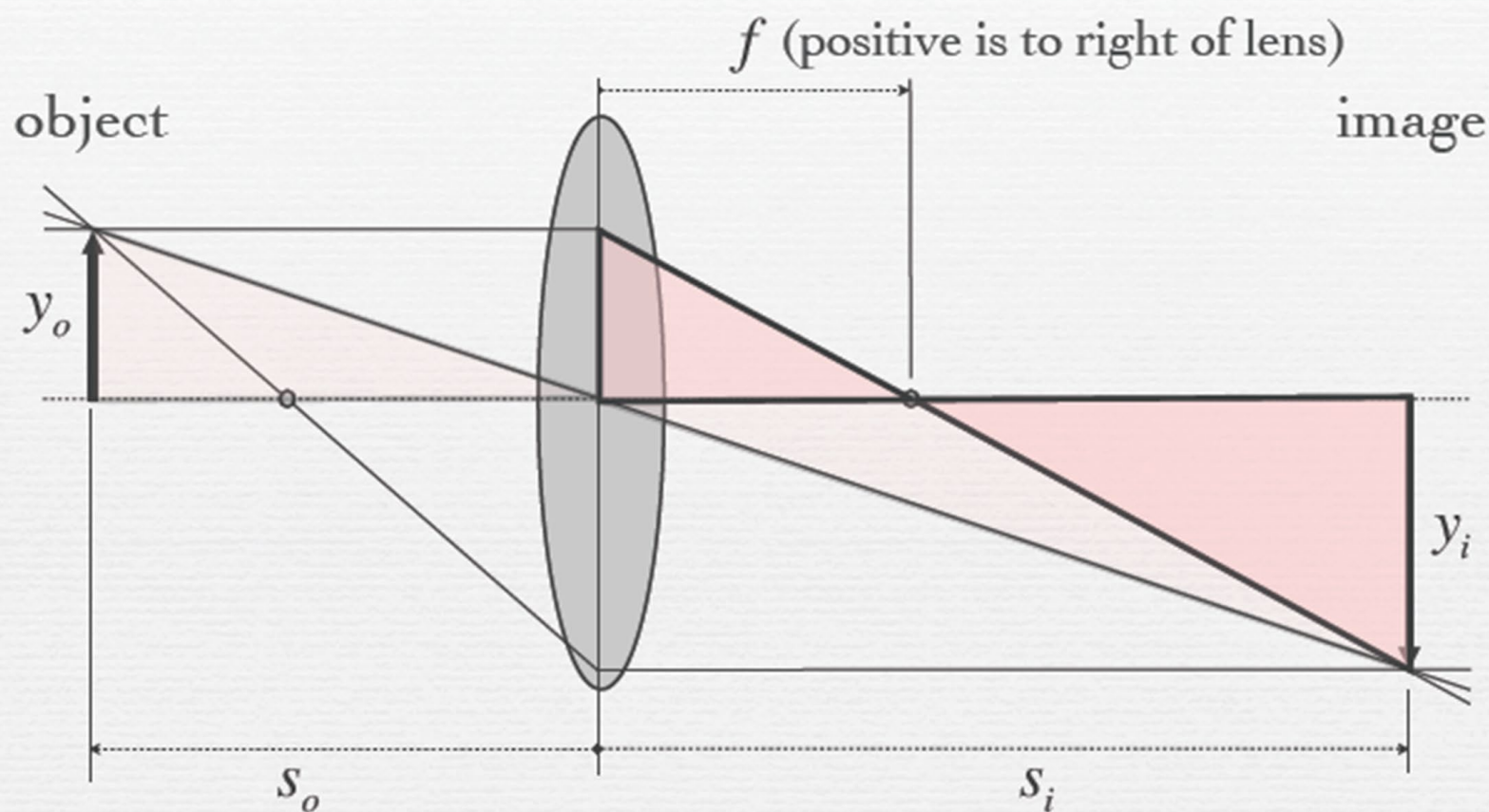
From Gauss's ray construction to the Gaussian lens formula



Exercise: Derive Relationship between s_o , s_i , f

Hint: Similar Triangles

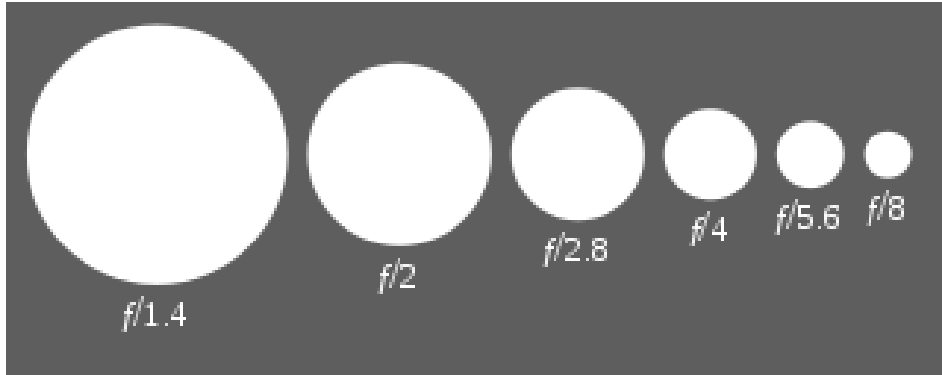
From Gauss's ray construction to the Gaussian lens formula



$$\frac{|y_i|}{y_o} = \frac{s_i}{s_o} \quad \text{and} \quad \frac{|y_i|}{y_o} = \frac{s_i - f}{f} \quad \dots$$

$$\frac{1}{s_o} + \frac{1}{s_i} = \frac{1}{f}$$

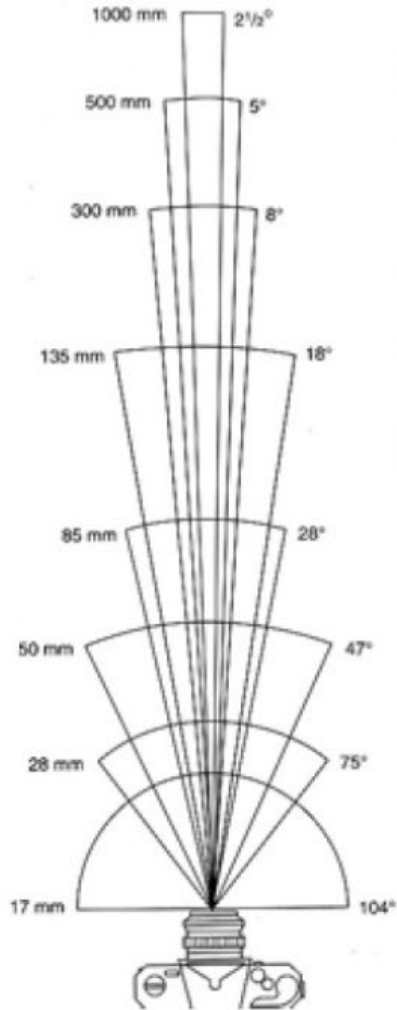
Depth of Field **(effect of varying aperture diameter)**



Smaller aperture: larger DoF



Field of View



135mm



300mm



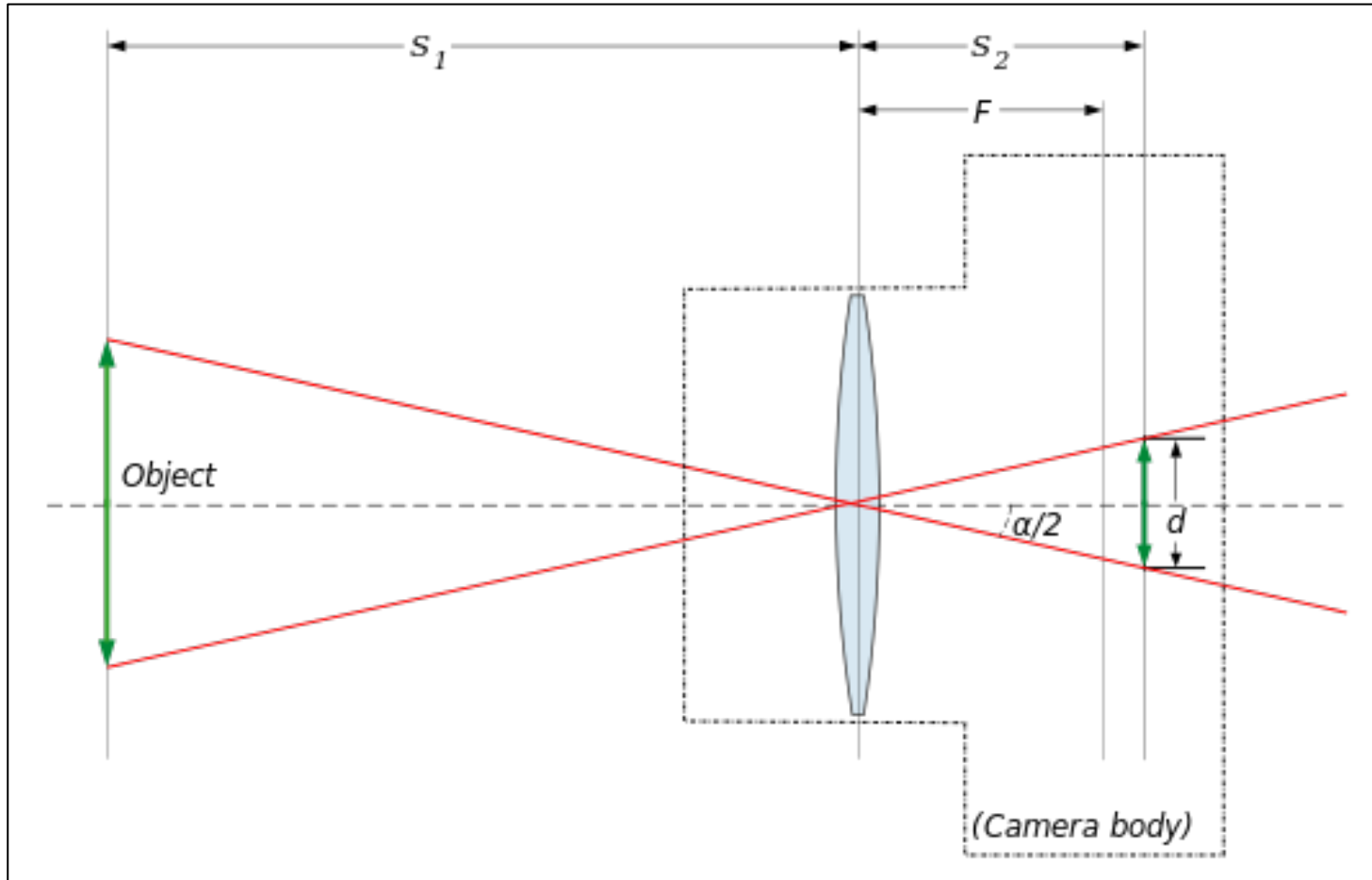
500mm



1000mm

What does FOV depend on?

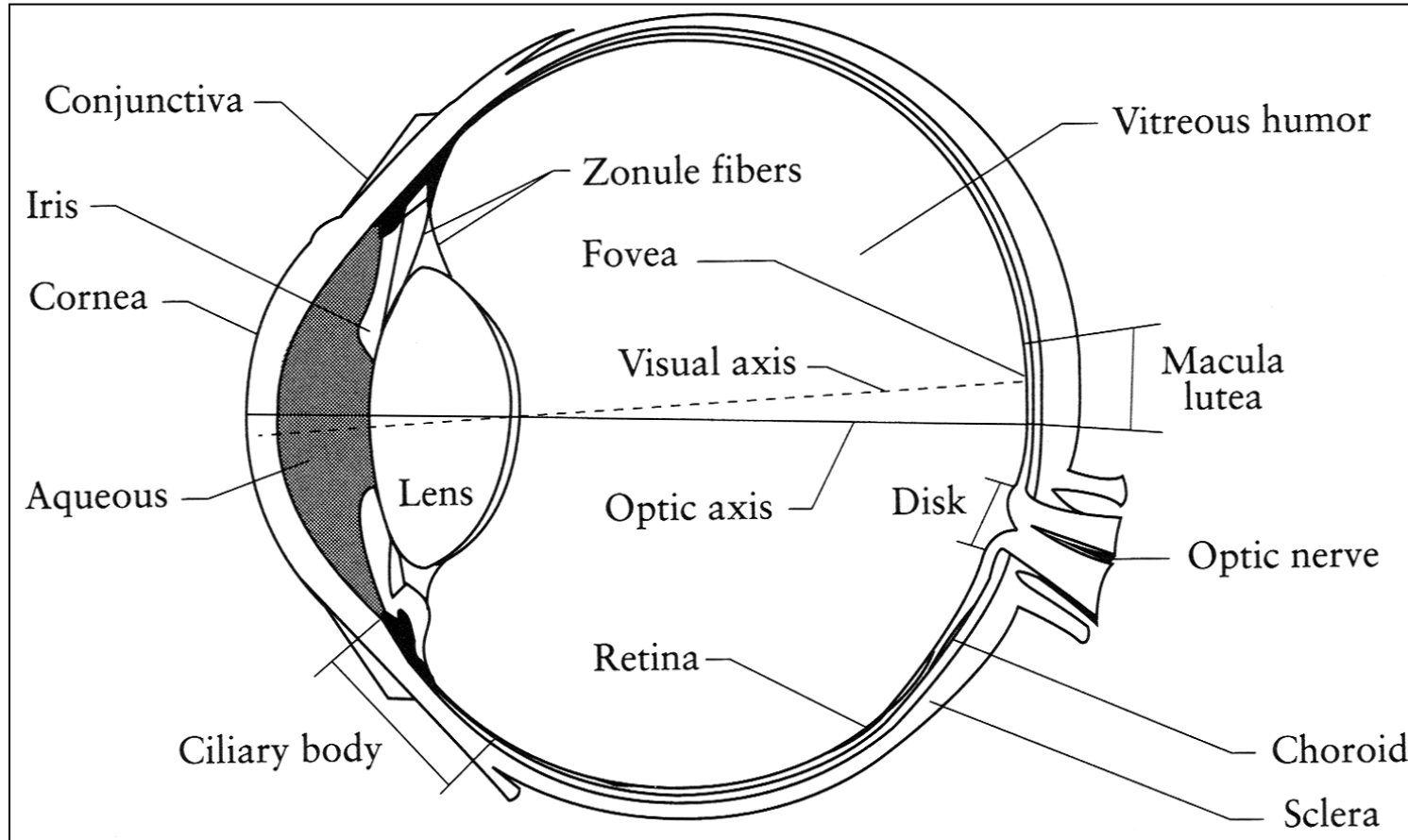
Field of View (effect of varying focal length)



Smaller $f \rightarrow$ larger DoF

$$\alpha = 2 \arctan \frac{d}{2f}$$

The Eye is a Camera



- **Iris**

- colored annulus with radial muscles

- **Pupil**

- the hole (aperture)
- size is controlled by the iris

- What's the "film"?





Disposable cameras are fun,
although it does seem wasteful



And you don't ever
get to see your pictures.



- YEAH, IT'S EITHER TAPING
OR CALLING.



ALSO, HOW DO CAMERAS WORK?

Digital Images

Subjective terms to describe color

Hue

Name of the color
(yellow, red, blue, green, . . .)

Value/Lightness/Brightness

How light or dark a color is.

Saturation/Chroma/Color Purity

How "strong" or "pure" a color is.

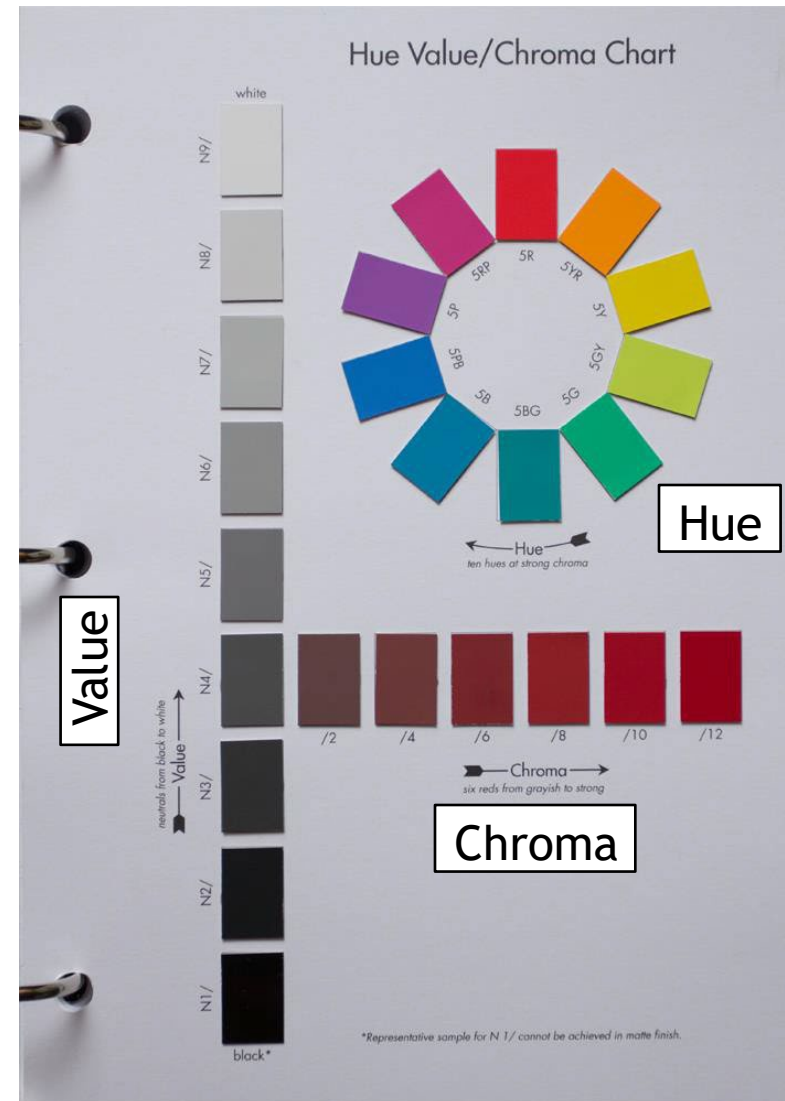
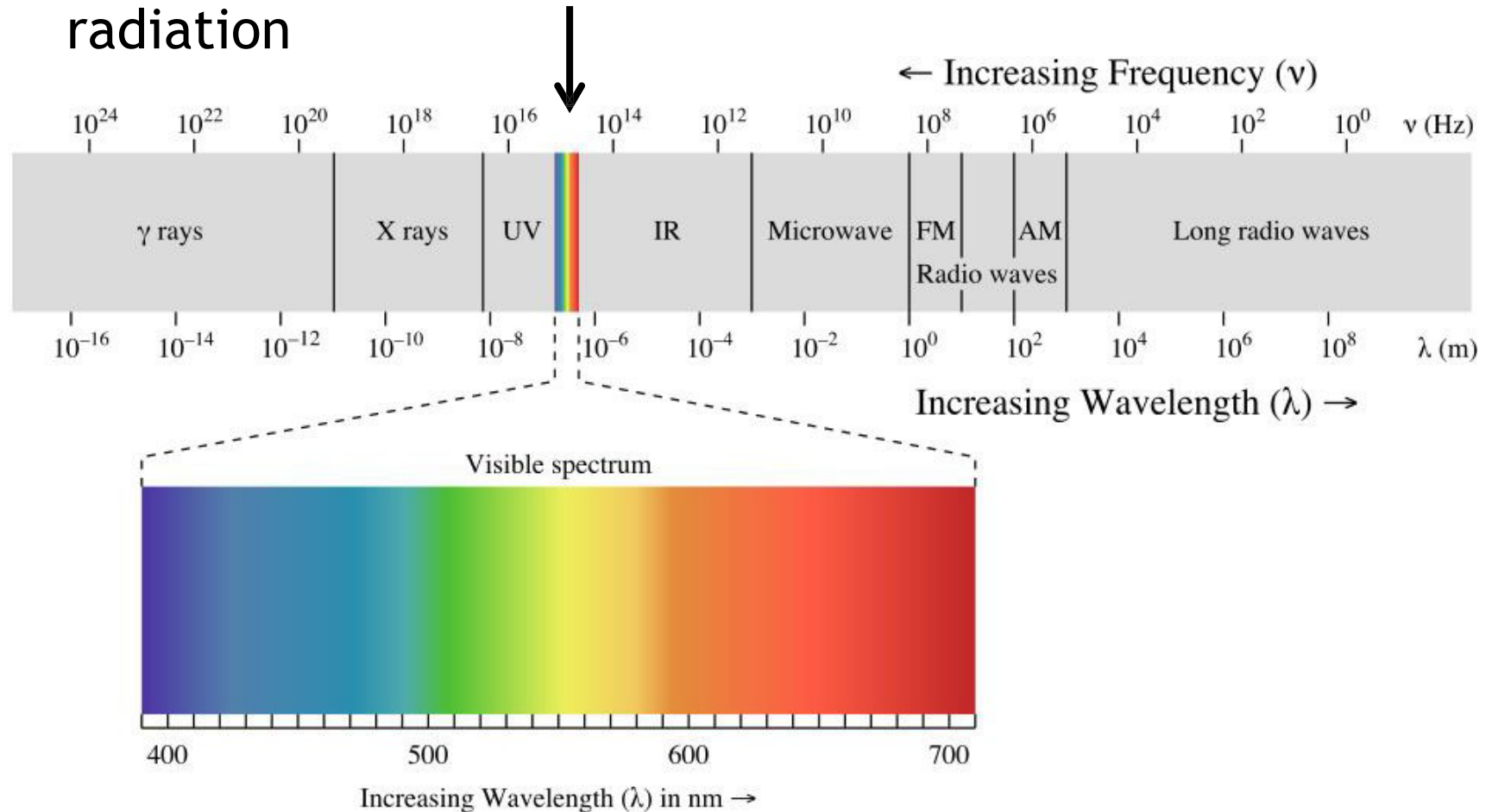


Image from Benjamin Salley
A page from a Munsell Student Color
Set

Where do “color sensations” come from?

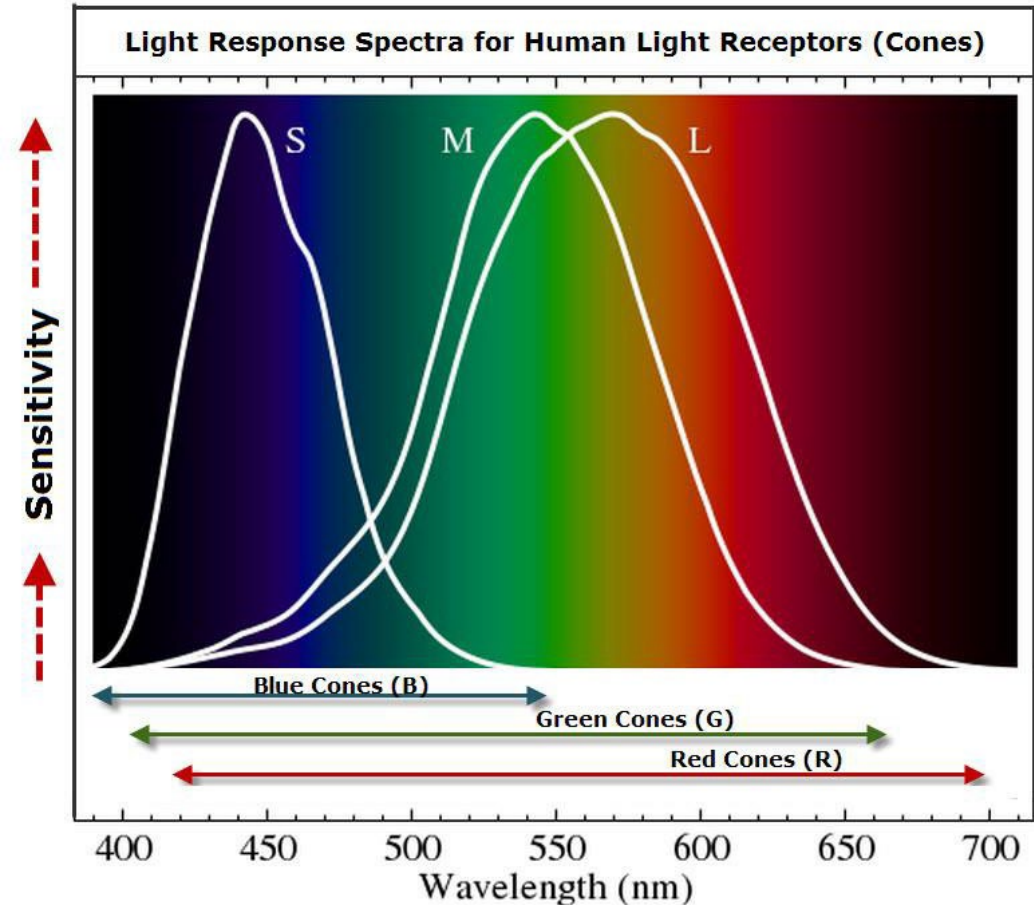
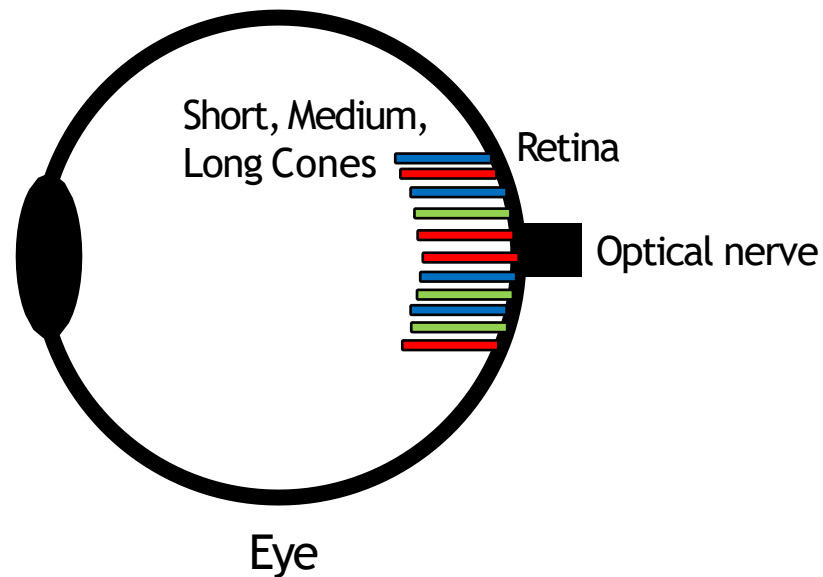
A very small range of electromagnetic radiation



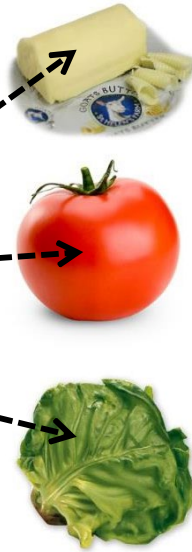
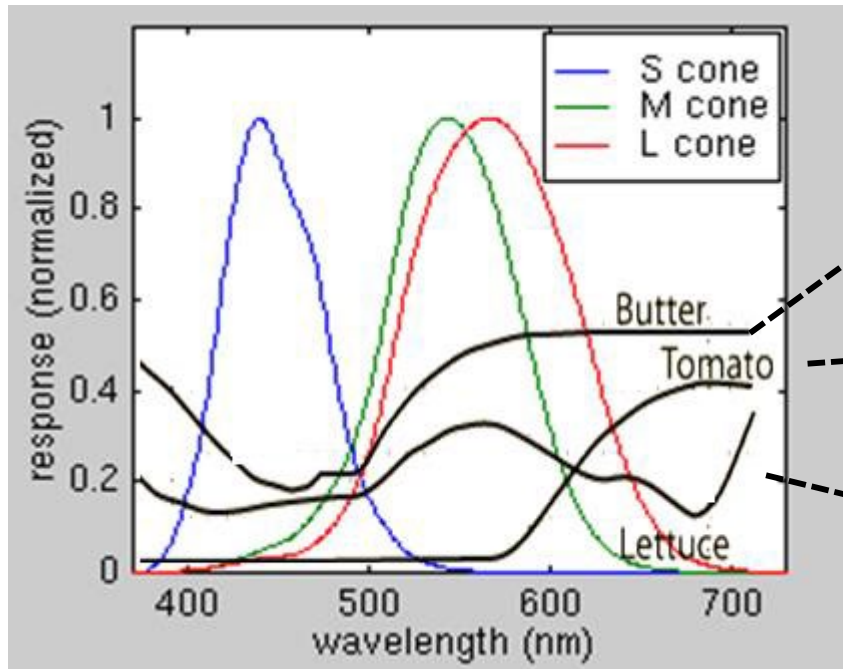
Generally, wavelengths from 380 to 720nm are visible to most individuals

Biology of color sensations

- Our eye has three receptors (cone cells) that respond to visible light and give the sensation of color



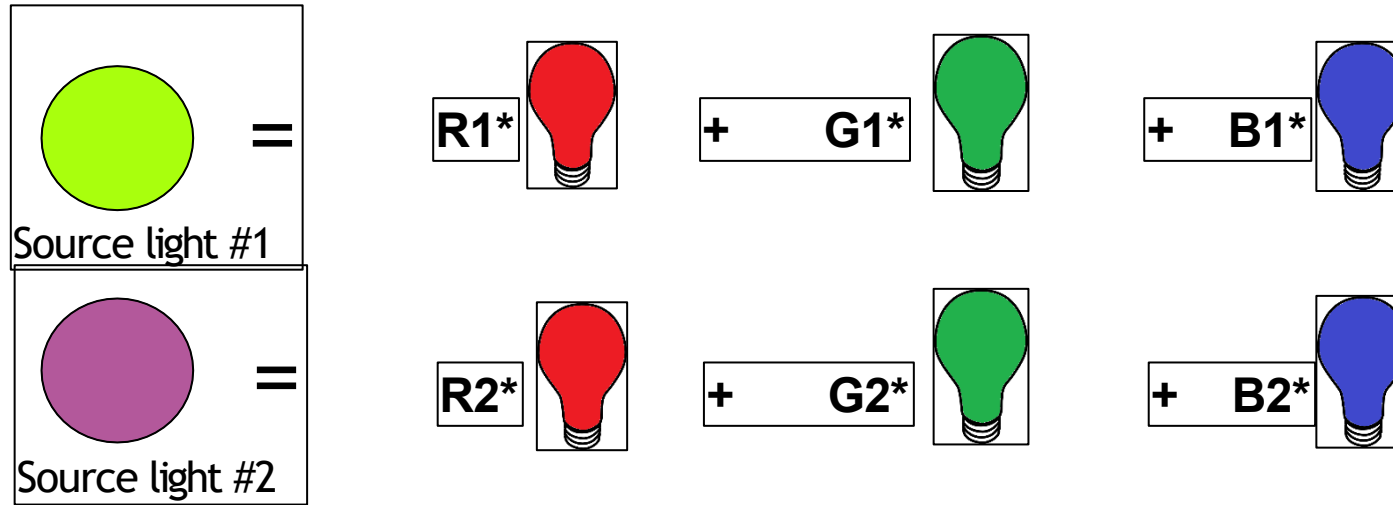
Spectral power distribution (SPD)



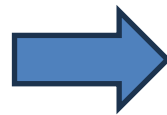
- We rarely see monochromatic light in real world scenes
- Instead, objects reflect a wide range of wavelengths.
- This can be described by a *spectral power distribution* (SPD)
- The SPD plot shows the relative amount of each wavelength reflected over the visible spectrum.

Tristimulus color theory (Grassman's Law)

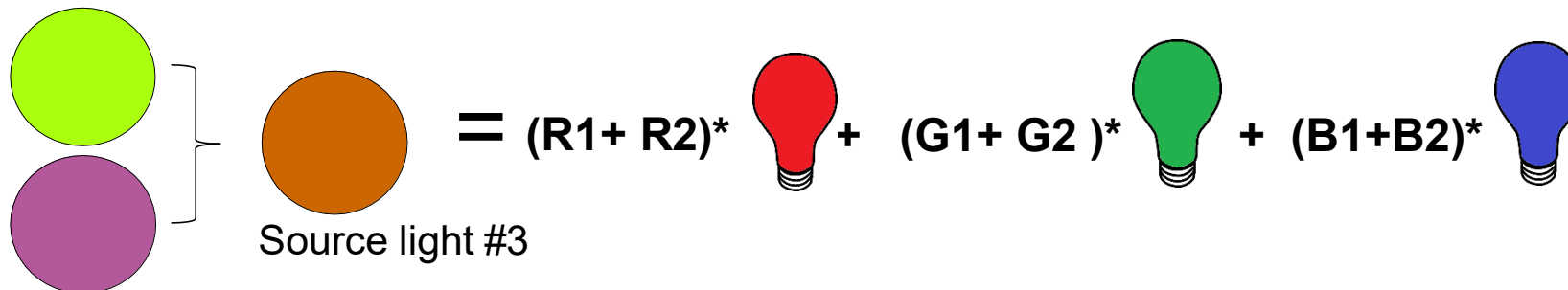
Source color can be matched by a linear combination of three independent "primaries".



If we combined source lights 1 & 2 to get a new source light 3

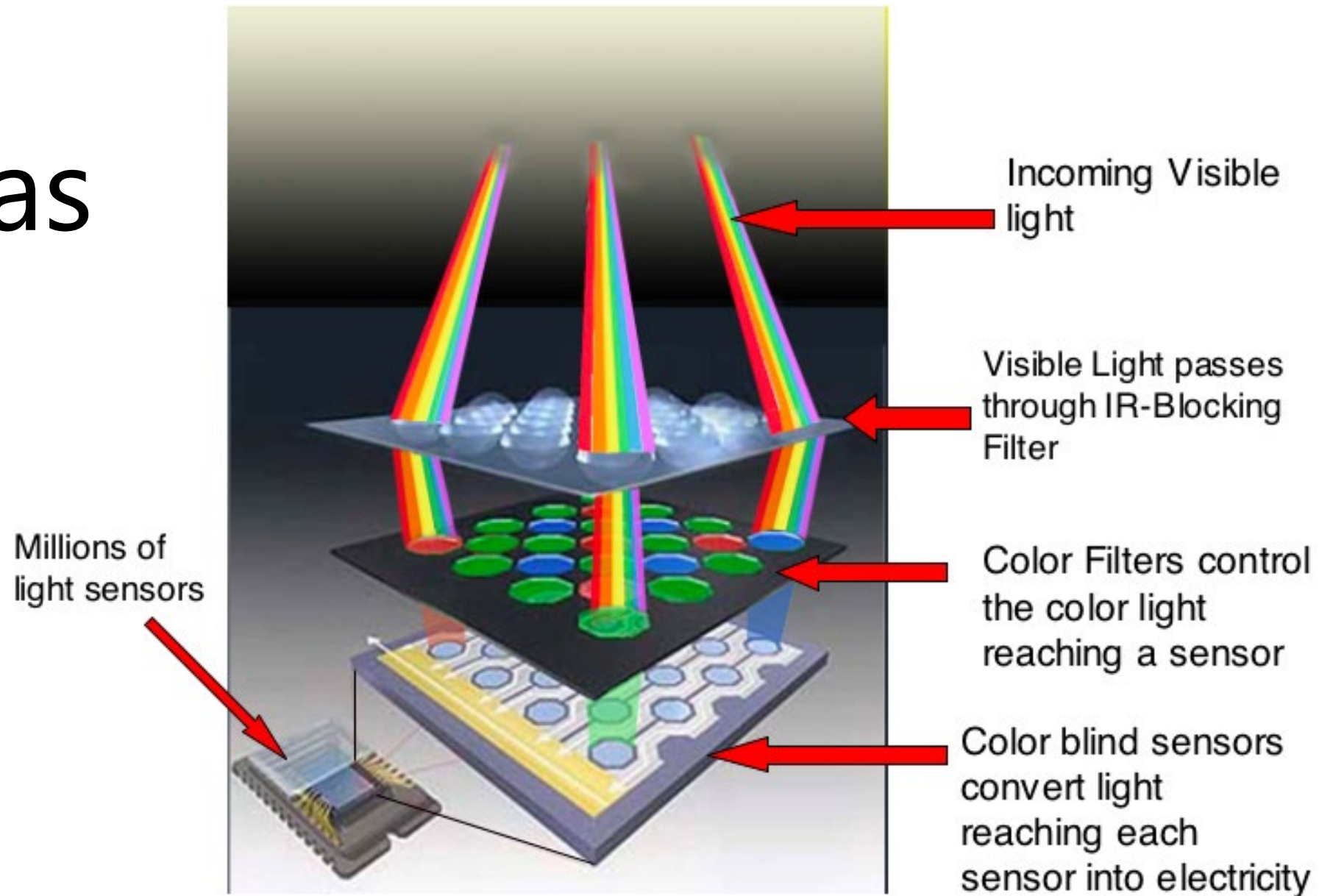


The amount of each primary needed to match the new light #3 is the sum of the weights that matched lights sources #1 & #2.

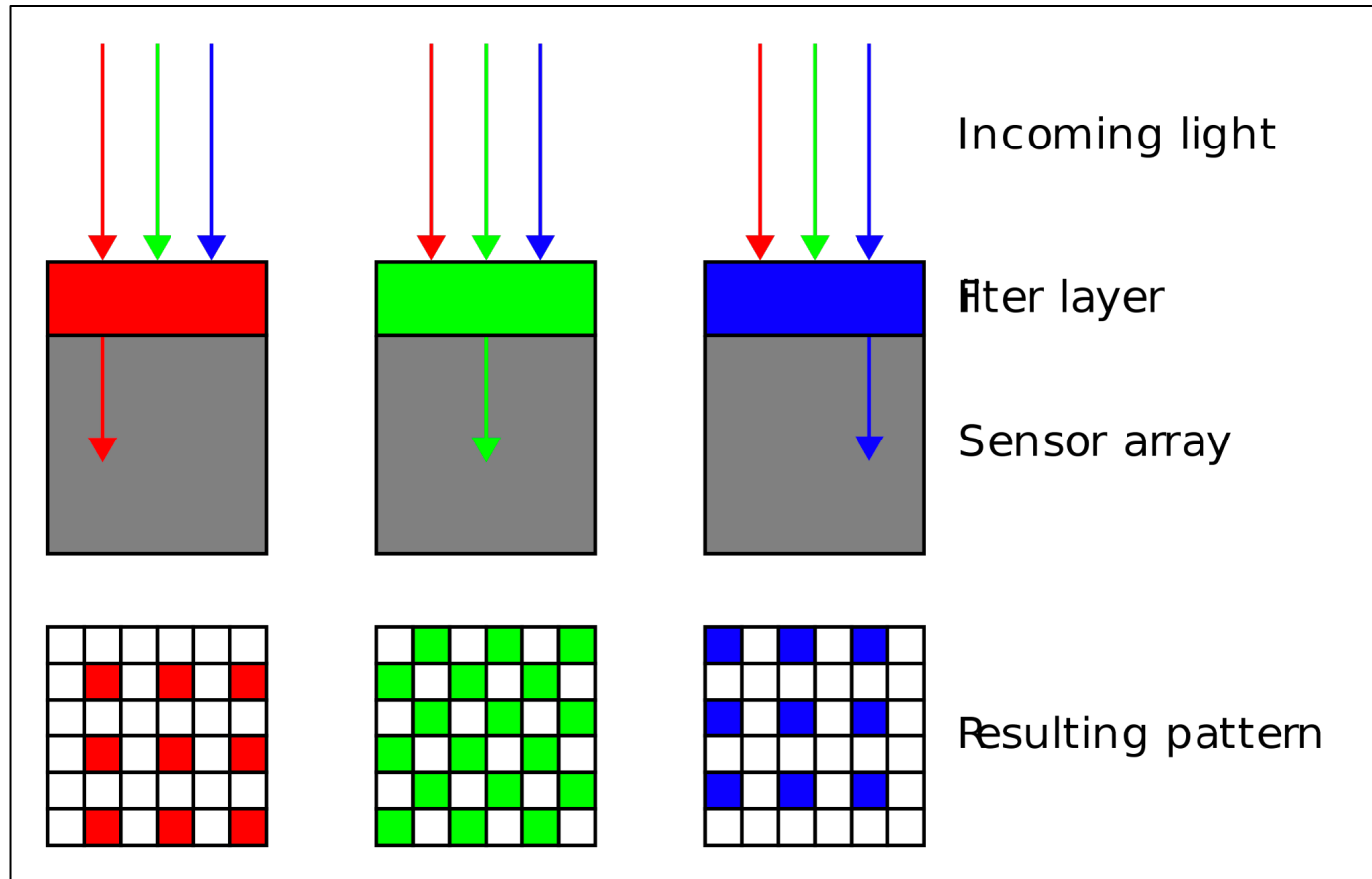


This may seem obvious now, but discovering that light obeys the laws of linear algebra was a huge and useful discovery.

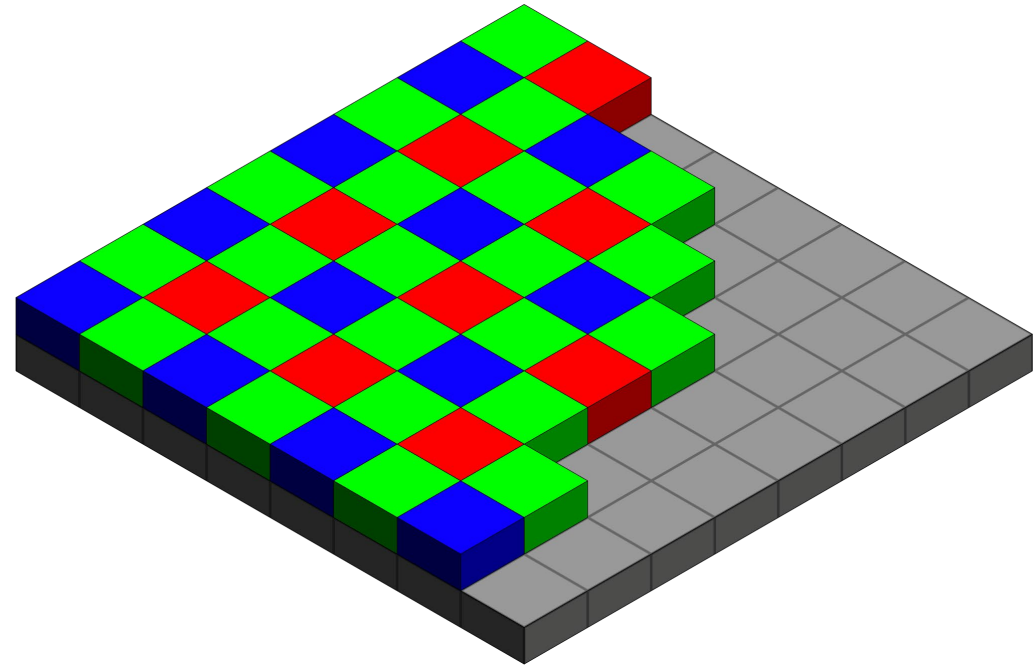
RGB in Cameras



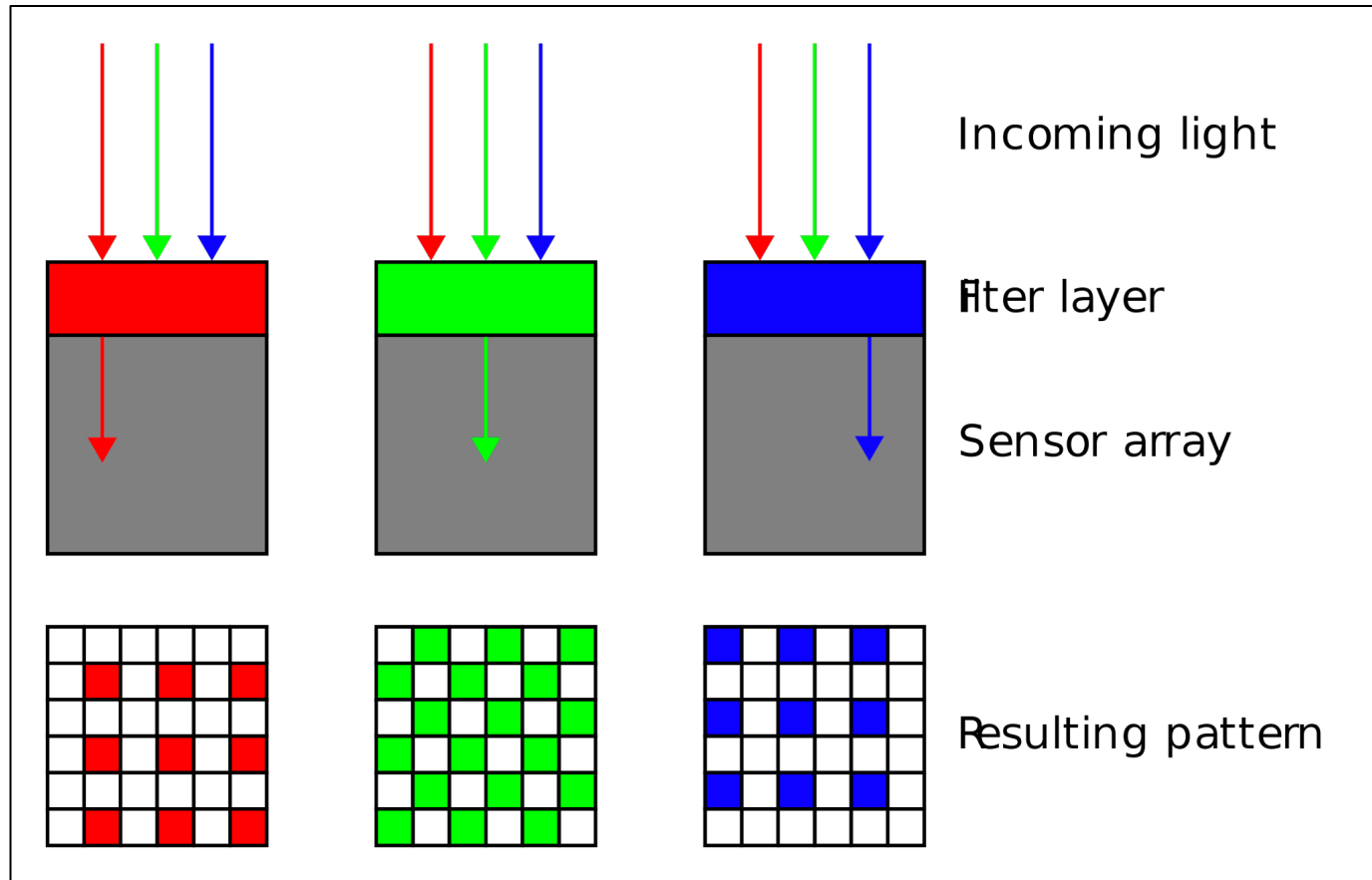
RGB in Cameras - Bayer Pattern



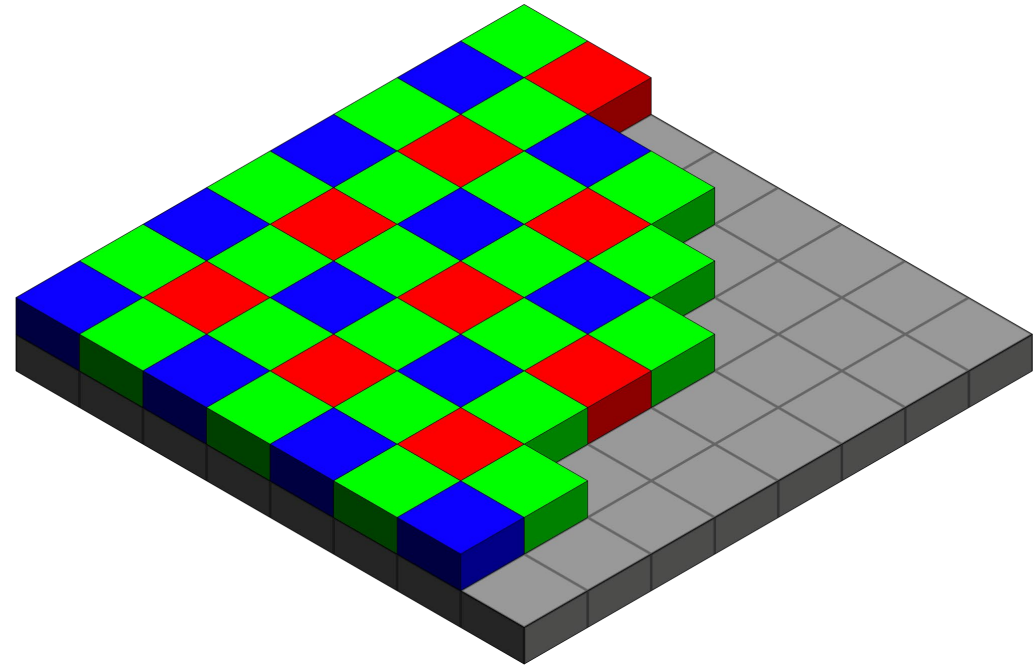
25% pixels see Red
25% pixels see Blue
50% pixels see Green



RGB in Cameras - Bayer Pattern



Then how do we get ***all colors*** at ***all pixels***?



RGB in Cameras - Debayering / Demosaicing

How? → Interpolation !

Method 1: nearest-neighbor interpolation

- For each pixel, for the missing channel, assign the value of the closest pixel with that channel available

Method 2: Bi-Linear Interpolation

- Red-value of a non-red pixel = avg of 2 or 4 adjacent reds
- Similar for green and blue

More Advanced Methods ...

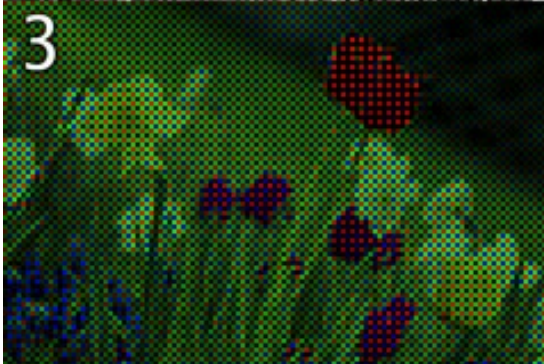
Original
(High
Resolution)



Bayer (120x80)
Intensities



Bayer
Color-Coded

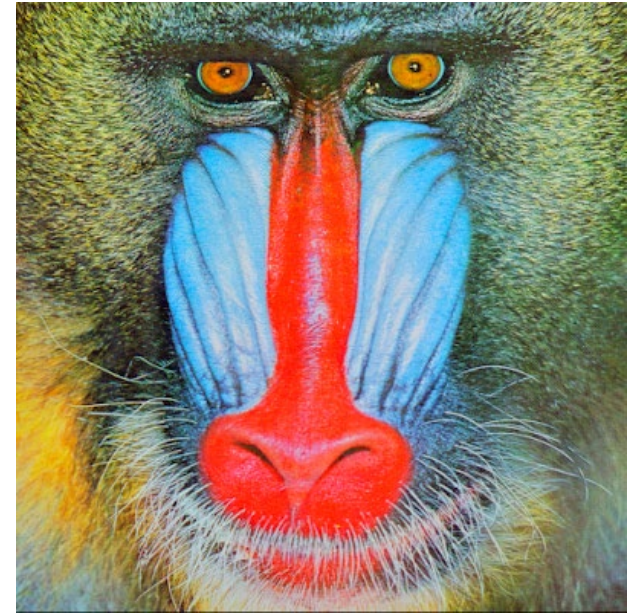


After
Interpolation

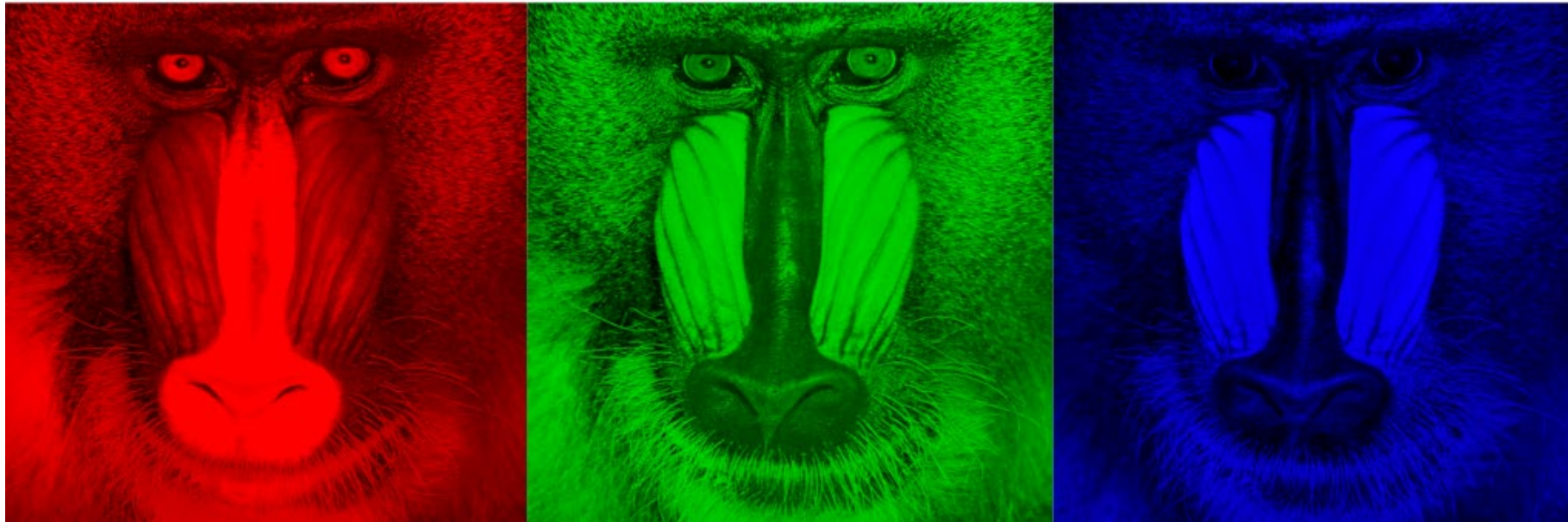


Finally ! Digital **R****G****B** images!

What we see



What the camera stores



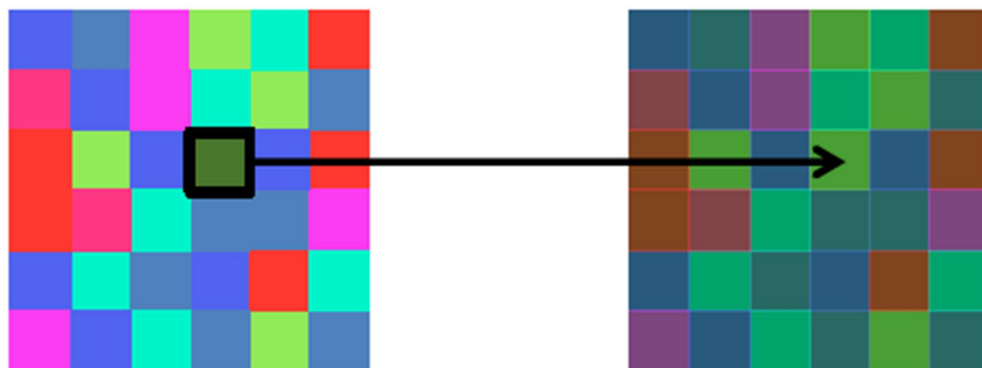
Computer Vision

“understanding” the visual world by processing (RGB) images



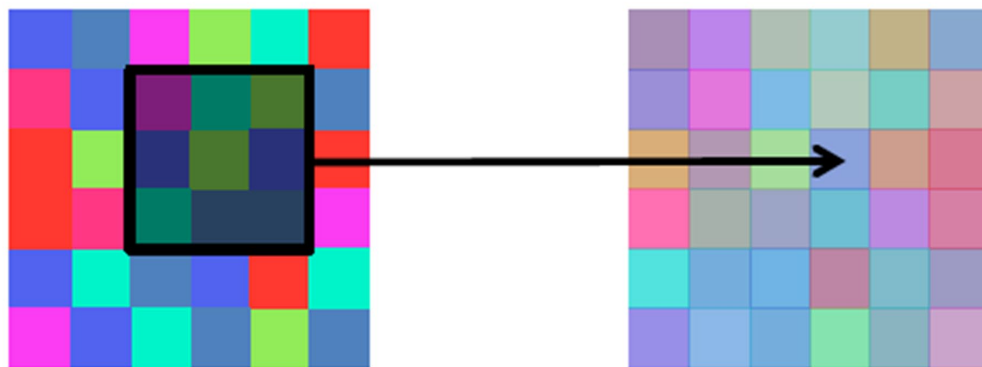
Point Processing vs Image Filtering

Point Operation



point processing

Neighborhood Operation



“filtering”

How would you
implement these?

Examples of point processing

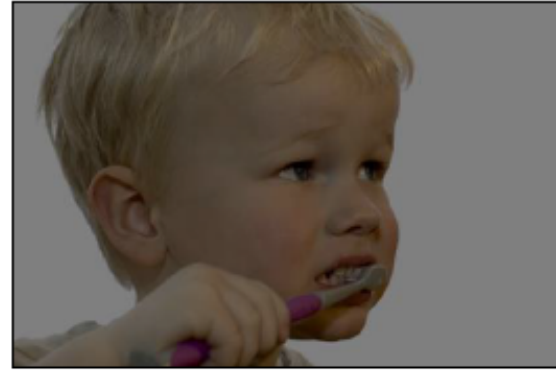
original



darken



lower contrast



non-linear lower contrast



How would you
implement these?

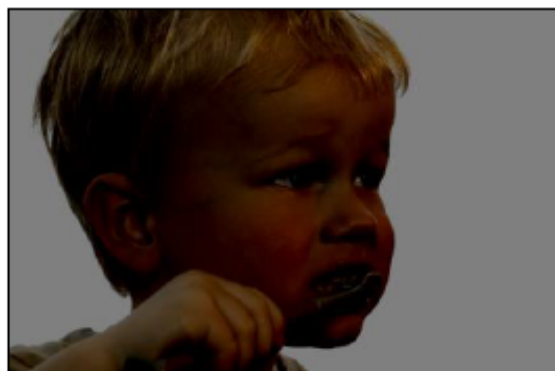
Examples of point processing

original



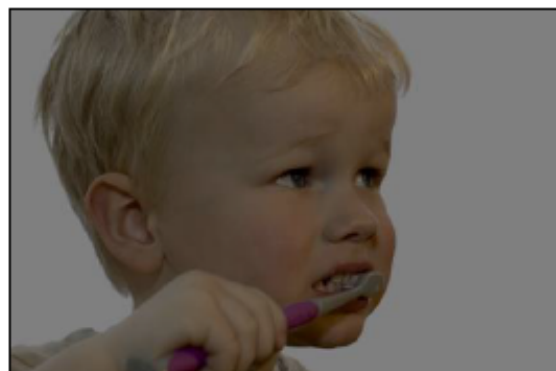
$$x$$

darken



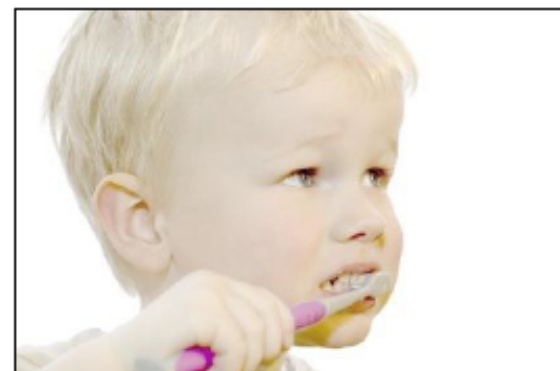
$$x - 128$$

lower contrast



$$\frac{x}{2}$$

non-linear lower contrast



$$\left(\frac{x}{255}\right)^{1/3} \times 255$$

How would you
implement these?

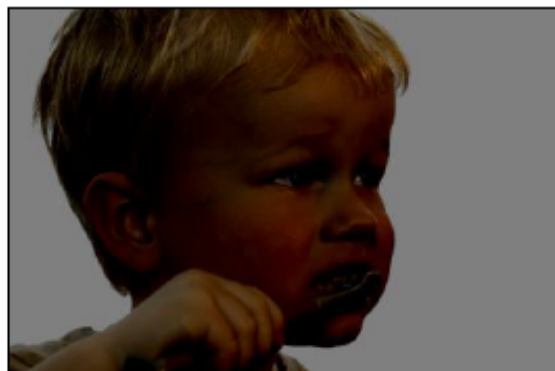
Examples of point processing

original



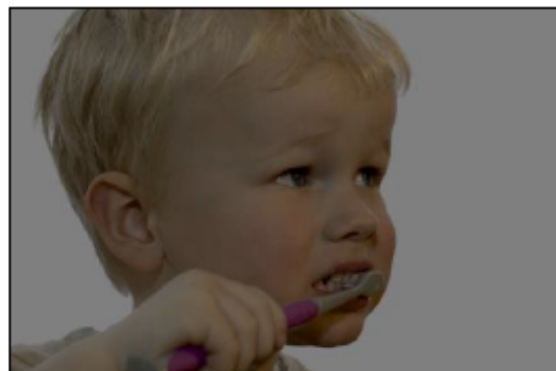
$$x$$

darken



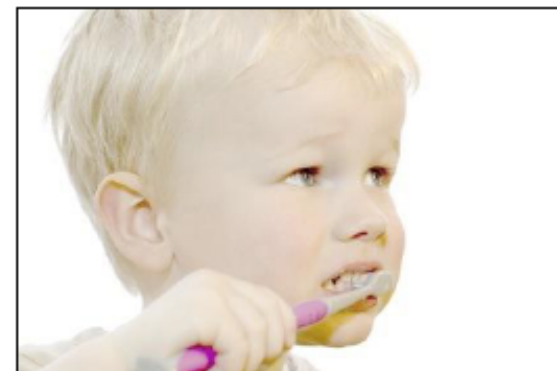
$$x - 128$$

lower contrast



$$\frac{x}{2}$$

non-linear lower contrast

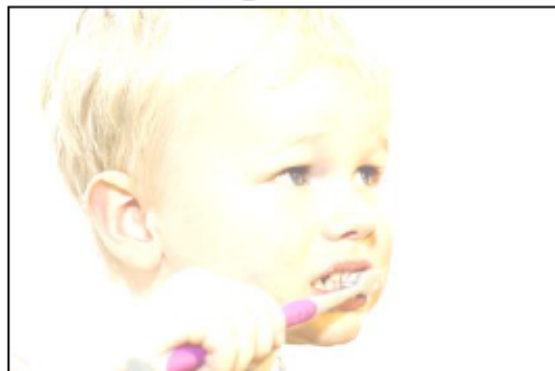


$$\left(\frac{x}{255}\right)^{1/3} \times 255$$

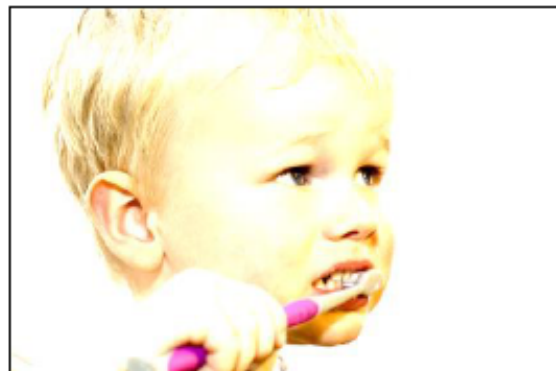
invert



lighten



raise contrast



non-linear raise contrast



How would you
implement these?

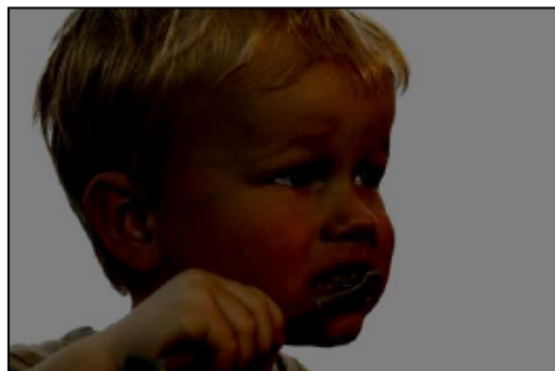
Examples of point processing

original



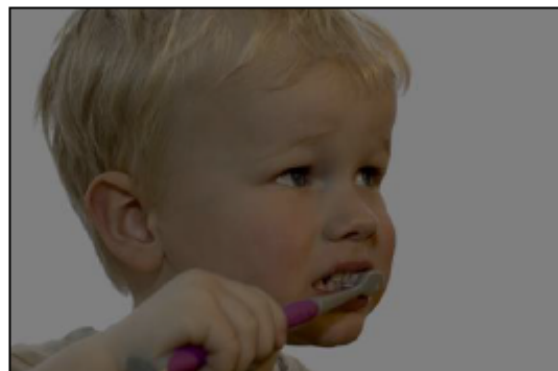
$$x$$

darken



$$x - 128$$

lower contrast



$$\frac{x}{2}$$

non-linear lower contrast



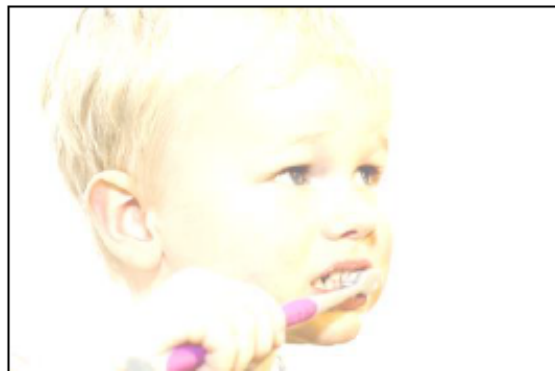
$$\left(\frac{x}{255}\right)^{1/3} \times 255$$

invert



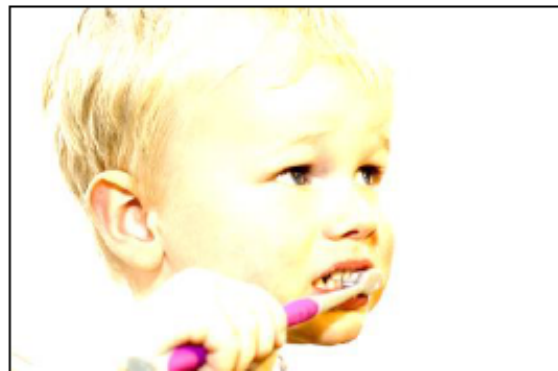
$$255 - x$$

lighten



$$x + 128$$

raise contrast



$$x \times 2$$

non-linear raise contrast



$$\left(\frac{x}{255}\right)^2 \times 255$$



Convolution

Convolution for 1D continuous signals

Definition of filtering as convolution:

$$(f * g)(x) = \int_{-\infty}^{\infty} f(y)g(x - y)dy$$

filtered signal \nearrow \nwarrow notice the flip
filter \nwarrow input signal

$$(f * g)(i) = \sum_{j=1}^m g(j) \cdot f(i - j + m/2)$$

Convolution for 1D *discrete* signals

Definition of filtering as convolution:

$$(f * g)(i) = \sum_{j=1}^m g(j) \cdot f(i - j + m/2)$$

1D Convolution. Example

Suppose our input 1D image is:

$$f = \begin{array}{|c|c|c|c|c|c|c|} \hline 10 & 50 & 60 & 10 & 20 & 40 & 30 \\ \hline \end{array}$$

and our kernel is:

$$g = \begin{array}{|c|c|c|} \hline 1/3 & 1/3 & 1/3 \\ \hline \end{array}$$

Let's call the output image h . What is the value of $h(3)$?

1D Convolution. Example

Suppose our input 1D image is:

$$f = \begin{array}{|c|c|c|c|c|c|c|} \hline 10 & 50 & 60 & 10 & 20 & 40 & 30 \\ \hline \end{array}$$

and our kernel is:

$$g = \begin{array}{|c|c|c|} \hline 1/3 & 1/3 & 1/3 \\ \hline \end{array}$$

“Box” Filter that causes “Blur” or “Smoothing”

Let's call the output image h . What is the value of $h(3)$?

$$h = \begin{array}{|c|c|c|c|c|c|c|} \hline 20 & 40 & 40 & 30 & 20 & 30 & 23.333 \\ \hline \end{array}$$

Convolution for 2D discrete signals

Definition of filtering as convolution:

$$(f * g)(x, y) = \sum_{i, j = -\infty}^{\infty} f(i, j) I(x - i, y - j)$$

filtered image \nearrow $f(i, j)$ filter \nwarrow $I(x - i, y - j)$ input image \nwarrow notice the flip

Convolution for 2D discrete signals

Definition of filtering as convolution:

$$(f * g)(x, y) = \sum_{i, j = -\infty}^{\infty} f(i, j) I(x - i, y - j)$$

filtered image \nearrow \nwarrow notice the flip \nwarrow
filter \nwarrow input image

If the filter $f(i, j)$ is non-zero only within $-1 \leq i, j \leq 1$, then

$$(f * g)(x, y) = \sum_{i, j = -1}^1 f(i, j) I(x - i, y - j)$$

The kernel we saw earlier is the 3x3 matrix representation of $f(i, j)$.

3	5	2	8	1
9	7	5	4	3
2	0	6	1	6
6	3	7	9	2
1	4	9	5	1

Convolutional Filter

1	0	0
1	1	0
0	0	1

0	0	1
0	1	1
1	0	0

flipped

What's the output?

Convolution vs correlation

Definition of discrete 2D convolution:

$$(f * g)(x, y) = \sum_{i, j = -\infty}^{\infty} f(i, j) I(x - i, y - j)$$

notice the flip

Definition of discrete 2D correlation:

$$(f * g)(x, y) = \sum_{i, j = -\infty}^{\infty} f(i, j) I(x + i, y + j)$$

notice the lack of a flip

- Most of the time won't matter, because our kernels will be symmetric.
- Will be important when we discuss frequency-domain filtering

Image Convolution Examples

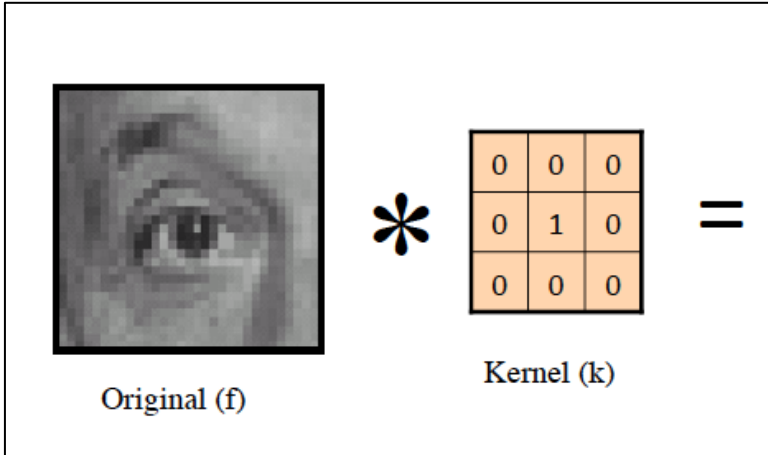


Image Convolution Examples

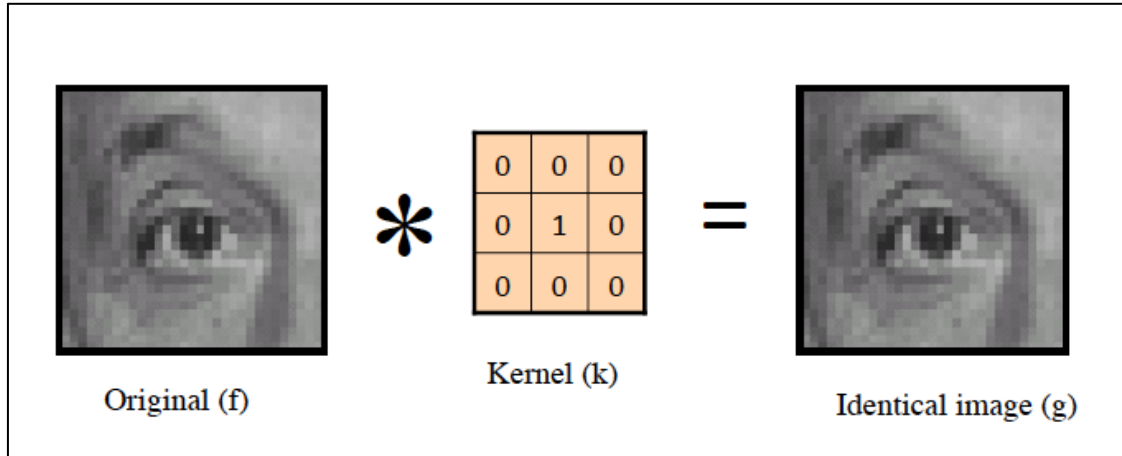


Image Convolution Examples

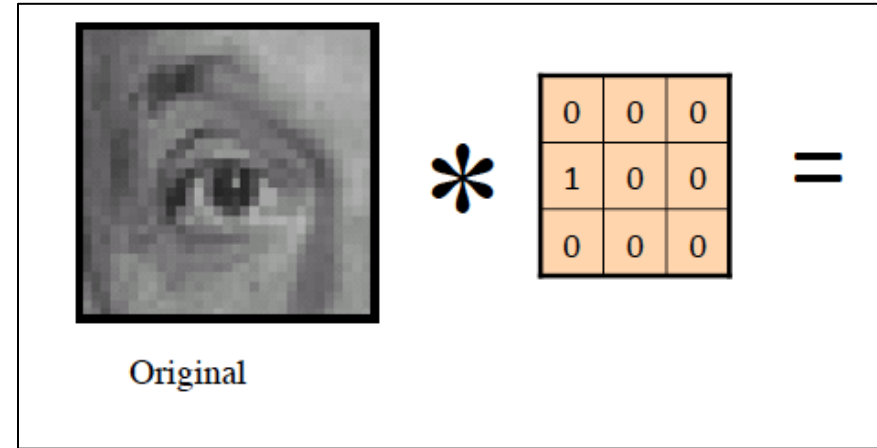
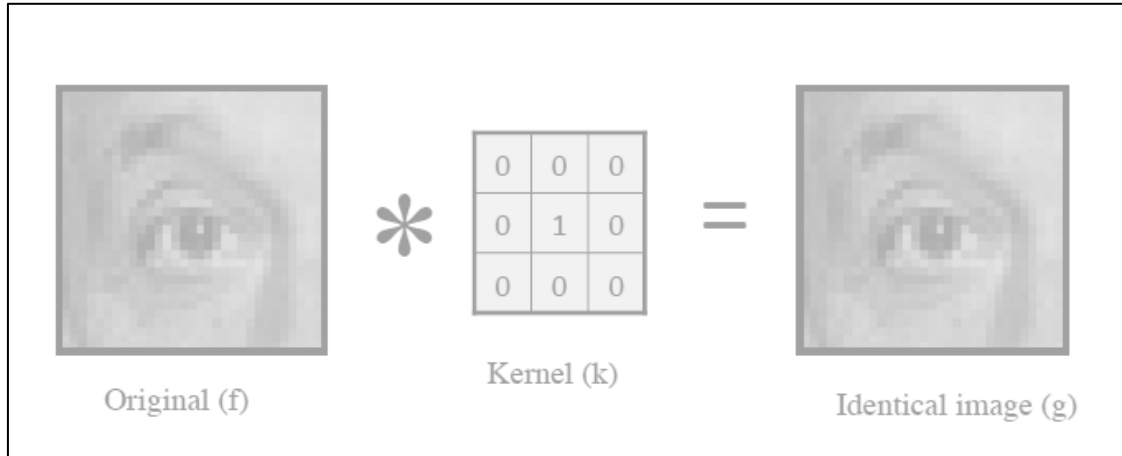


Image Convolution Examples

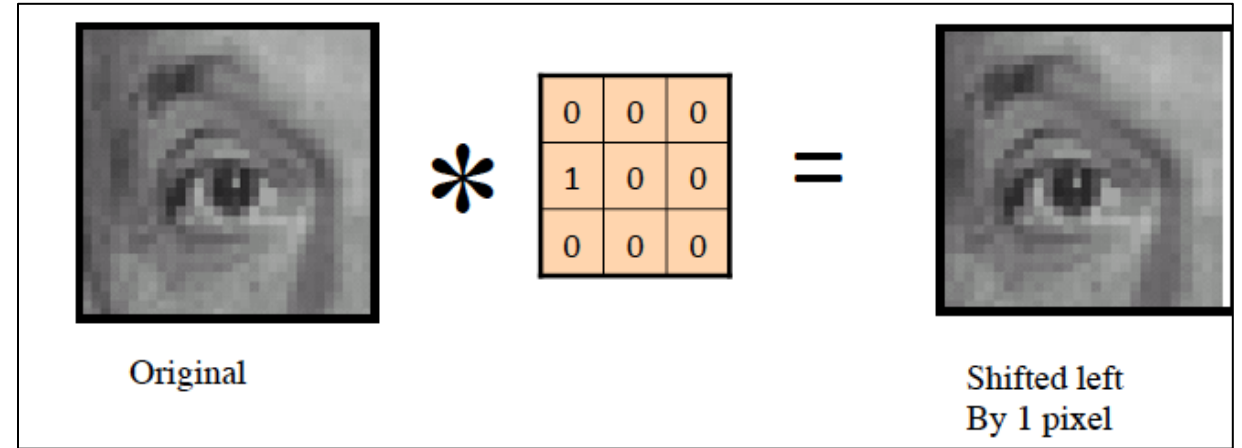
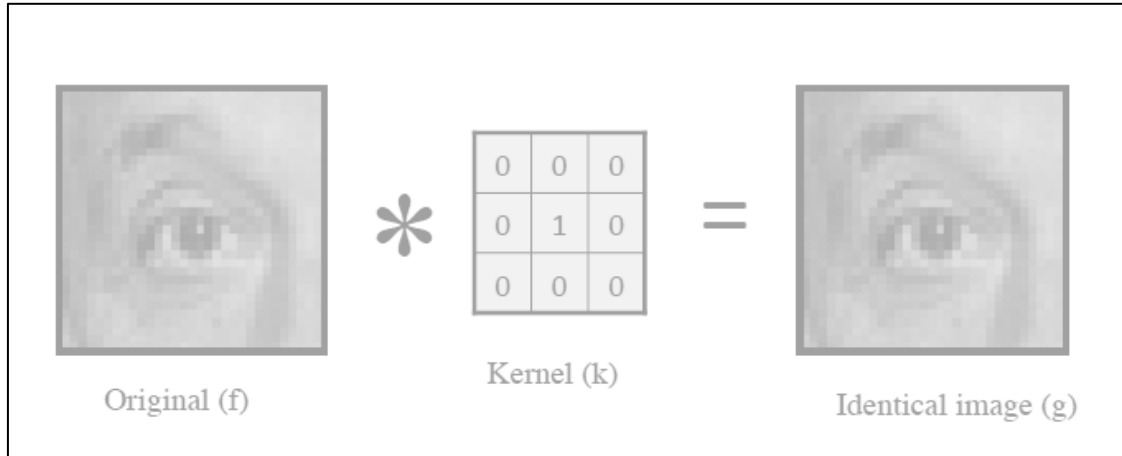


Image Convolution Examples

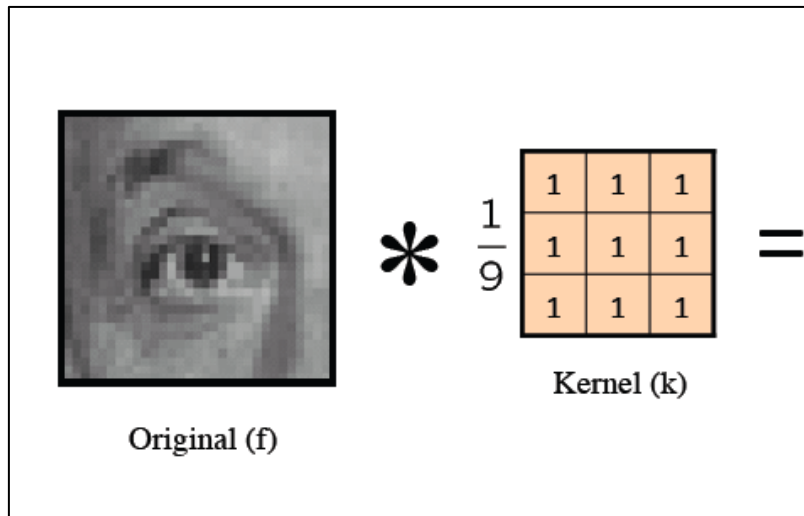
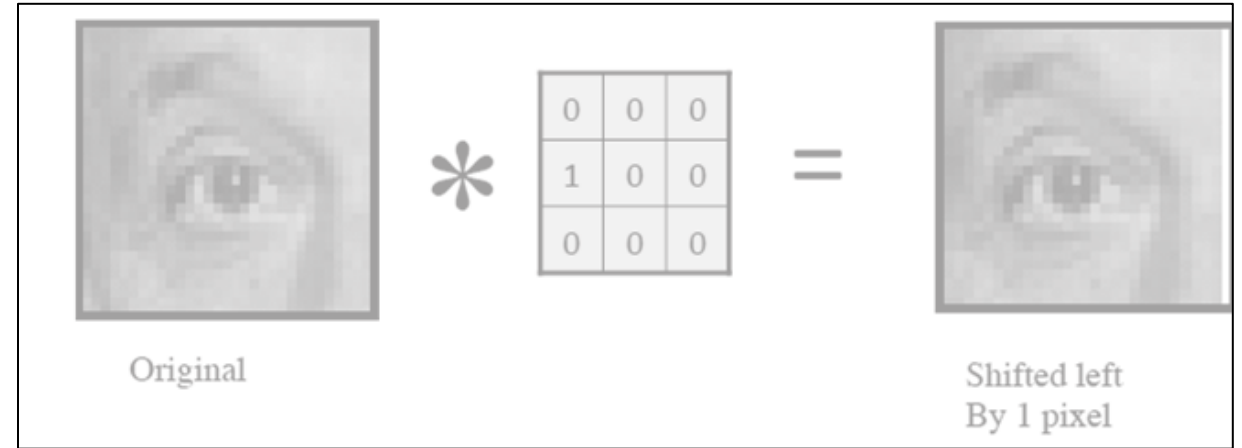
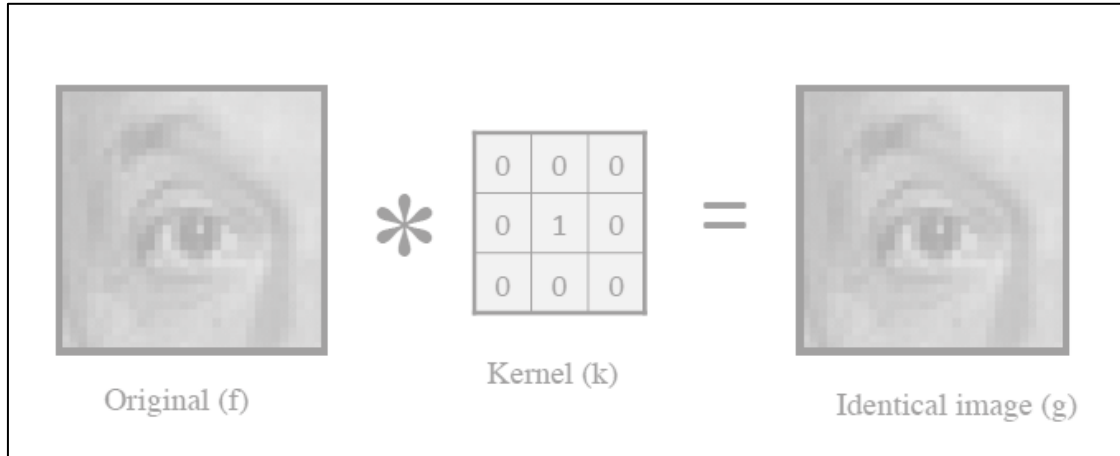


Image Convolution Examples

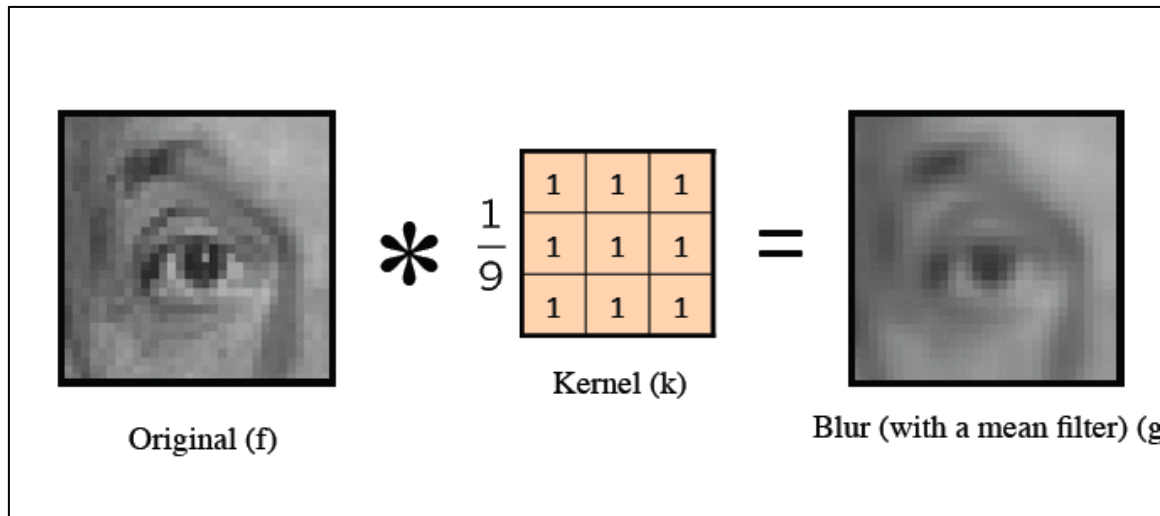
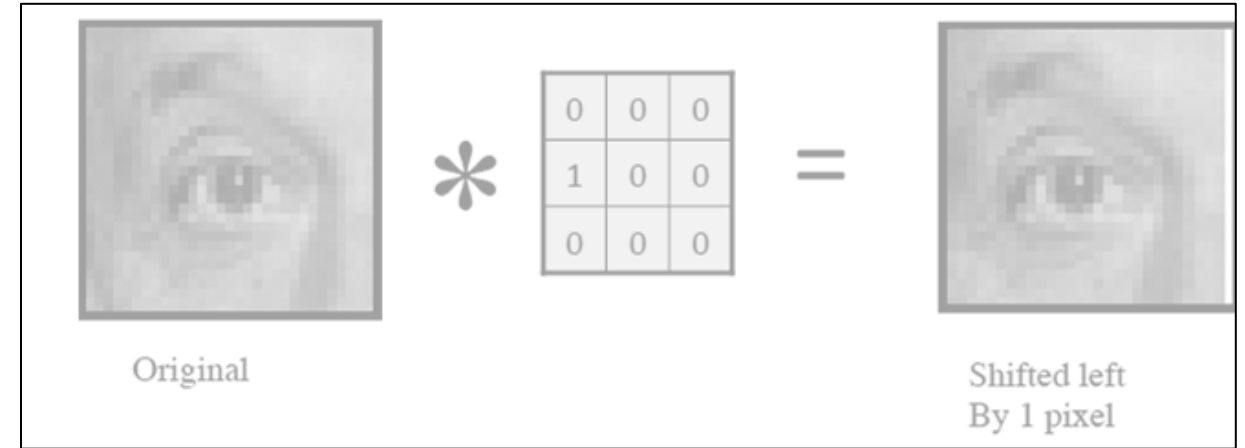
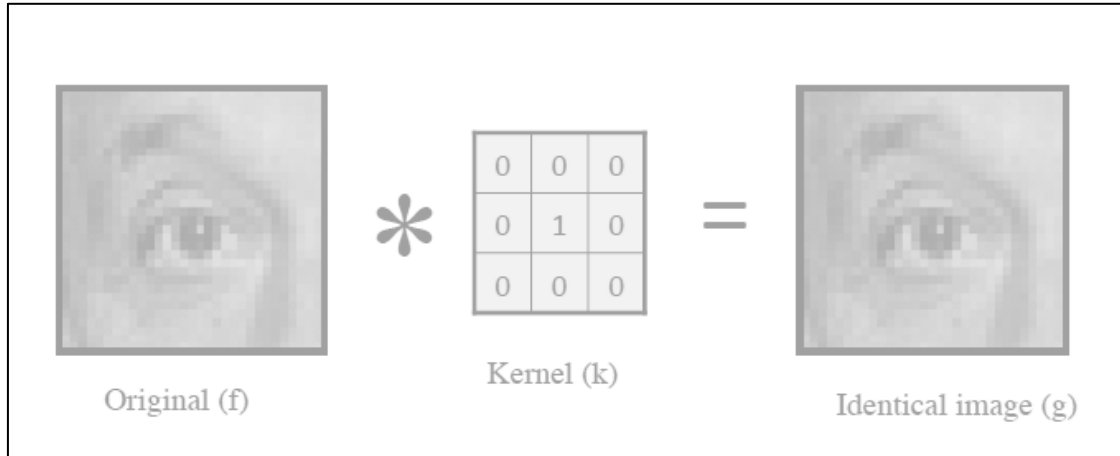
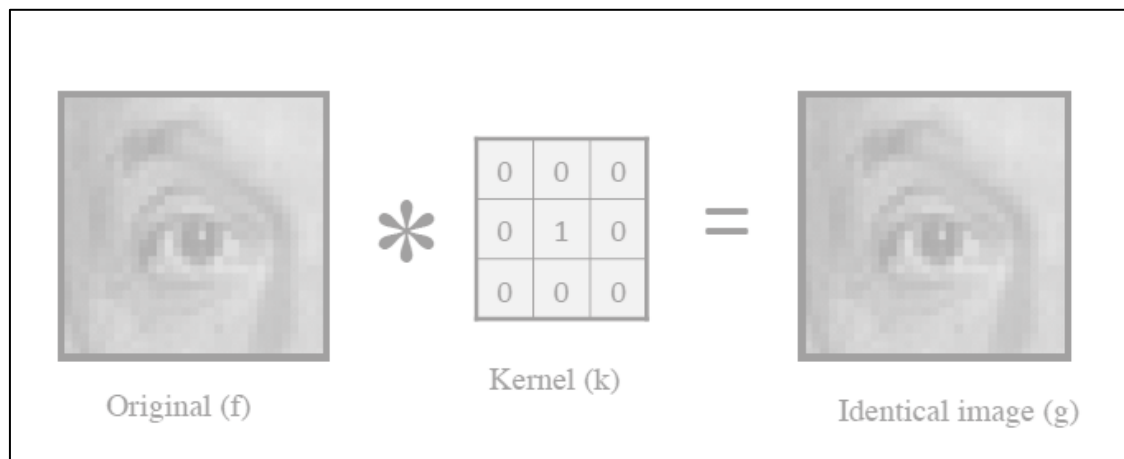


Image Convolution Examples

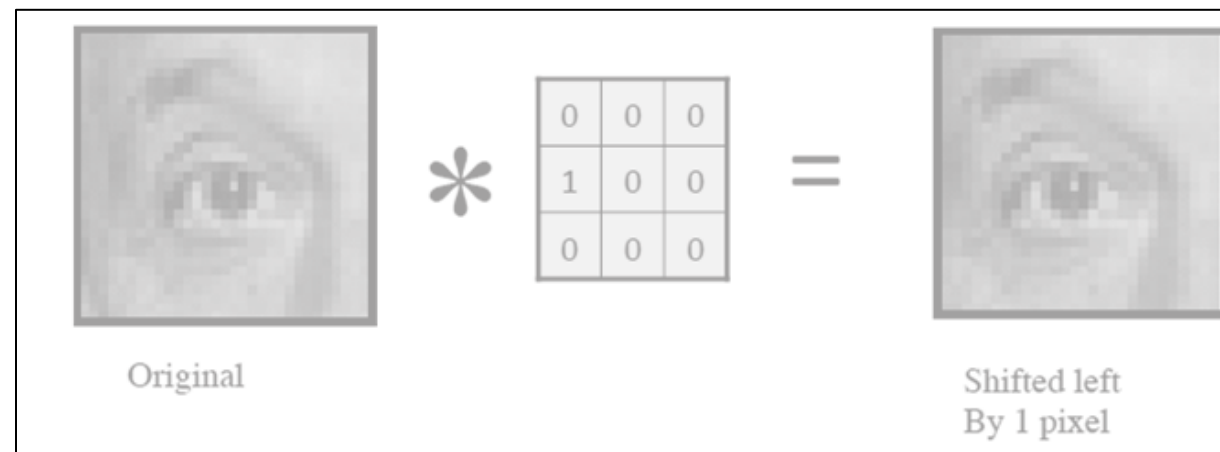


Original (f) $*$

0	0	0
0	1	0
0	0	0

 = Identical image (g)

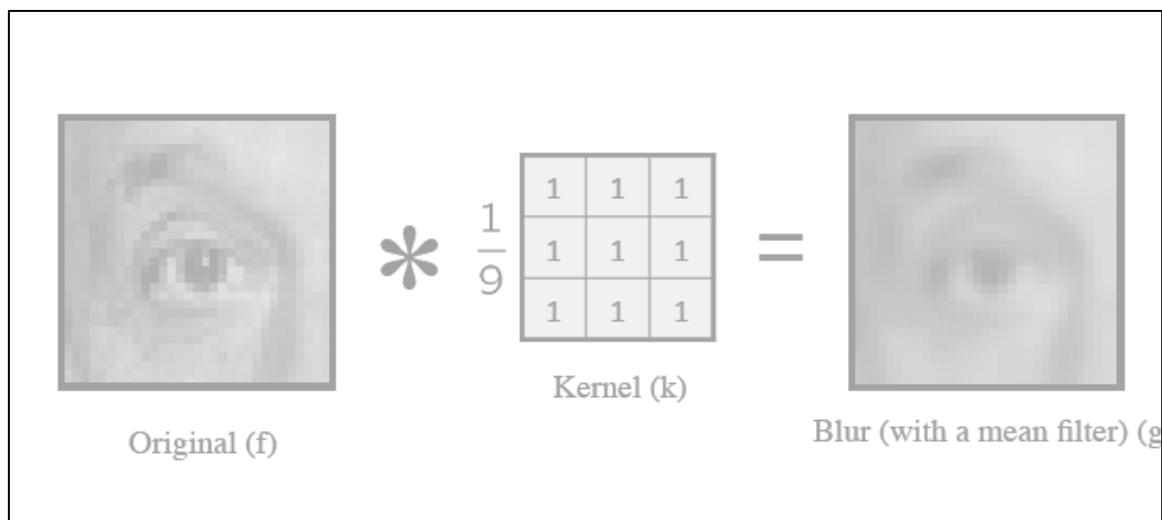
Kernel (k)



Original $*$

0	0	0
1	0	0
0	0	0

 = Shifted left
By 1 pixel

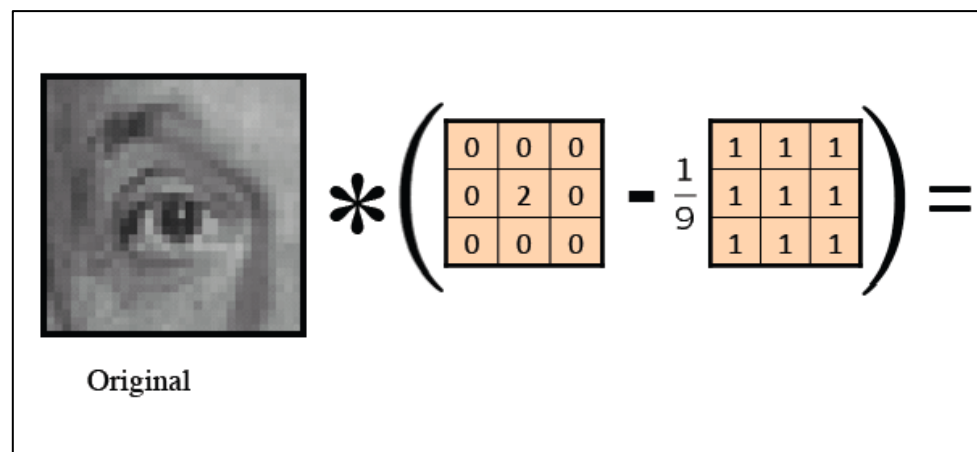


Original (f) $*$ $\frac{1}{9}$

1	1	1
1	1	1
1	1	1

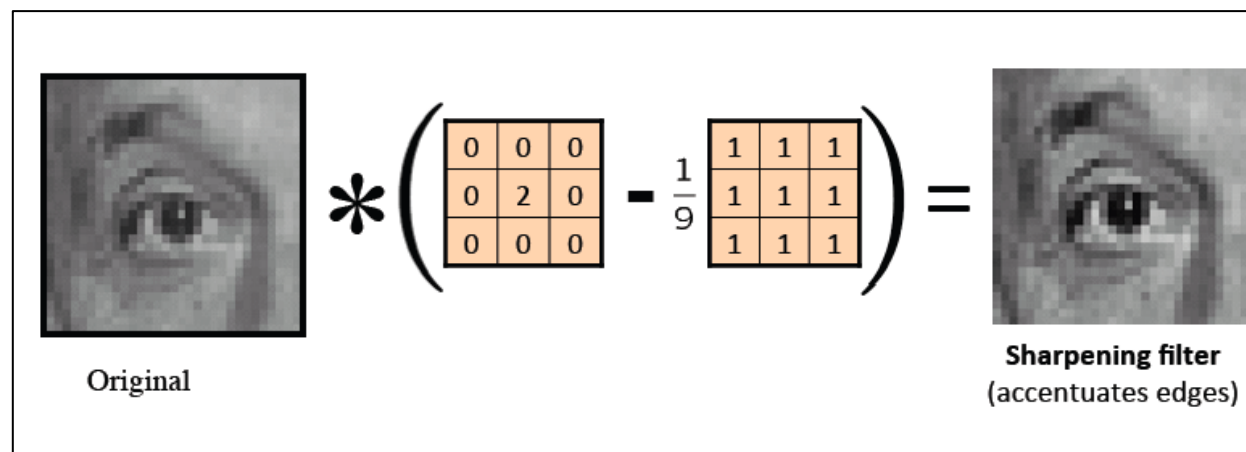
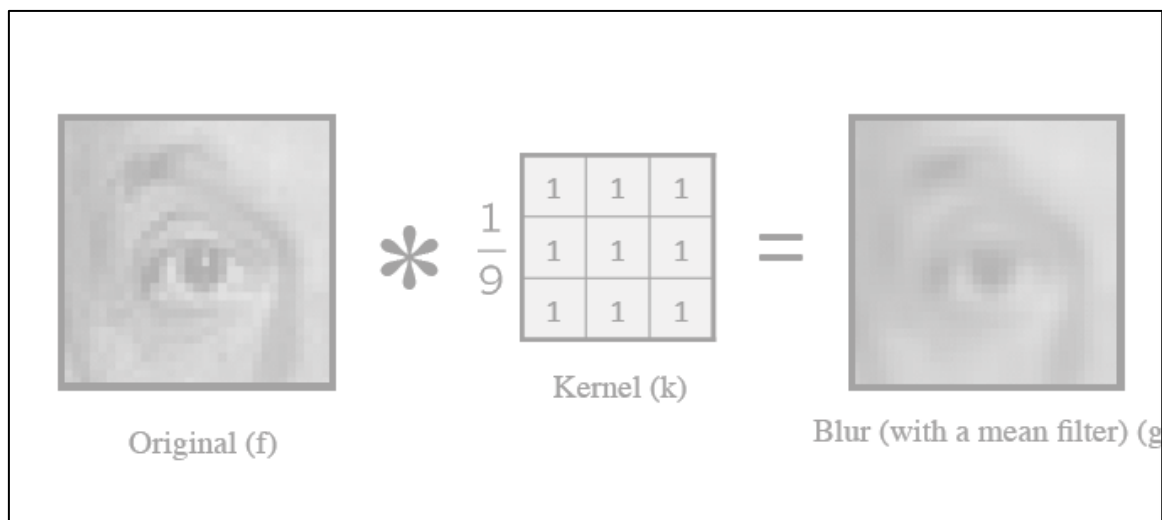
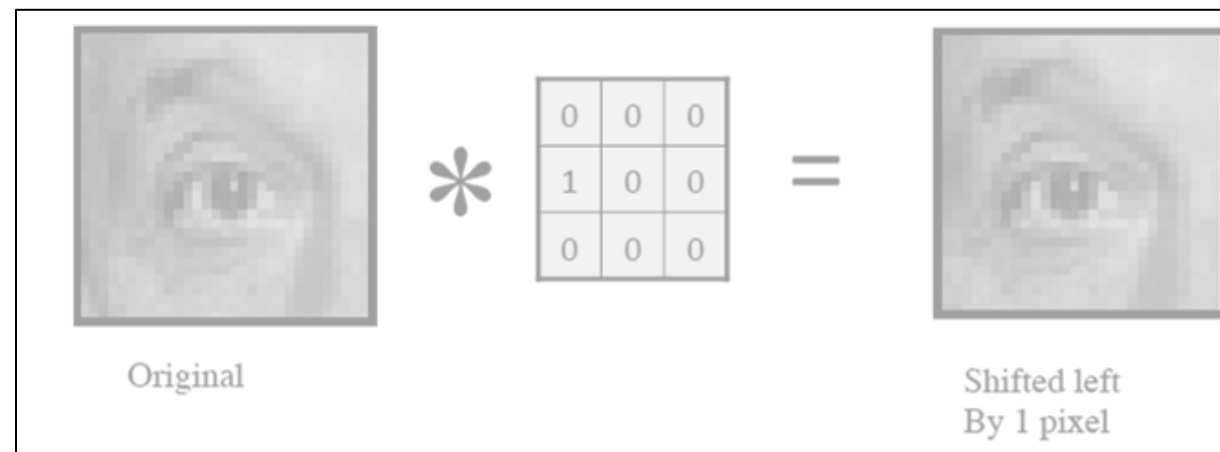
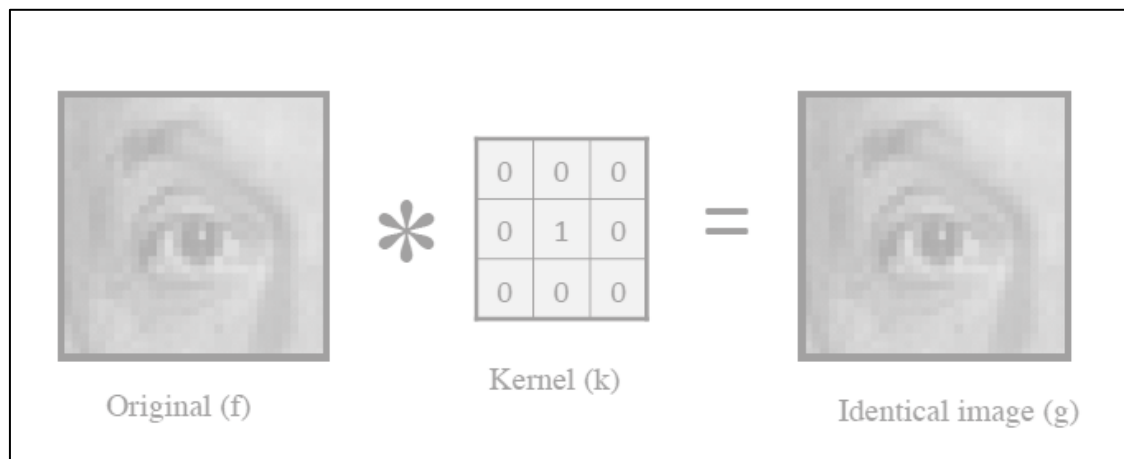
 = Blur (with a mean filter) (g)

Kernel (k)



Original $*$ $\left(\begin{matrix} \begin{matrix} 0 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 0 \end{matrix} - \frac{1}{9} \begin{matrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{matrix} \end{matrix} \right) =$

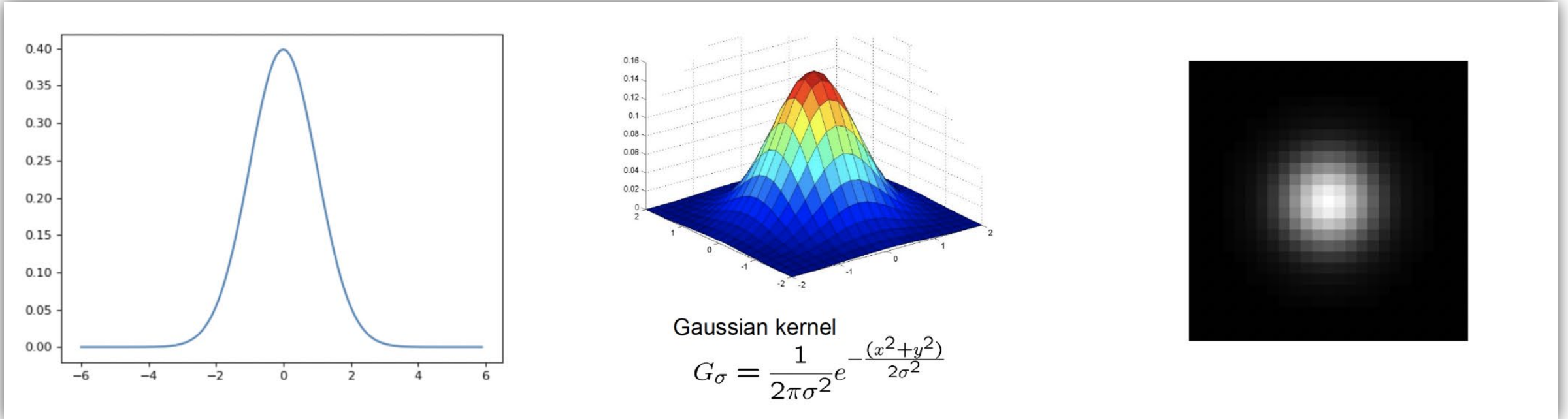
Image Convolution Examples



The Gaussian filter

- named (like many other things) after Carl Friedrich Gauss

$$f(i, j) = \frac{1}{2\pi\sigma^2} e^{-\frac{i^2+j^2}{2\sigma^2}}$$

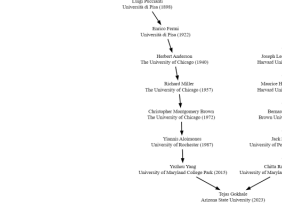
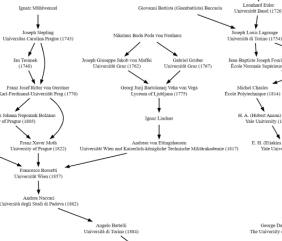
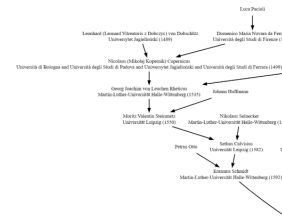
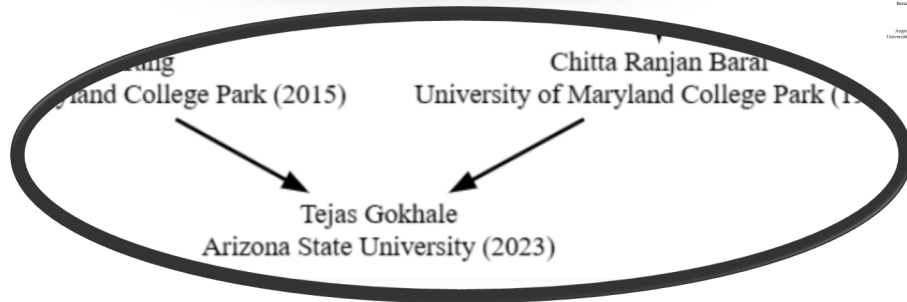
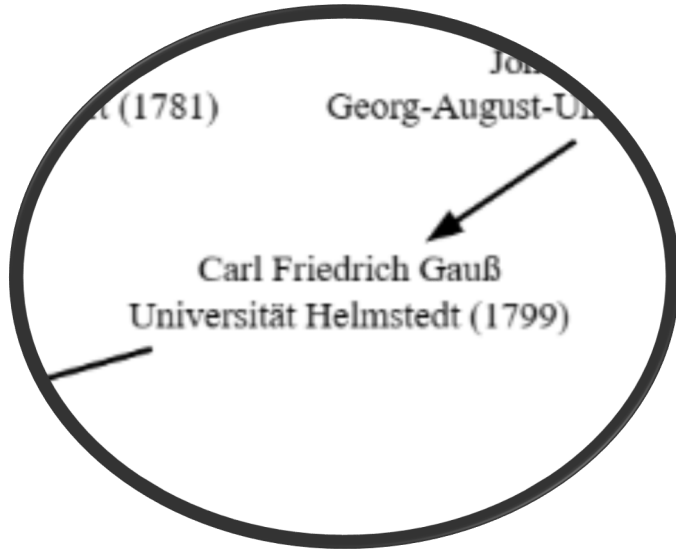
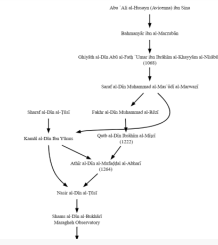


- weight falls off with distance from center pixel
- theoretically infinite, in practice truncated to some maximum distance

$$\frac{1}{16} \begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix}$$

3x3 Gaussian kernel

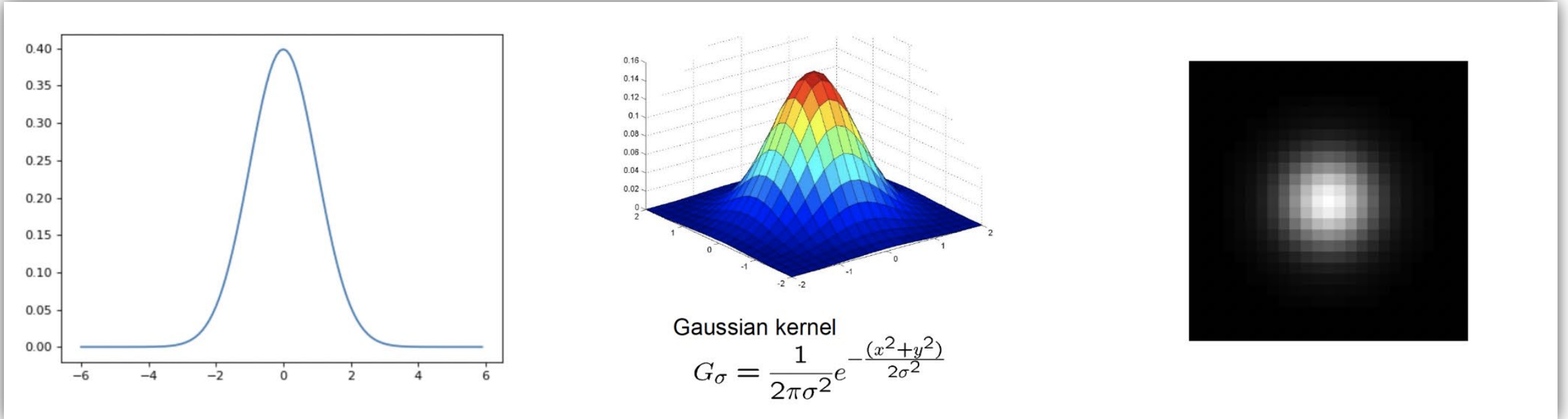
If you do a CS PhD in US/UK/EU Gauss is your ancestor (in most cases)



The Gaussian filter

- named (like many other things) after Carl Friedrich Gauss

$$f(i, j) = \frac{1}{2\pi\sigma^2} e^{-\frac{i^2+j^2}{2\sigma^2}}$$

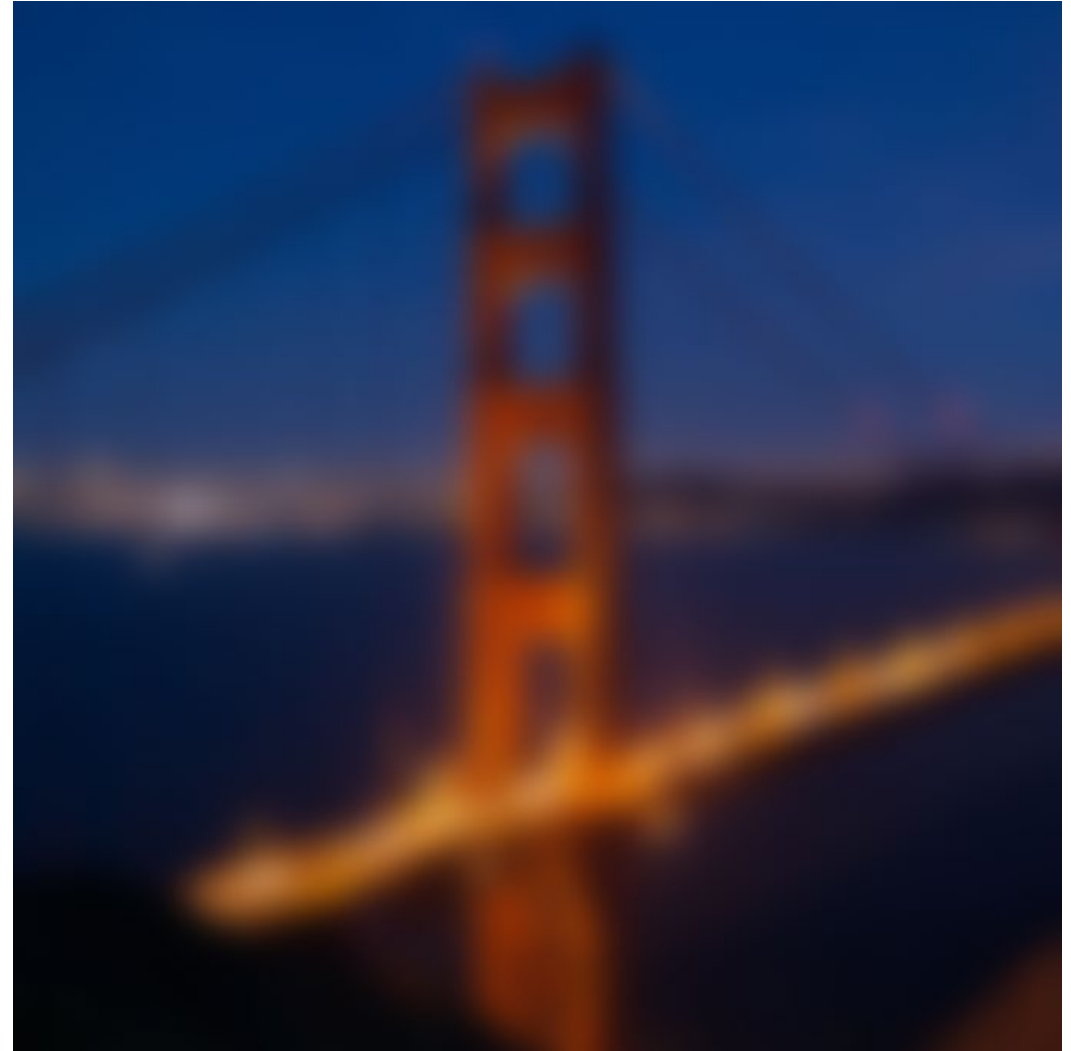


- weight falls off with distance from center pixel
- theoretically infinite, in practice truncated to some maximum distance

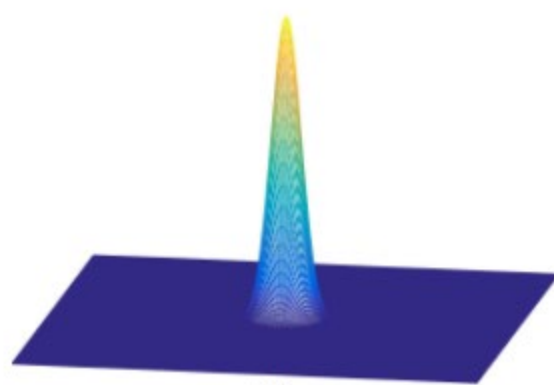
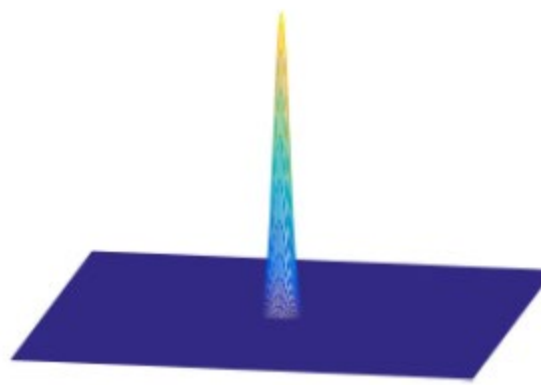
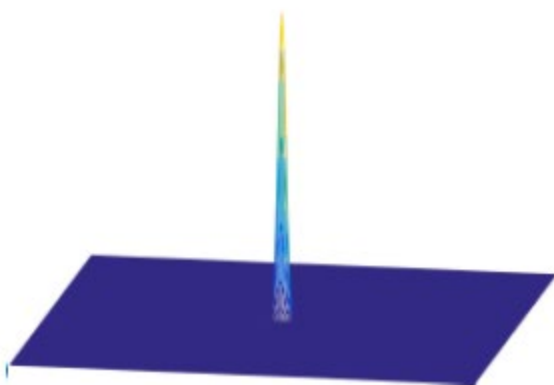
$$\frac{1}{16} \begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix}$$

3x3 Gaussian kernel

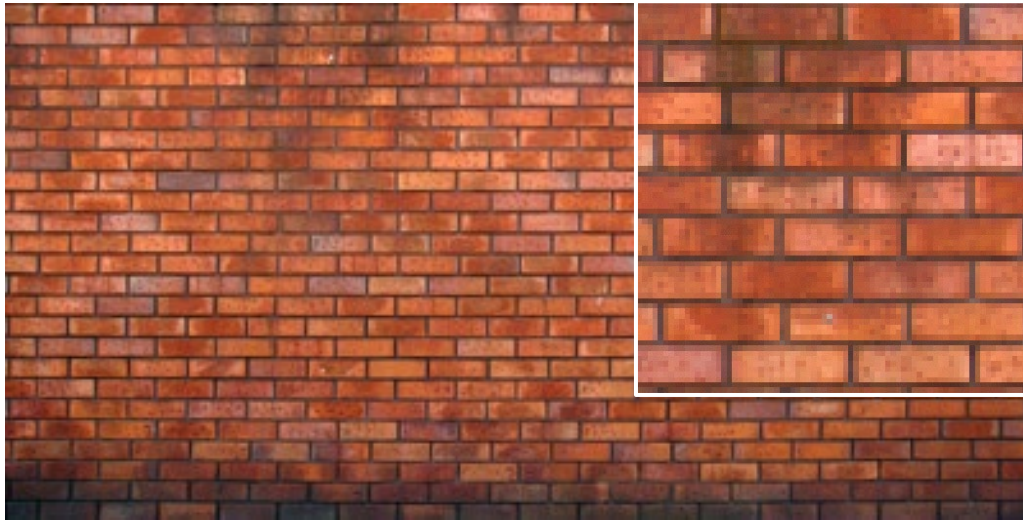
Gaussian filtering example



Scale



Gaussian vs box filtering

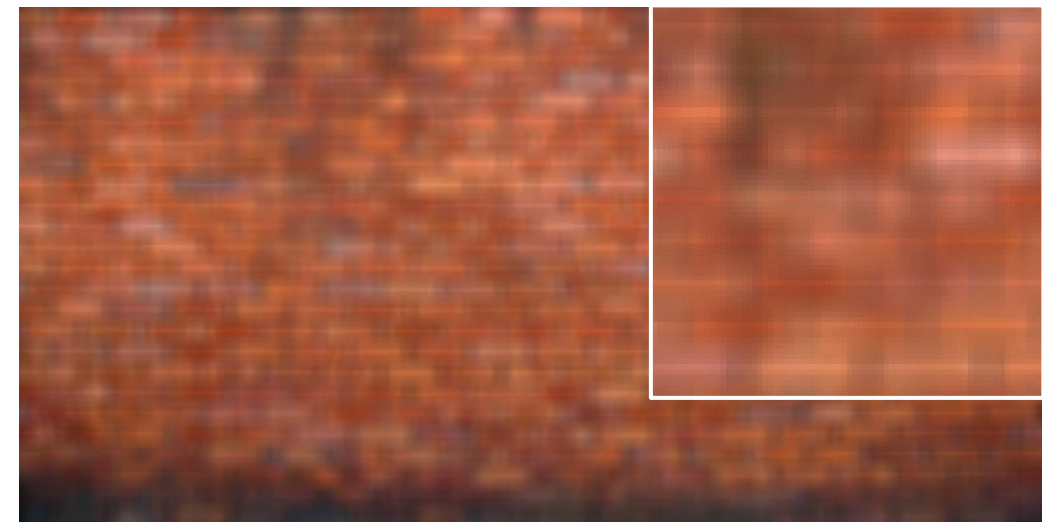


original

Which blur do you like better?



7x7 Gaussian



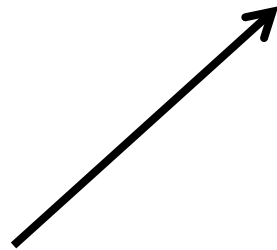
7x7 box

How would you create a soft shadow effect?

CMU



CMU



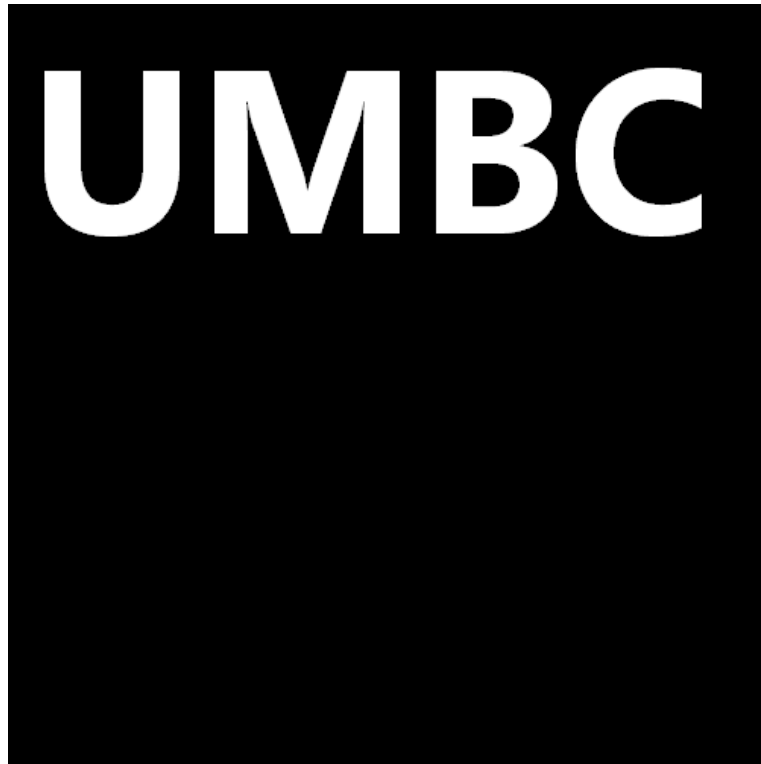
overlay

CMU

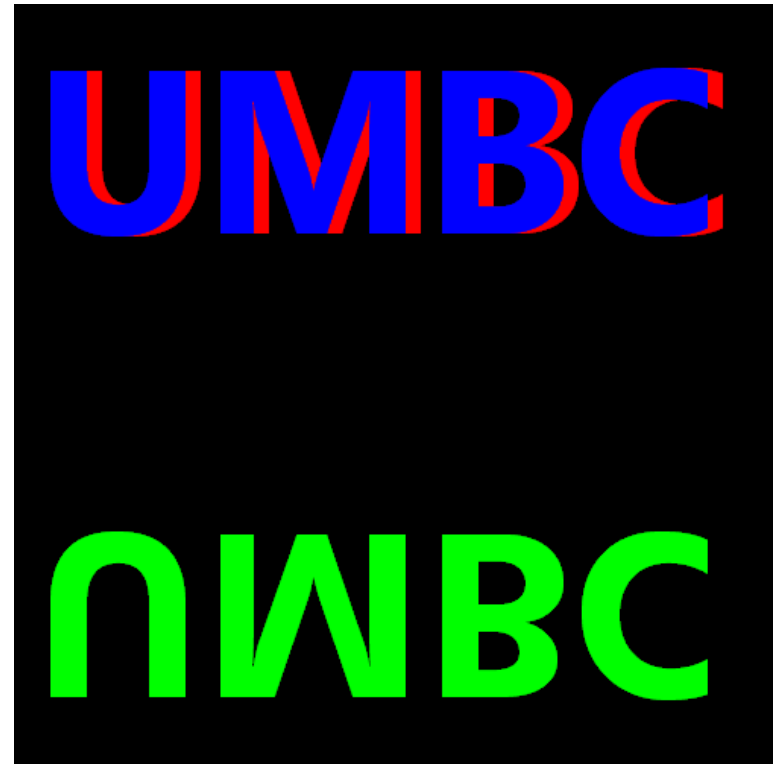
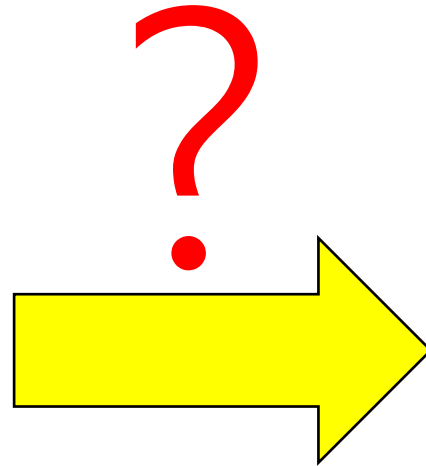
Gaussian blur

Quiz! (Bring Answers to Next Class)

Write an Equation to generate X_{out} using X , appropriate filters, point operators, etc.



X



X_{out}