Description Logics

Description Logics

- Major focus of KR research in the 80's
 - Led by Ron Brachman (AT&T Labs)
 - Grew out of early network-based KR systems like semantic networks and frames.
- Major systems and languages
 - 80s: KL-ONE, NIKL, KANDOR, BACK, CLASSIC, LOOM
 - 90s: FACT, RACER, ...
 - 00s: DAML+OIL, OWL, Pellet, Jena, FACT++
- Used as the basis for the Semantic web languages DAML+OIL and OWL
- Some commercial systems

What Are Description Logics?

- A family of logic based KR formalisms
- Descendants of semantic networks and KL-ONE
- Describe domain in terms of concepts (classes), roles (relationships) and individuals
- Distinguished by:
- Formal semantics (typically model theoretic)
 - Decidable fragments of FOL
 - Closely related to Propositional Modal & Dynamic Logics
- Provision of inference services
 - Sound and complete decision procedures for key problems
 - Implemented systems (highly optimized)

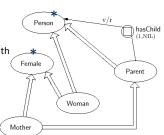
Description Logics

Thought to be well-suited for the representation of and reasoning about

- ontologies
- terminological knowledge
- Configurations and configuration problems
- database schemata
 - schema design, evolution, and query optimization
 - source integration in heterogeneous databases/data warehouses
 - conceptual modeling of multidimensional aggregation

Example of Network KR

- Person, Female, etc. are concepts
- hasChild is a property of Person
- hasChild relates Parent to Person
- Nil means infinity. A Parent is a Person with between 1 and infinity children
- Large arrows are "IS-A" links
- A Mother is a (specialization of a) Parent
- Concepts either primitive or definitions
- Primitive concepts have only necessary properties
- Defined concepts have necessary and sufficient conditions



Graphical notation introduced by KL-ONE

DL Paradigm

- A Description Logic characterized by a set of constructors that allow one to build complex descriptions or terms out of concepts and roles from atomic ones
 - Concepts correspond to classes
 - and are interpreted as sets of objects,
 - Roles correspond to relations
 - and are interpreted as binary relations on objects
- Set of axioms for asserting facts about concepts, roles and individuals

Necessary vs. Sufficient

- Necessary properties of an object are common to all objects of that type
 - Being a man is a necessary condition for being a father
- Sufficient properties allow one to identify an object as belonging to a type and need not be common to all members of the type
 - Speeding is a sufficient reason for being stopped by the police
- Definitions often specify both necessary and sufficient properties

Basic Concepts of a DL

- Individuals are treated exactly the same as constants in FOL
 - john
- Concepts are exactly the same as Unary Predicates in FOL
 - Person(john)
- Roles are exactly the same as Binary Predicates in FOL
 - has_mother(john, mary)

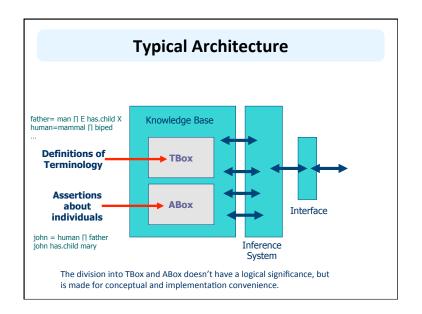
Descriptions

- Like FOL, we are dealing with (ultimately) sets of individuals and relations between them
- Basic unit of semantic significance is a Description
- "We are describing sets of individuals"
- Description logics differ in allowed operators
- If a "happy father" is a man with both a son and daughter and all of whose children are either rich or happy, we describe it in DL as

HappyFather = Man \cap ∃hasChild.Female \cap ∃hasChild.Male \cap ∀hasChild.(Rich \cup Happy)

A family of languages

- The expressiveness of a description logic is determined by the operators that it uses
- Add or eliminate operators (e.g., ¬, ∪), and the statements that can be expressed are increased/ reduced in number
- Higher expressiveness implies higher complexity
- AL or Attributive Language is the base and includes just a few operators
- Other DLs are described by the additional operators they include



AL: Attributive Language

Constructor	Syntax	Example
atomic concept	С	Human
atomic negation	~ C	~ Human
atomic role	R	hasChild
conjunction	$C \land D$	Human ∧ Male
value restriction	R.C	Human 3 hasChild.Blond
existential rest. (lim)	∃R	Human ∃ hasChild
Top (univ. conc.)	T	T
bottom (null conc)	T	T

for concepts C and D and role R

ALC

ALC is the smallest DL that is propositionally closed (i.e., includes full negation and disjunction) and include booleans (and, or, not) and restrictions on role values

constructor	Syntax	Example
atomic concept	С	Human
negation	~ C	~ (Human V Ape)
atomic role	R	hasChild
conjunction	C ^ D	Human ^ Male
disjunction	CVD	Nice V Rich
value restrict.	∃R.C	Human ∃ hasChild.Blond
existential rest.	∃R.C	Human ∃ hasChild.Male
Top (univ. conc.)	Т	Т
bottom (null conc)	Т	Τ

Other Constructors

Constructor	Syntax	Example
Number restriction	>= n R <= n R	>= 7 hasChild <= 1 hasmother
Inverse role	R-	haschild-
Transitive role	R*	hasChild*
Role composition	$R \circ R$	hasParent • hasBrother
Qualified # restric.	>= n R.C	>= 2 hasChild.Female
Singleton concepts	{ <name>}</name>	{Italy}

∀ and **∃** deserve special attention.

• Note that they only can come before a Role:

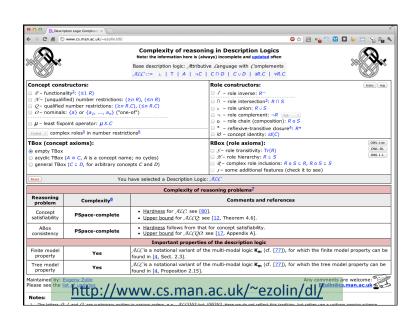
∀*HasChild.Girl* ∃*isEmployedBy.Farmer*

- Remember, they describe sets of individuals
- ∀HasChild.Girl would be interpreted as:
 The set { x | ∀(y)(HasChild(x,y) → Girl(y)) }
 Note the conditional: Are you in that set?
- ∃isEmployedBy.Farmer would be:
 The set { x | ∃(y)(isEmployedBy(x,y) ∧ Farmer(y)) }

Special names and combinations

See http://en.wikipedia.org/wiki/Description logic

- S = ALC + transitive properties
- H = role hierarchy, e.g., rdfs:subPropertyOf
- O = nominals, e.g., values constrained by enumerated classes, as in owl:oneOf and owl:hasValue
- I = inverse properties
- N = cardinality restrictions (owl:cardinality, maxCardonality)
- (D) = use of datatypes properties
- R = complex role axioms (e.g. (ir)reflexivity, disjointedness)
- Q = Qualified cardinality (e.g., at least two female children)
- → OWL-DL is SHOIN(D)
- → OWL 2 is SROIQ^(D)



Constructor	DL Syntax	Example	(Modal Syntax)	
intersectionOf	$C_1 \sqcap \ldots \sqcap C_n$	Human ⊓ Male	$C_1 \wedge \ldots \wedge C_n$	
unionOf	$C_1 \sqcup \ldots \sqcup C_n$	Doctor ⊔ Lawyer	$C_1 \vee \ldots \vee C_n$	
complementOf	$\neg C$	⊣Male	$\neg C$	
oneOf	$\{x_1 \dots x_n\}$	{john, mary}	$x_1 \vee \ldots \vee x_n$	
allValuesFrom	$\forall P.C$	∀hasChild.Doctor	[P]C	
someValuesFrom	$\exists P.C$	∃hasChild.Lawyer	$\langle P \rangle C$	
maxCardinality	$\leq nP$	≼1hasChild	$[P]_{n+1}$	
minCardinality	$\geqslant nP$	≽2hasChild	$\langle P \rangle_n$	
 XMLS datatypes as well as classes in ∀P.C and ∃P.C E.g., ∃hasAge.nonNegativeInteger 				
Arbitrarily complex nesting of constructors				
E.g., Person ∀hasChild.(Doctor ∃hasChild.Doctor)				

OWL as a DL

- OWL-DL is SHOIN^(D)
- We can think of OWL as having three kinds of statements
- Ways to specify classes
 - the intersection of humans and males
- Ways to state axioms about those classes
 - Humans are a subclass of apes
- Ways to talk about individuals
 - John is a human, john is a male, john has a child mary

OWL Axioms				
Axiom	DL Syntax	Example		
subClassOf	$C_1 \sqsubseteq C_2$	Human ⊑ Animal ⊓ Biped		
equivalentClass	$C_1 \equiv C_2$	Man ≡ Human ⊓ Male		
disjointWith	$C_1 \sqsubseteq \neg C_2$	Male ⊑ ⊣Female		
sameIndividualAs	$\{x_1\} \equiv \{x_2\}$	$\{President_Bush\} \equiv \{G_W_B$		
differentFrom	$\{x_1\} \sqsubseteq \neg \{x_2\}$	{john} ⊑ ¬{peter}		
subPropertyOf	$P_1 \sqsubseteq P_2$	hasDaughter ⊑ hasChild		
equivalentProperty	$P_1 \equiv P_2$	cost ≡ price		
inverseOf	$P_1 \equiv P_2^-$	$hasChild \equiv hasParent^-$		
transitiveProperty	$P^+ \sqsubseteq P$	ancestor ⁺ ⊑ ancestor		
functionalProperty	$\top \sqsubseteq \leqslant 1P$	⊤ ⊑ ≼1hasMother		
inverseFunctionalProperty	$\top \sqsubseteq \leqslant 1P^-$	$\top \sqsubseteq \leqslant 1 \text{hasSSN}^-$		
\mathscr{T} satisfies $C_1 \sqsubseteq C_2$ iff $C_1^{\mathcal{I}} \subseteq C_2^{\mathcal{I}}$; satisfies $P_1 \sqsubseteq P_2$ iff $P_1^{\mathcal{I}} \subseteq P_2^{\mathcal{I}}$				
\mathscr{T} satisfies ontology $\mathcal O$ (is a model of $\mathcal O$) iff satisfies every axiom in $\mathcal O$				
Logical Foundations for the Semantic Web – p. 18/3				

Subsumption: $D \subseteq C$?

- Concept C subsumes D iff on every interpretation I
 - $-I(D)\subseteq I(C)$
- This means the same as ∀(x)(D(x) → C(x)) for complex statements D & C
- Determining whether one concept *logically* contains another is called the *subsumption problem*.
- Subsumption is undecidable for reasonably expressive languages
 - e.g.; for FOL: does one FOL sentence imply another
- and non-polynomial for fairly restricted ones

Other reasoning problems

These problems can be reduced to subsumption (for languages with negation) and to the satisfiability problem, as well

• Concept satisfiability is C (neccessarilty) empty?

• **Instance Checking** Father(john)?

• **Equivalence** CreatureWithHeart ≡ CreatureWithKidney

• Disjointness C ∏ D

• **Retrieval** Father(X)? X = {john, robert}

• **Realization** X(john)? X = {Father}

Definitions

- A definition is a description of a concept or a relationship
- It is used to assign a meaning to a term
- In description logics, definitions use a specialized logical language
- Description logics are able to do limited reasoning about concepts defined in their logic
- One important inference is classification (computation of subsumption)

Necessary vs. Sufficient

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Subsumption

Meaning of Subsumption

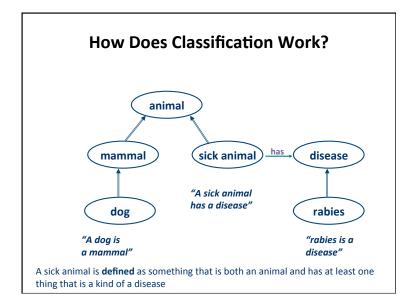
A more general concept or description is said to **subsume** a more specific one. Members of a subsumed concept are necessarily members of a subsuming concept

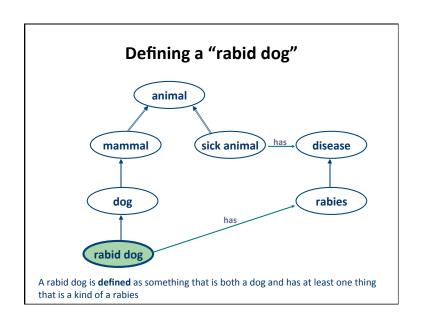
- Two ways to formalize the meaning of subsumption
 - Using logic
 - Satisfying a subsumed concept implies that the subsuming concept is satisfied also

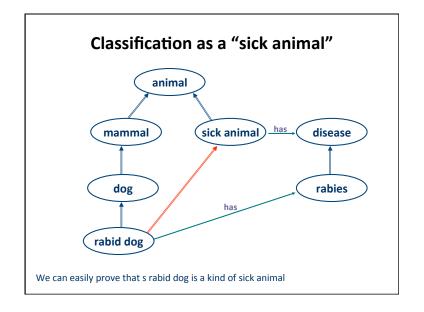
E.g., if john is a person, he is also an animal

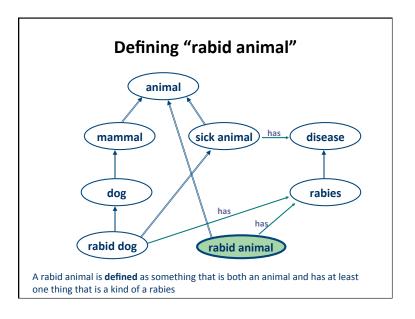
- Using set theory
 - The instances of subsumed concept are necessarily a subset of the subsuming concept's instances

E.g., the set of all persons is a subset of all animals









Primitive versus Structured (Defined)

- Description logics reason with definitions
 - They prefer to have *complete* descriptions
 - A complete definition includes both necessary conditions and sufficient conditions
- This is often impractical or impossible, especially with natural kinds.
- A "primitive" definition is an incomplete definition
 - This limits the amount of classification that can be done automatically
- Example:

- Primitive: a Person

- Defined: Parent = Person with at least one child

DL reasoners places concepts in hierarchy **Note:** we can remove the subclass link from rabid animal to animal because it is redundant. We don't need to. But animal humans like to see the simplest structure and it may be informative for agents as well. has sick animal disease mammal rabid animal dog rabies rabid dog We can easily prove that s rabid dog is a kind of rabid animal

Intentional versus Extensional Semantics

- Extensional Semantics are a model-theoretic idea. They define the meaning of a description by enumerating the set of objects that satisfy the description.
- Intensional Semantics defines the meaning of a description based on the intent or use of the description.
- Example:
 - Morning-Star Evening-Star
 - Extensional: Same object, namely Venus
 - Intensional: Different objects, one meaning Venus seen in the morning and one in the evening.

Definition vs. Assertion

- A definition describes intrinsic properties of an object. The parts of a description have meaning as a part of a composite description of an object
- An assertion is used to describe an incidental property of an object. Asserted facts have meaning on their own.
- Example: "a black telephone"
 Could be either a description or an assertion, depending on the meaning and import of "blackness" on the concept telephone.

Definition versus Assertion

- In English, "a black telephone" is ambiguous
 - (1) A black telephone is a common sight in an office
 - (2) A black telephone is on the corner of my desk
- KR languages should not be ambiguous so typically distinguish between descriptions of classes and descriptions of individuals
- KR languages often allow additional assertions to be made that are not part of the definition (e.g., annotation properties in OWL)

Classification is very useful

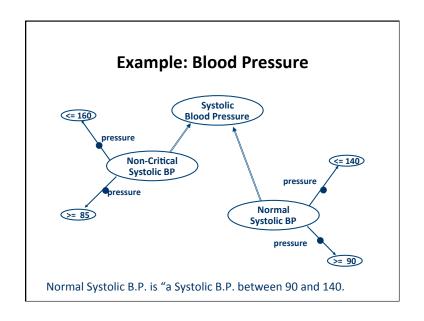
- Classification is a powerful kind of reasoning that is very useful
- Many expert systems can be usefully thought of as doing "heuristic classification"
- Logical classification over structured descriptions and individuals is also quite useful
- But... can classification ever deduce something about an individual other than what classes it belongs to?
- And what does *that* tell us?

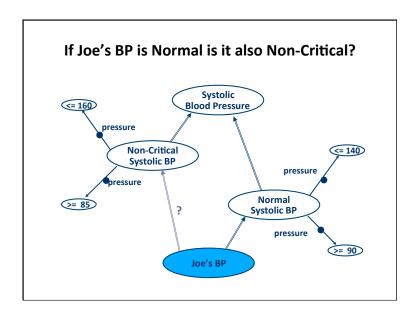
Example: Blood Pressure Systolic Blood Pressure Non-Critical Systolic BP

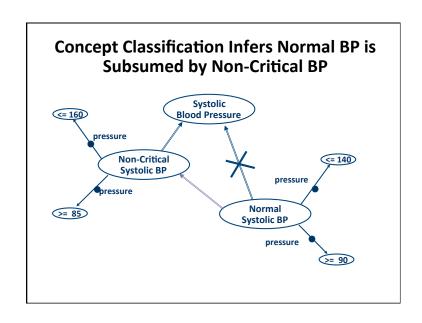
A Non-Critical Blood Pressure is "a Systolic

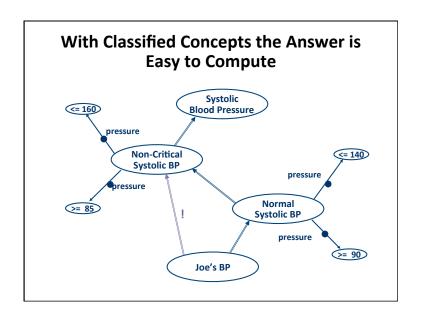
B.P. between 85 and

160."



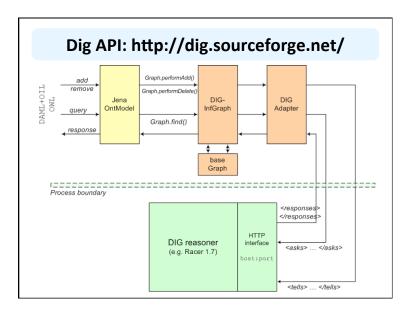






Incidental properties

 If we allow incidental properties (e.g., ones that don't participate in the description mechanism) then these can be deduced via classification



Some DL reasoners

- •See http://en.wikipedia.org/wiki/Description logic
 - CEL, free (for non-commercial use), LISP
 - Cerebra Engine, commercial, C++
 - FaCT++, free, open-source, C++
 - KAON2 free (for non-commercial usage), Java
 - MSPASS free, open-source, C
 - Pellet free, open-source, Java
 - RacerPro commercial, LISP
- DIG is a standard interface to a DL reasoner that predates RDF and today uses XML
- Protégé uses DIG and can thus use any of several DL reasoners that have a DIG interface