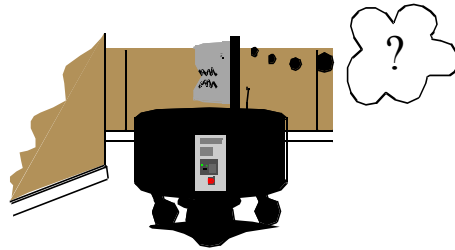


# Localization

*where am I? (again?)*

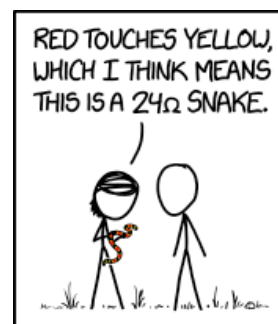


## Bookkeeping



2

- ◆ Assignment 3
  - ◆ Comments?
- ◆ Next Reading: *none*
  - ◆ Unless you are behind; catch up
- ◆ Today
  - ◆ Knowledge Representation
    - ◆ Maps
    - ◆ Belief states
- ◆ Upcoming
  - ◆ Grades



*The last band of color indicates the snake's tolerance for being held before biting.*

## Localization Review (1)



3

- ◆ What is localization?
  - ◆ Figuring out location wrt. a model of the world
- ◆ What are the two purely proprioceptive approaches?
  - ◆ Odometry: belief about motion only
    - ◆ Wheel encoders, mostly
  - ◆ Dead reckoning: belief about motion + heading sensors

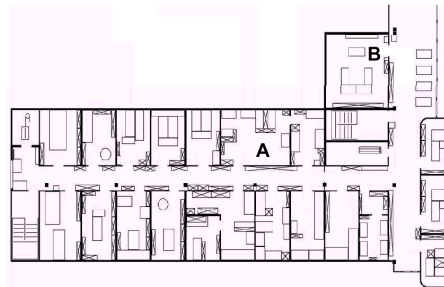
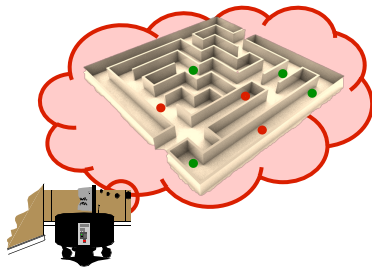


## Localization Review (2)



4

- ◆ What is sensor aliasing?
  - ◆ Different locations giving the same sensor readings
- ◆ What is behavior-based navigation?
  - ◆ Navigating without localizing



# Belief Representations



5

- ◆ (Model of) the *map* or *environment*
    - ◆ Discrete vs. continuous
    - ◆ Probabilistic vs. labeled
    - ◆ Geometric vs. topographical vs. semantic
  - ◆ Beliefs about the robot's *state* or *location*
    - ◆ Discrete vs. continuous
    - ◆ Probabilistic vs. bounded vs. point
    - ◆ Single vs. multiple hypotheses
  - ◆ Paths
    - ◆ Consecutive vs. kidnapped
- Design decisions:  
based on storage  
efficiency,  
reasoning speed,  
sensor capability,  
intended task, ...

# Map Representations



6

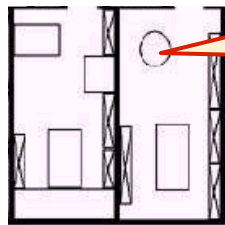
- ◆ How precise does it have to be?
  - ◆ To accomplish what?
- ◆ What types of features are represented?
  - ◆ Depends on robot's sensors
    - ◆ If the robot can't see it, no point storing it
  - ◆ How much processing power do we have?
- ◆ What characteristics does it have?

# Characterizing Maps (1)



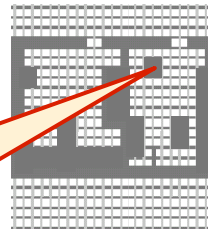
7

◆ Discrete vs. continuous



Continuous

Obstacles represented as polygons



Discretized

Obstacles represented as blocks in a grid

# Characterizing Maps (2)



8

◆ Geometric vs. topological



Geometric

Actual locations of obstacles and areas



Topological

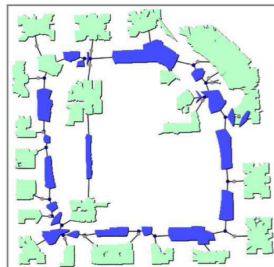
Relative locations

## Characterizing Maps (3)

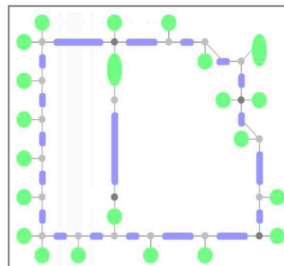


9

- ◆ Semantically labeled
  - ◆ Example: semantically labeled topological map



Topological



Semantic

Room

Hall

Junction

## Location (Belief) Representation



10

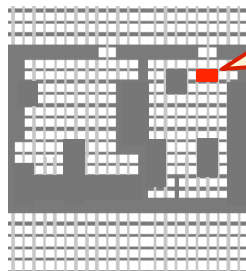
- ◆ What characteristics does it have?
- ◆ Discrete vs. continuous
  - ◆ Fixed to a grid, or anywhere?
- ◆ Single vs. multiple hypotheses
  - ◆ At any given time, how many possible locations are being considered?
- ◆ Probabilistic vs. bounded vs. point
  - ◆ The first two are multiple-hypothesis

# Characterizing Belief R. (1)



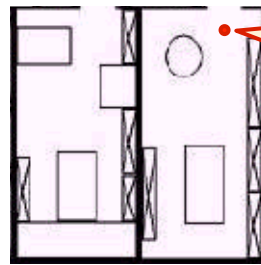
11

- ◆ Discrete vs. continuous
  - ◆ Fixed to a grid vs. infinitely fine resolution



Discrete

In one of these



Continuous

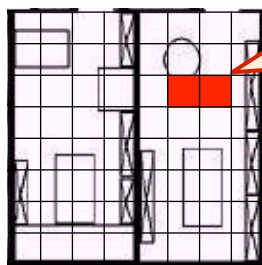
$\{x = 81.1, y = 14.2\}$

# Characterizing Belief R. (1.1)



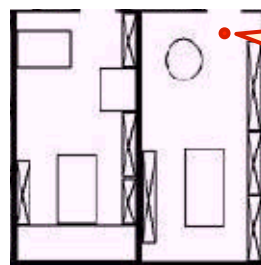
12

- ◆ Discrete vs. continuous
  - ◆ **Belief** can be discretized on a **continuous** map



Discrete

In one of these



Continuous

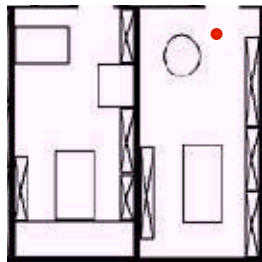
$\{x = 81.1, y = 14.2\}$

## Characterizing Belief R. (2)

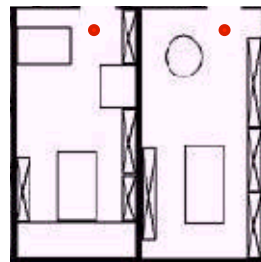


13

- ◆ Single hypothesis vs. multiple hypothesis



Single



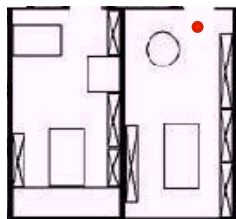
Multiple

## Characterizing Belief R. (3)

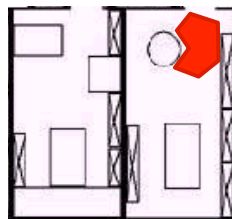
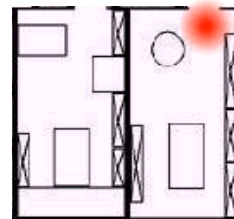


14

- ◆ Probabilistic vs. bounded vs. point



Point

Bounded  
Polygon

Probabilistic

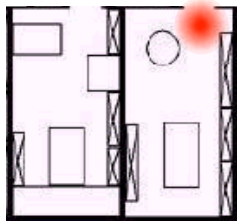
- ◆ You are here
- ◆ Somewhere in here (undifferentiated)
- ◆ Spread of likelihood

# Probability & Combinations

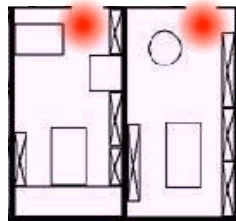


15

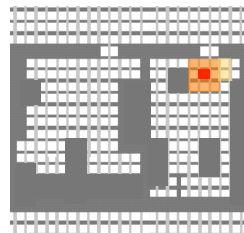
- ◆ Single or multiple, discrete or continuous



Single Hypothesis



Multiple Hypothesis



Discrete

- ◆ Point: these are orthogonal choices

# Belief Representation



16

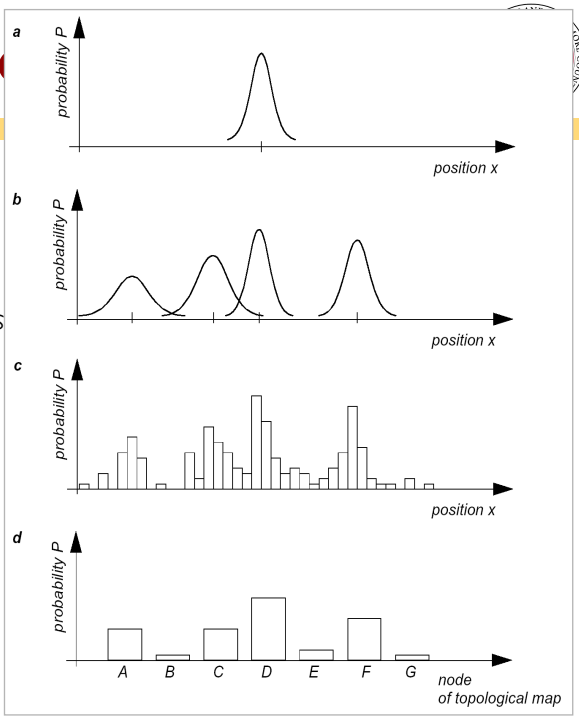
- ◆ a) Continuous map with *single hypothesis*
- ◆ b) Continuous map with *multiple hypothesis*
- ◆ d) Discretized map with probability distribution
- ◆ d) Discretized topological map with probability distribution



# Belief Repro

17

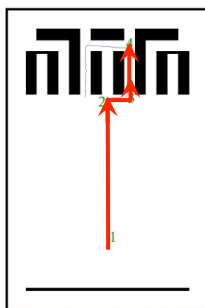
- ◆ a) Continuous map with *single hypothesis*
- ◆ b) Continuous map with *multiple hypothesis*
- ◆ d) Discretized map with probability distribution
- ◆ d) Discretized topological map with probability distribution



# Example



18



Path of the robot

Belief states at positions 2, 3 and 4

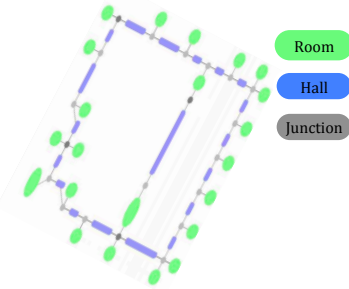
- ◆ Location: Probabilistic? Discrete? **yes, no**
- ◆ Map: Discretized? Topological? **maybe? no, geometric**

# The Environment



19

- ◆ Can contain:
  - ◆ Static or dynamic obstacles
  - ◆ Features (e.g., doors, floor tiles)
- ◆ Can be semantically labeled
- ◆ Environment Representation
  - ◆ Continuous Metric →  $\{x,y,\theta\}$
  - ◆ Discrete Metric → metric grid (eg, sq. D76)
  - ◆ Discrete Topological → topological grid

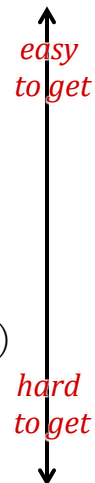


# The Environment: Features



20

- ◆ Raw sensor data (ex.: laser range, grayscale images)
  - ◆ Lots of data, low distinctiveness (per reading)
  - ◆ Uses all acquired information
- ◆ Low level features (ex.: line extraction)
  - ◆ Some data, average distinctiveness
  - ◆ Filters out some useful information, still ambiguities
- ◆ High level features (ex.: doors, a car, the Eiffel tower)
  - ◆ Little data, high distinctiveness
  - ◆ Filters out the useful information, few/no ambiguities, insufficient environmental information



# About Map Representations



21

1. Map precision vs. application
  - ◆ How precise does it need to be?
2. Features precision vs. map precision
  - ◆ 20cm. map precision  $\neq$  20cm. obstacle avoidance
3. Precision vs. computational complexity
  - ◆ More capability = more computational complexity
  - ◆ Continuous Representation
  - ◆ Decomposition (Discretization)

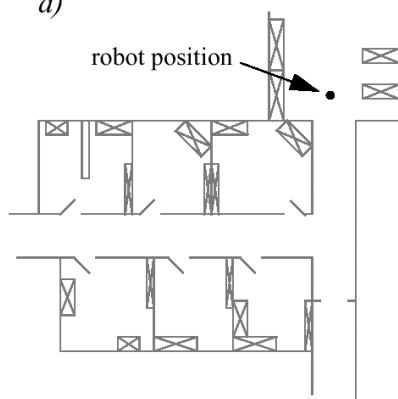
# Map Representations



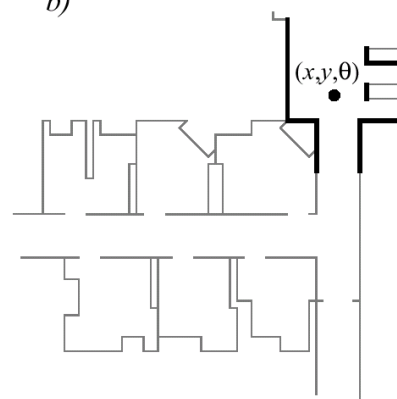
22

- ◆ Continuous line, single hypothesis

a)



b)



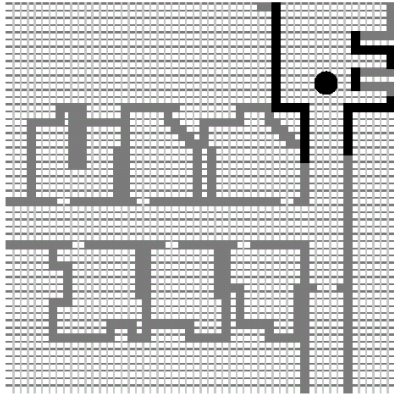
# Map Representations



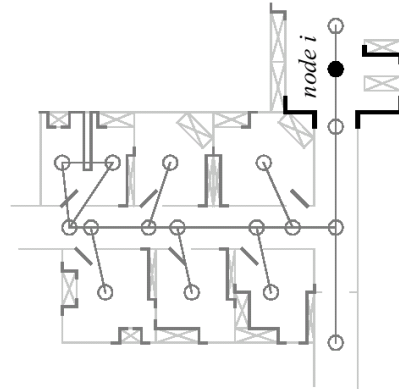
23

- ◆ Single hypothesis – Grid and Topological Map

c)



d)

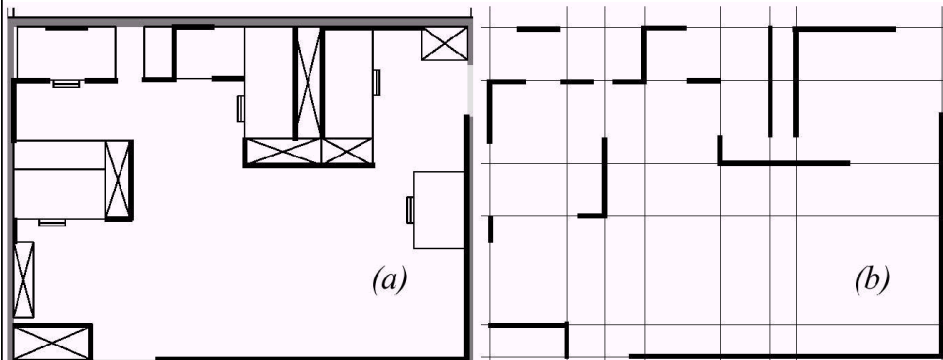


# Continuous Line Based



24

- a) Representation with set of infinite lines (line extraction)



(a)

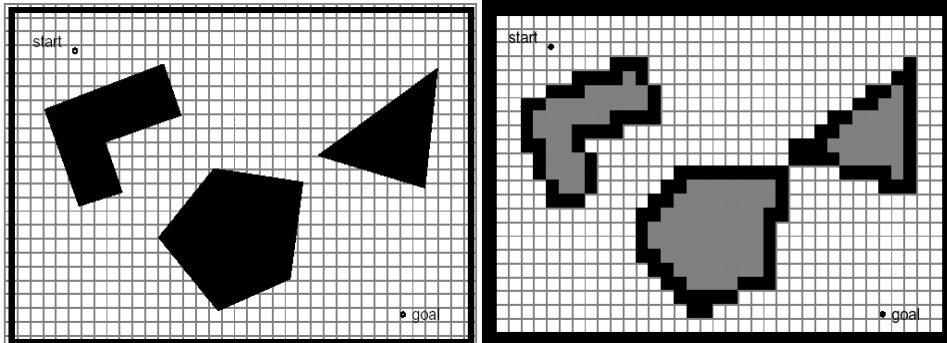
(b)

# Map Decomposition (1)



27

- ◆ Fixed cell decomposition
- ◆ Narrow passages disappear

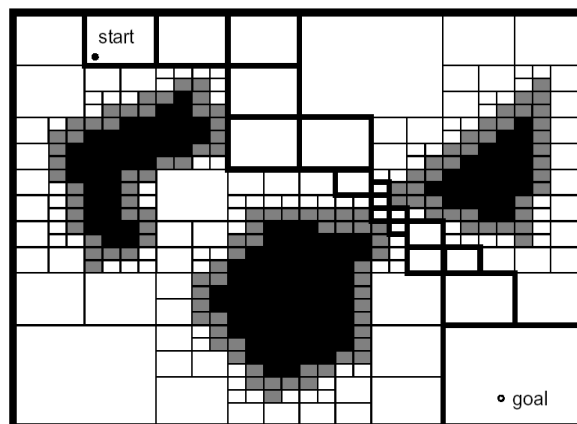


# Map Decomposition (2)



28

- ◆ Adaptive cell decomposition

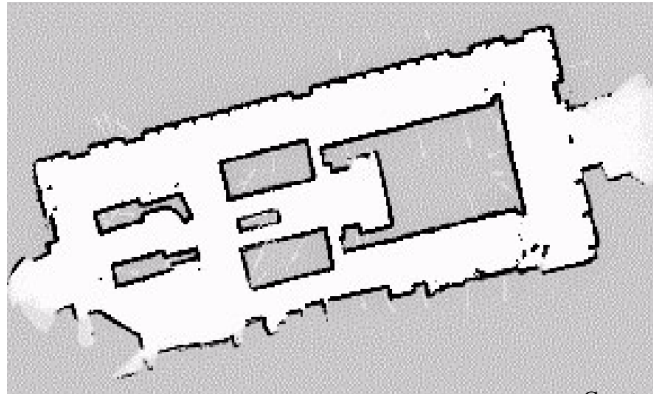


## Map Decomposition (3)



29

- ◆ Fixed cell decomposition – Example with very small cells



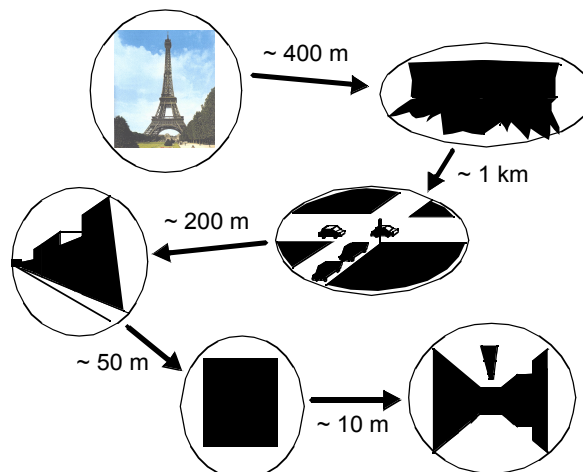
Courtesy of S. Thrun

## Map Decomposition (4)



32

- ◆ Topological Decomposition

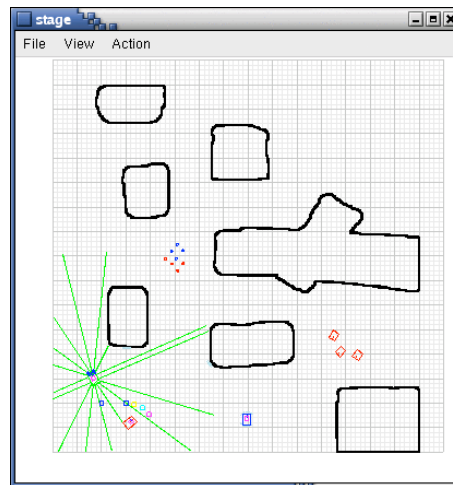


## Map Decomposition (5)



33

### ◆ Occupancy Grid



## Probabilistic Map-Based Localization



35

- ◆ Consider a mobile robot moving in a known environment
- ◆ As it starts to move from a precisely **known location**, it might **keep track of its location using odometry**.
- ◆ However, after a certain movement the robot will **get very uncertain about its position**.
- ➔ update using an **observation of its environment**.
- ◆ observation lead also to an **estimate of the robots position** which can then be **fused** with the **odometric estimation** to get the best possible **update of the robots actual position**.

