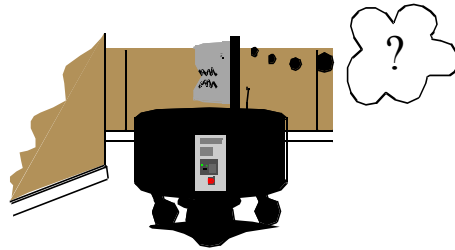


# Localization

*where am I?*



## Bookkeeping



2

- ◆ Quiz 3 – short review
- ◆ Assignment 3: How Thursday will work
- ◆ Next Reading: SNS 5.5 – 5.6.4
- ◆ Today
  - ◆ Scheduling for demos & presentations
  - ◆ Localization

## Quiz 3: Manipulators



3

- ◆ Which of the following statements is true of a manipulator?
  - ◆ Synonymous with robot arm.
  - ◆ Has *grippers* to grasp or move things.
  - ◆ Has six degrees of freedom.
  - ◆ Can interact with the world (exteroceptive) or remain passive in the world (proprioceptive).
  - ◆ *Can* mark all false
    - ◆ Since many people didn't, ungraded question
- ◆ An open-chain manipulator is modeled as a series of rigid links connected by joints, starting at the base.

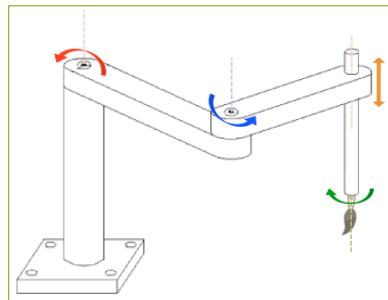


## Quiz 3: Manipulators



4

- ◆ Where is first joint?
- ◆ How many degrees of freedom?
- ◆ Is this manipulator's motion
  - ◆ Revolute
  - ◆ Prismatic
  - ◆ Both
- ◆ Can paintbrush take any position or orientation in workspace?
- ◆ Paintbrush is: end effector



## Quiz 3: Manipulators



5

- ◆ Which of these is a *gripper*?
  - ◆ Bending 'fingers' that close around an object.
  - ◆ Sliding surfaces that pinch an object in between them.
  - ◆ A contact switch that clicks closed when pressed against an object.
  - ◆ A vacuum nozzle that seals against the surface of an object.
  - ◆ A nozzle that dispenses glue between two objects, adhering them together.
  - ◆ Needles that pierce a piece of cloth on two sides to lift it.

## Quiz 3: Manipulators



6

- ◆ Which of these is a *gripper*?
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# Quiz 3: Manipulators




7

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  - ◆ A contact switch that clicks closed when pressed against an object.
  - ◆ A vacuum nozzle that seals against an object.
  - ◆ A nozzle that dispenses glue between them together.
  - ◆ Needles that pierce a piece of material.

### Grippers

◆ Four categories of robot grippers:

- ◆ **Impactive grasping**
  - ◆ Jaws or claws which physically grasp by direct impact upon the object
- ◆ **Ingressive**
  - ◆ Pins, needles or needles penetrate surface
    - ◆ Textile, carbon and fiberglass handling
- ◆ **Astrictive**
  - ◆ Suction forces applied to surface
  - ◆ Vacuum, magneto- or electroadhesion
- ◆ **Kontugutive / Contigutive**
  - ◆ Requiring direct contact for adhesion
  - ◆ Glue, surface tension or freezing



Montano, Hesse, Stammann, Schenk. Robot Grippers -2007  
[www.nationalinstruments.com/news/2007/05/09/2007-robot-hand-picture.html](http://www.nationalinstruments.com/news/2007/05/09/2007-robot-hand-picture.html)

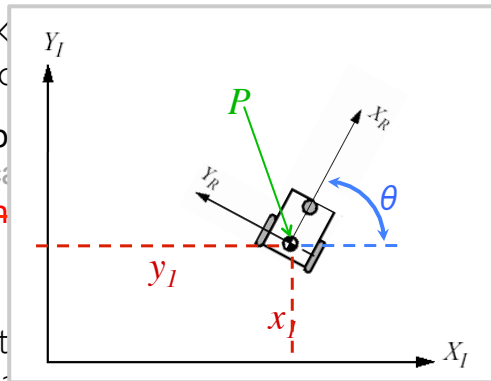
# Quiz 3: Kinematics



8

- ◆ Solving kinematics and IK for a mobile robot in two frames of reference, one global and one local.
 

Global	Rob
Initial	Local
Cartesian	Joint
Plane	
World	
- ◆ How many parameters to describe the pose of a mobile robot, and what are they?
  - ◆ If you put {x,y,z}, r/p/y, since I didn't specify wheeled, okay



$$\xi_I = \begin{bmatrix} x \\ y \\ \theta \end{bmatrix}$$

## Quiz 3: Kinematics



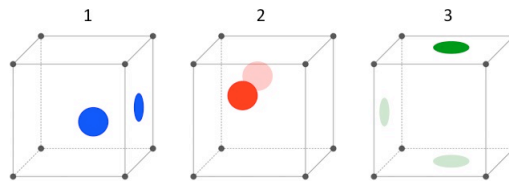
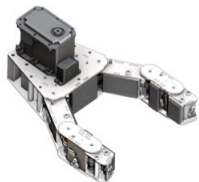
9

- ◆ Forward or Inverse?
  - ◆ We know where everything in the room is from a ceiling cam
  - ◆ Robot needs charging
  - ◆ Trying to decide what commands to send its actuators
  - ◆ What kind of kinematics problem do we need to solve?
- ◆ Kinematic models of wheels
  - ◆ Rolling: all motion accompanied by wheel spin
    - ◆ No skidding front to back
  - ◆ Sliding: wheel can move only in its plane of rotation
    - ◆ No skidding side to side
  - ◆ Single point of contact

## Quiz 3: Grasping



10



- ◆ Which grasp is best? Why?
  - ◆ Note: *grasps* are independent of *pickup action*
- ◆ Grading
  - ◆ Correct cube *–or–* something about using the back of the hand
  - ◆ Otherwise, only -1 if something reasonable

# Assignment 3



11

- ◆ Recommendation: read the assignment
  - ◆ Build LED circuit
    - ◆ Breadboard-based circuit building
    - ◆ Everyone/each pair should have 2 AA batteries
  - ◆ Build motor
    - ◆ Very simple conceptually
  - ◆ Writeup
    - ◆ Circuit diagram, explanations of current, efficiency of motor
    - ◆ 1-1.5 pages
  - ◆ In-class workshop
    - ◆ 12<sup>th</sup> November: demonstrate stuff working, seek help
  - ◆ Then: projects time

**Why do I have 2 LEDs?**  
(use provided parts ≠ use ALL provided parts)

**Resistors**

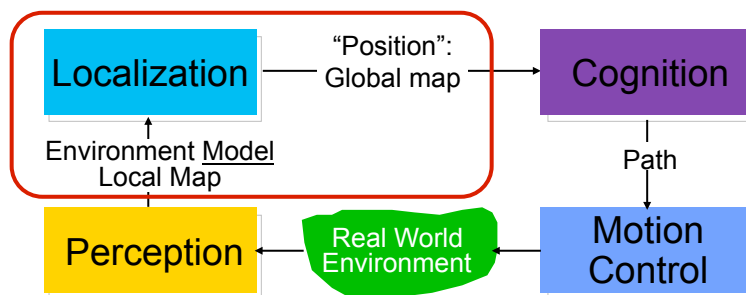
**How can I make a switch?**  
(it will have moving parts!)

# Localization



12

- ◆ Where am I (in a model of the environment)?

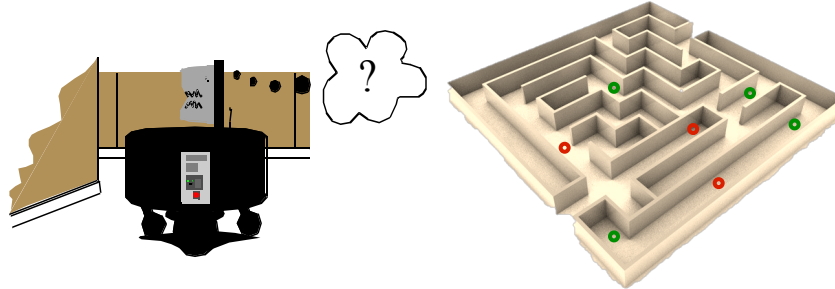


## Sensor Aliasing



13

- ◆ Robots: non-uniqueness of sensors readings is the norm
- ◆ Many-to-one mapping from environmental states to robot's perceptual inputs



- ◆ Not NO information

## Odometry & Dead Reckoning



14

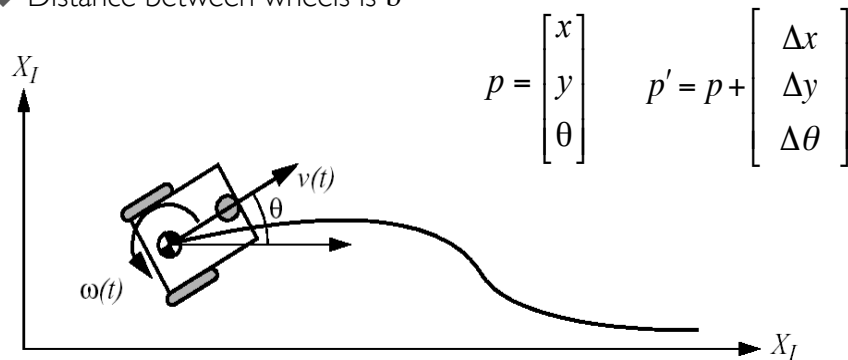
- ◆ Position update is based on proprioceptive sensors
  - ◆ Odometry: uses ...
  - ◆ Dead reckoning: uses ...
- ◆ How?
  - ◆ Sense movement
  - ◆ Integrate that into map model to get the position
- ◆ Extra sensors **reduce** accumulated errors
  - ◆ Same problem
- ◆ Effectors introduce uncertainty about future state

# Odometry & Diff. Drive



15

- ◆ Given a discrete sampling rate  $\Delta t$
- ◆ And motion  $\Delta s_r, \Delta s_l =$  right wheel, left wheel distance travelled
- ◆ Changes in pose are  $\Delta x, \Delta y, \Delta \theta$
- ◆ Distance between wheels is  $b$



# Odometry & Diff. Drive



16

- ◆ Kinematics

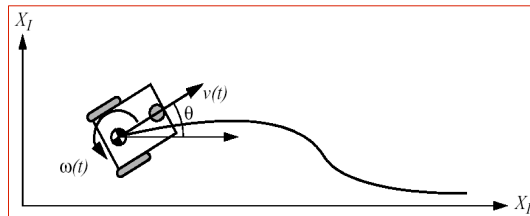
$$\Delta x = \Delta s \cos(\theta + \Delta \theta / 2)$$

$$\Delta y = \Delta s \sin(\theta + \Delta \theta / 2)$$

$$\Delta \theta = \frac{\Delta s_r - \Delta s_l}{b}$$

$$\Delta s = \frac{\Delta s_r + \Delta s_l}{2}$$

$$p' = f(x, y, \theta, \Delta s_r, \Delta s_l) = \begin{bmatrix} x \\ y \\ \theta \end{bmatrix} + \begin{bmatrix} \frac{\Delta s_r + \Delta s_l}{2} \cos\left(\theta + \frac{\Delta s_r - \Delta s_l}{2b}\right) \\ \frac{\Delta s_r + \Delta s_l}{2} \sin\left(\theta + \frac{\Delta s_r - \Delta s_l}{2b}\right) \\ \frac{\Delta s_r - \Delta s_l}{b} \end{bmatrix}$$





# Odometry & Diff. Drive



17

- ◆ Error model – represent uncertainty of location over time in covariance matrix
- ◆  $\Sigma_p$  is initial matrix
- ◆ Errors of 2 wheels independent
- ◆ Variance of error  $\propto \Delta s_r, \Delta s_l$

$$\Sigma_{\Delta} = \text{covar}(\Delta s_r, \Delta s_l) = \begin{bmatrix} k_r |\Delta s_r| & 0 \\ 0 & k_l |\Delta s_l| \end{bmatrix}$$

$$\Sigma_{p'} = \nabla_p f \cdot \Sigma_p \cdot \nabla_p f^T + \nabla_{\Delta_r l} f \cdot \Sigma_{\Delta} \cdot \nabla_{\Delta_r l} f^T$$

$$F_p = \nabla_p f = \nabla_p (f^T) = \begin{bmatrix} \frac{\partial f}{\partial x} & \frac{\partial f}{\partial y} & \frac{\partial f}{\partial \theta} \end{bmatrix} = \begin{bmatrix} 1 & 0 & -\Delta s \sin(\theta + \Delta\theta/2) \\ 0 & 1 & \Delta s \cos(\theta + \Delta\theta/2) \\ 0 & 0 & 1 \end{bmatrix}$$

$$F_{\Delta_r l} = \begin{bmatrix} \frac{1}{2} \cos\left(\theta + \frac{\Delta\theta}{2}\right) - \frac{\Delta s}{2b} \sin\left(\theta + \frac{\Delta\theta}{2}\right) & \frac{1}{2} \cos\left(\theta + \frac{\Delta\theta}{2}\right) + \frac{\Delta s}{2b} \sin\left(\theta + \frac{\Delta\theta}{2}\right) \\ \frac{1}{2} \sin\left(\theta + \frac{\Delta\theta}{2}\right) + \frac{\Delta s}{2b} \cos\left(\theta + \frac{\Delta\theta}{2}\right) & \frac{1}{2} \sin\left(\theta + \frac{\Delta\theta}{2}\right) - \frac{\Delta s}{2b} \cos\left(\theta + \frac{\Delta\theta}{2}\right) \\ & \frac{1}{b} & & -\frac{1}{b} \end{bmatrix}$$

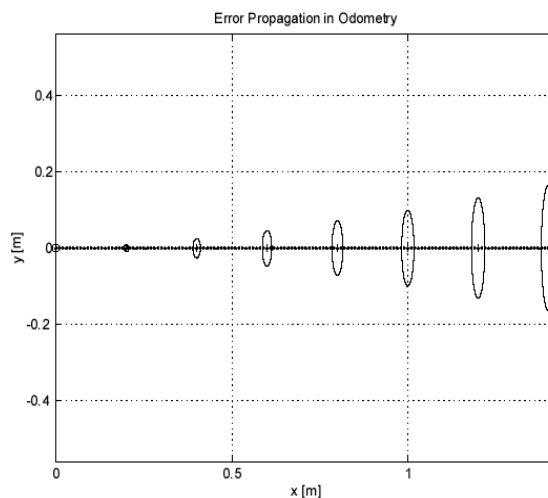
# Odometry:

## Growth of Pose Uncertainty for Straight Line Movement



18

- ◆ Note: Errors perpendicular to the direction of movement are growing much faster!



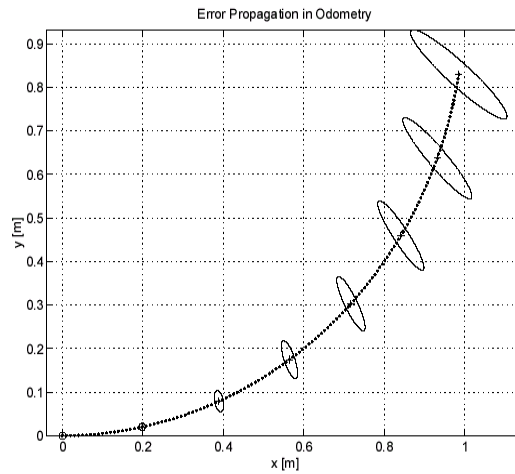
# Odometry:

Growth of Pose uncertainty for Movement on a Circle



19

- ◆ Note: Errors ellipse in does not remain perpendicular to the direction of movement!

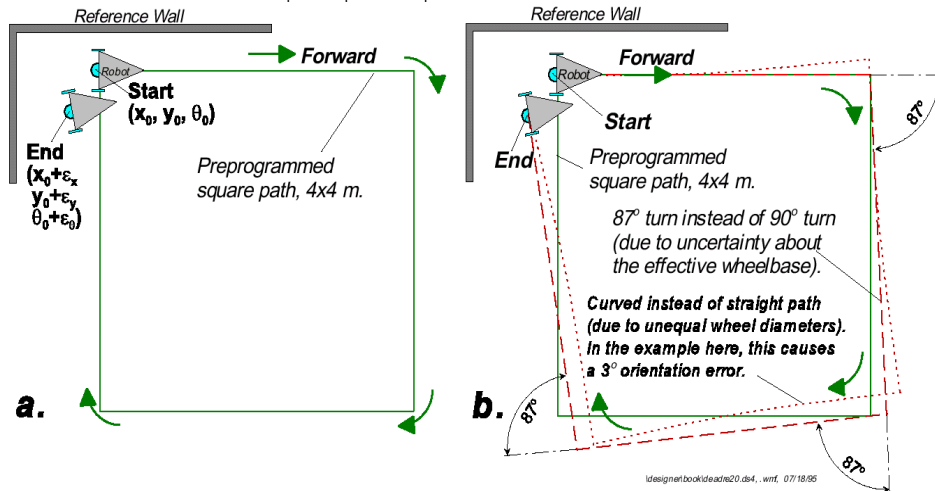


# Calibration of Errors



20

- ◆ The unidirectional square path experiment

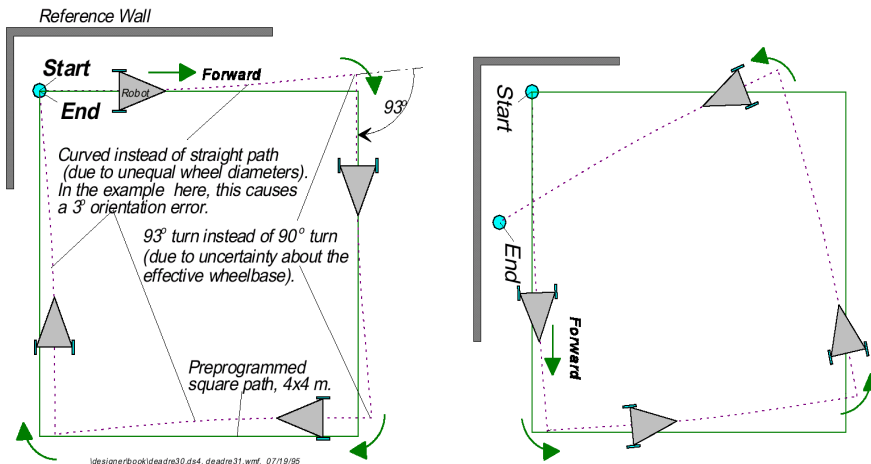


# Calibration of Errors



21

- ◆ The bi-directional square path experiment

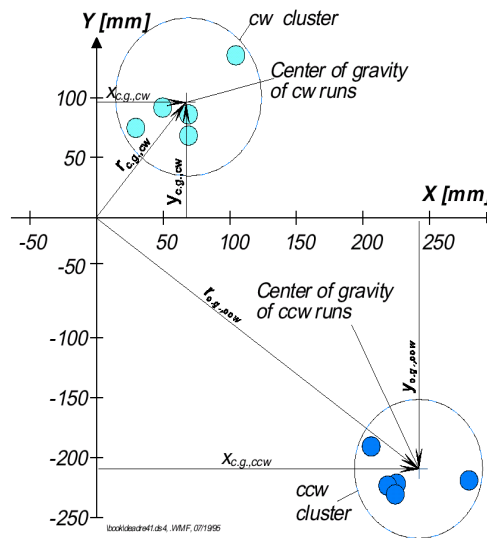


# Calibration of Errors



22

- ◆ The deterministic and non-deterministic errors

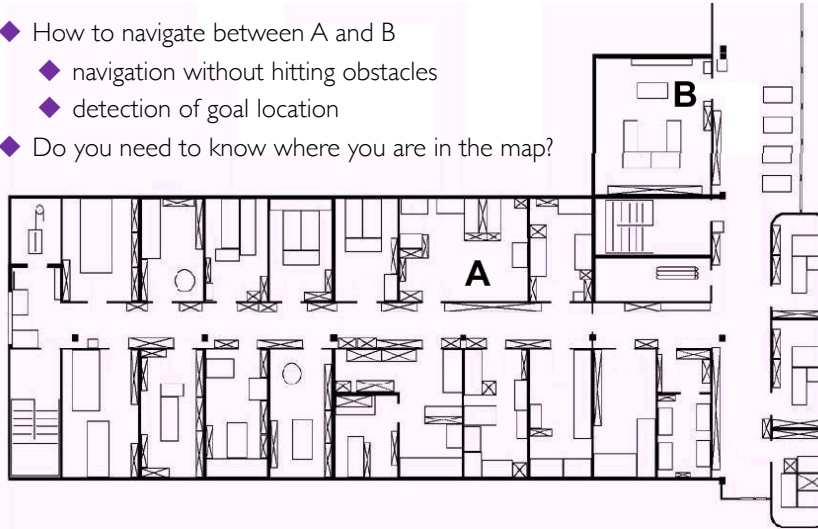


## Localize, Or Not?



23

- ◆ How to navigate between A and B
  - ◆ navigation without hitting obstacles
  - ◆ detection of goal location
- ◆ Do you need to know where you are in the map?

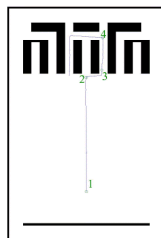


## Behavior Based Navigation



24

- ◆ Fast to implement
- ◆ Effective in unchanging environment
- ◆ Does not scale to new environments
- ◆ Behaviors must be designed and debugged
- ◆ Sensor changes change behavior
- ◆ Harder to represent to users



Path of the robot

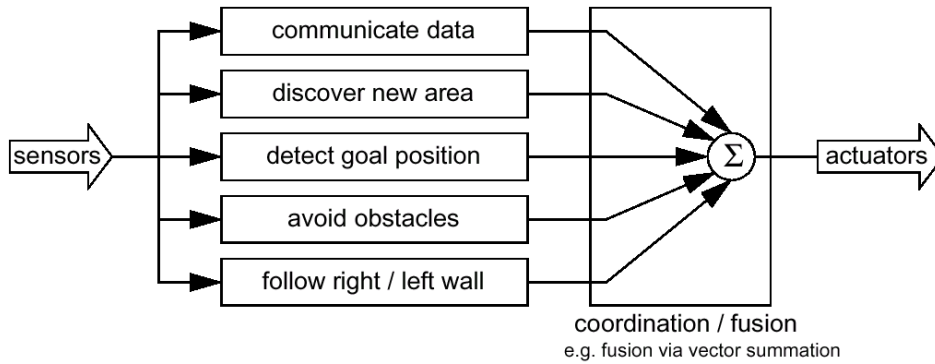


Belief states at positions 2, 3 and 4

# Behavior Based Navigation



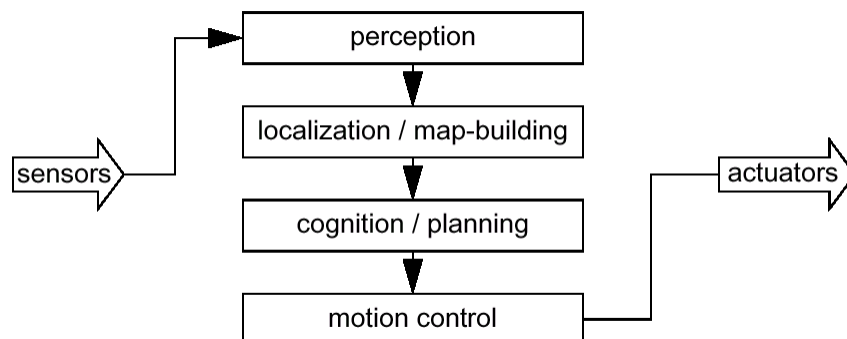
25



# Model Based Navigation



26



# Belief Representation



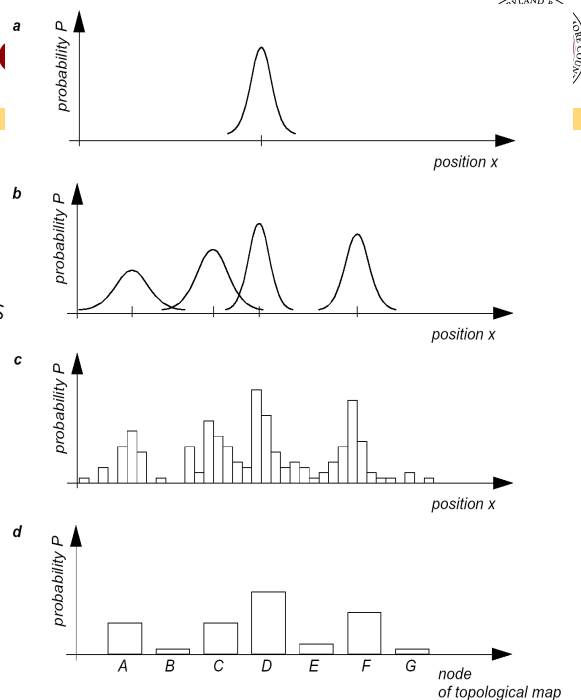
27

- ◆ a) Continuous map with *single hypothesis*
- ◆ b) Continuous map with *multiple hypothesis*
- ◆ d) Discretized map with probability distribution
- ◆ d) Discretized topological map with probability distribution

# Belief Representation

28

- ◆ a) Continuous map with *single hypothesis*
- ◆ b) Continuous map with *multiple hypothesis*
- ◆ d) Discretized map with probability distribution
- ◆ d) Discretized topological map with probability distribution



# Characteristics



29

## Belief Representation can be...

- ◆ Continuous
  - ◆ Precision bound by sensor data
  - ◆ Typically single hypothesis pose estimate
  - ◆ Lost when diverging (for single hypothesis)
  - ◆ Compact representation and typically reasonable in processing power.
- ◆ Discrete
  - ◆ Precision bound by resolution of discretisation
  - ◆ Typically multiple hypothesis pose estimate
  - ◆ Never lost (when diverges converges to another cell)
  - ◆ Important memory and processing power needed. (not the case for topological maps)