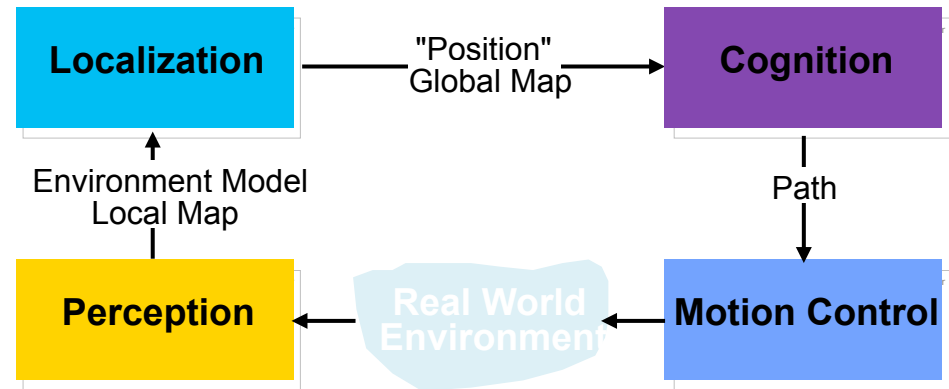
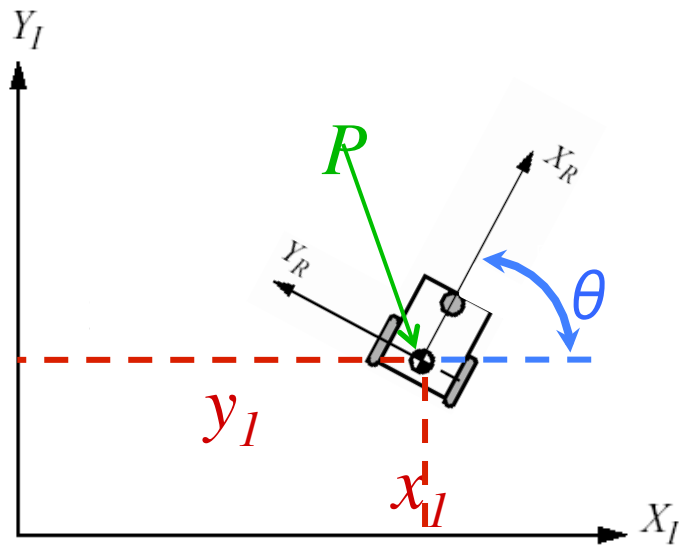


# Kinematics

## *Mobile Kinematics*





# Bookkeeping

2

- ◆ Upcoming
  - ◆ Assignment 2
- ◆ Quiz 2
  - ◆ Curve TBD: probably ~8%
  - ◆ A note on number/length of answers
- ◆ Today
  - ◆ Quiz 2 review
  - ◆ Mobile Robot Kinematics
- ◆ Reading: SNS 3.2 (should now have 3.1-3.3)

# About That Microphone

3

- ◆ 5-hertz sampling rate
- ◆ Sequential notes
  - ◆ Playing one note per second
- ◆ Every time a change is detected:
  - ◆ Output changes color
  - ◆ Vertical bar added
  - ◆ Gray = no tone is detected



*Sensor  
output*

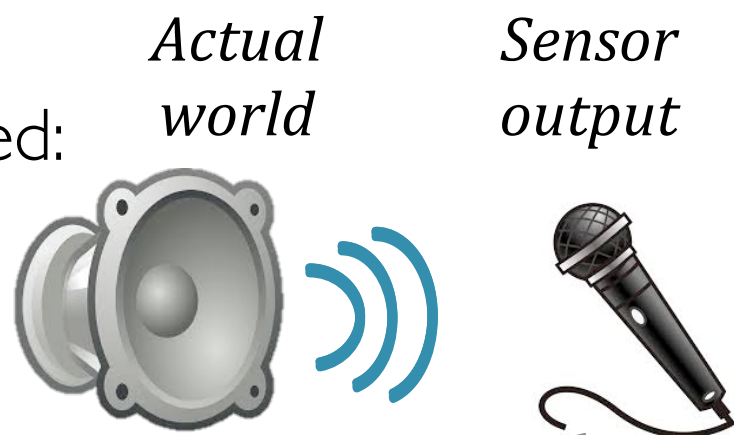




# About That Microphone

4

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# Characterizing Sensors

5

- ◆ Active/Passive
  - ◆ Does it put energy out into the world?
- ◆ Exteroceptive/Proprioceptive
  - ◆ Senses the world around it, vs. sensing internal state
- ◆ Linear/Nonlinear
  - ◆ Does the output function vary with respect to input function?





# Characterizing Sensors

6

- ◆ Active/Passive

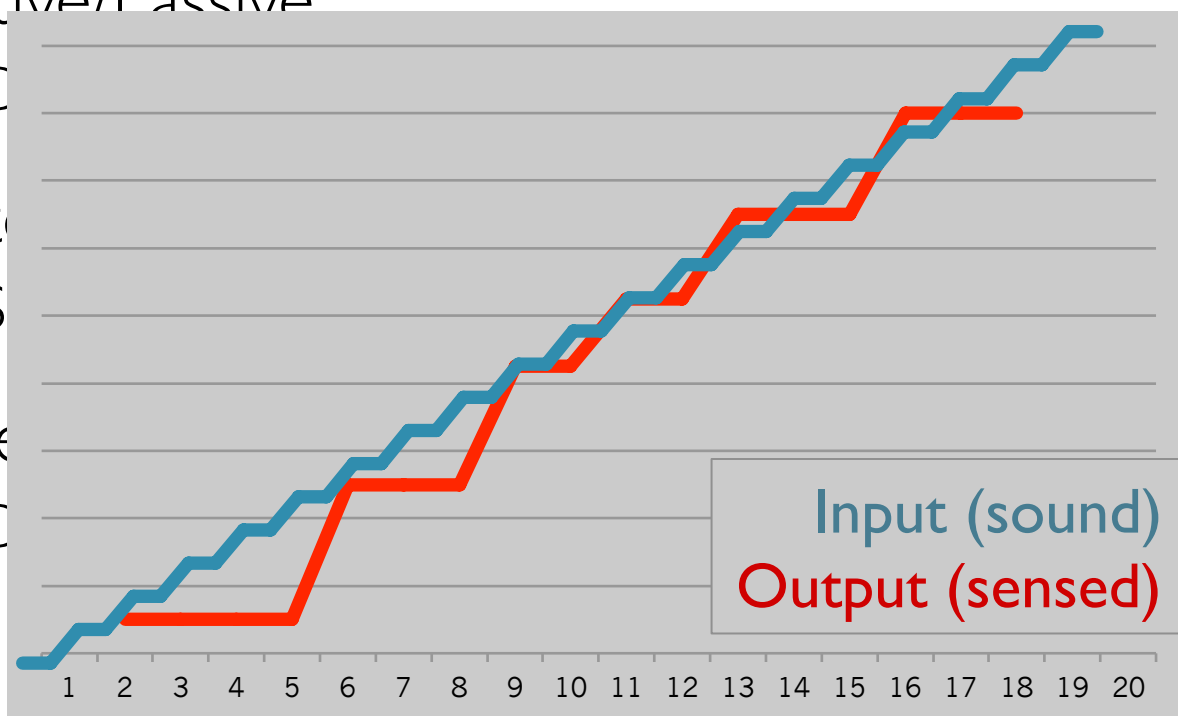
- ◆ D

- ◆ Ext

- ◆ S

- ◆ Line

- ◆ D



ate

input function?

Input (sound)  
Output (sensed)





# Detecting Changes

## 7 Doesn't detect a change every note because...

- ◆ Sampling Rate: how often the sensor can take a reading
  - ◆ Notes are playing 1/second
  - ◆ Sensor is 5 Hz – 5 samples per second
- ◆ Cross-Sensitivity: sensitive to something *other than* target signal
  - ◆ E.g., a mic is supposed to pick up sound but also picks up EM noise
- ◆ Sensitivity: Ratio of output change to input change
  - ◆ How much change in world affects change in sensor readings
  - ◆ E.g., does the reading change every note? Every 1/10<sup>th</sup> note?





# Classification

8 The way this microphone reports output suggests that it is an:

- ◆ Incremental sensors
  - ◆ Reports an incremental change (up/down, warmer/cooler)
- ◆ Absolute sensors
  - ◆ Unambiguously reports its state
- ◆ This mic:
  - ◆ Every time a change is detected, output changes color, vertical bar added

Sidebar: is this how microphones work?







# Range and Resolution

9

- ◆ Range of a sensor:
  - ◆ Upper limit to lower limit
- ◆ Resolution
  - ◆ Minimum measurable difference between any two values





# Representing Uncertainty

10

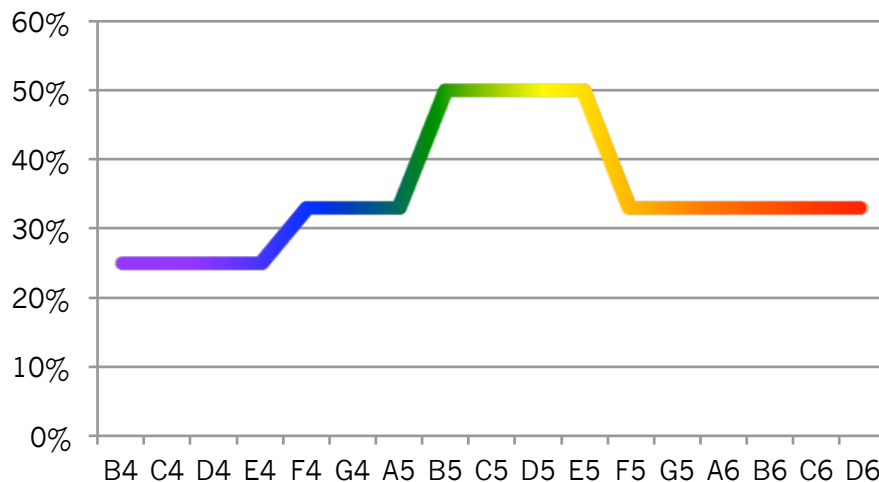
- ◆ “A *probability mass function* gives the **probability** that a discrete random variable is **equal to some value**.”
  - ◆ Given green output, what is the probability the input is B5?
  - ◆ What is the hidden variable we want?
    - ◆ The thing we don't know for certain but are trying to sense.
- ◆ Given some input, what is the probability of the output being a particular note?
- ◆ What does that look like across all notes in the range?





# Representing Uncertainty

◆ Graph: given some input, likelihood of knowing the correct output



- Unimodal?
  - ◆ One hump
- Bimodal?
  - ◆ Two humps
- Zero mean?
  - ◆ Equally likely to be wrong up or down
- Asymmetric?
  - ◆ Same error distribution above and below zero





# Depth / Range Sensing

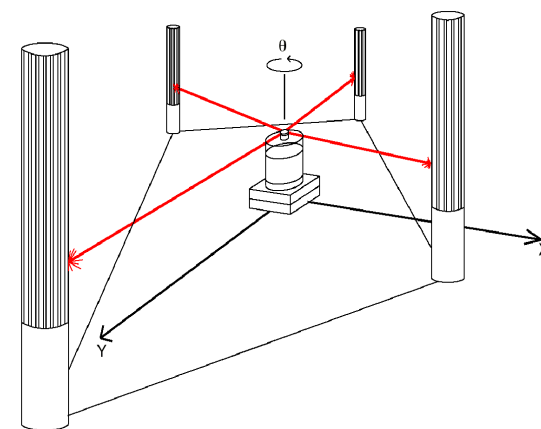
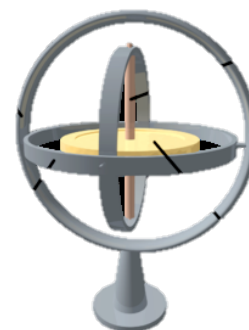
12

- ◆ Structured Light: display a known pattern of light and dark and measure geometric distortion.
  - ◆ Kinect
- ◆ Time-of-flight: emit a wave and measure time for it to reach something and reflect back.
  - ◆ Laser range-finder, Sonar, Kinect 2
- ◆ Stereo: two calibrated cameras see a scene from different angles and calculate depth based on disparities.
  - ◆ Humans, Bumblebee sensor

# Heading Sensor

13

- ◆ Tells you what direction you are pointed
  - ◆ With respect to some frame of reference
  - ◆ Is this **position** or **orientation**?
- ◆ What do the following tell you?
  - ◆ Compass
  - ◆ Gyroscope
  - ◆ Inclinometer
  - ◆ GPS
  - ◆ Location beacons



# Image Processing

14

- ◆ What type of processing has been performed here?
- ◆ We looked at edge detection, corner detection, blob finding





# Types of Errors

15

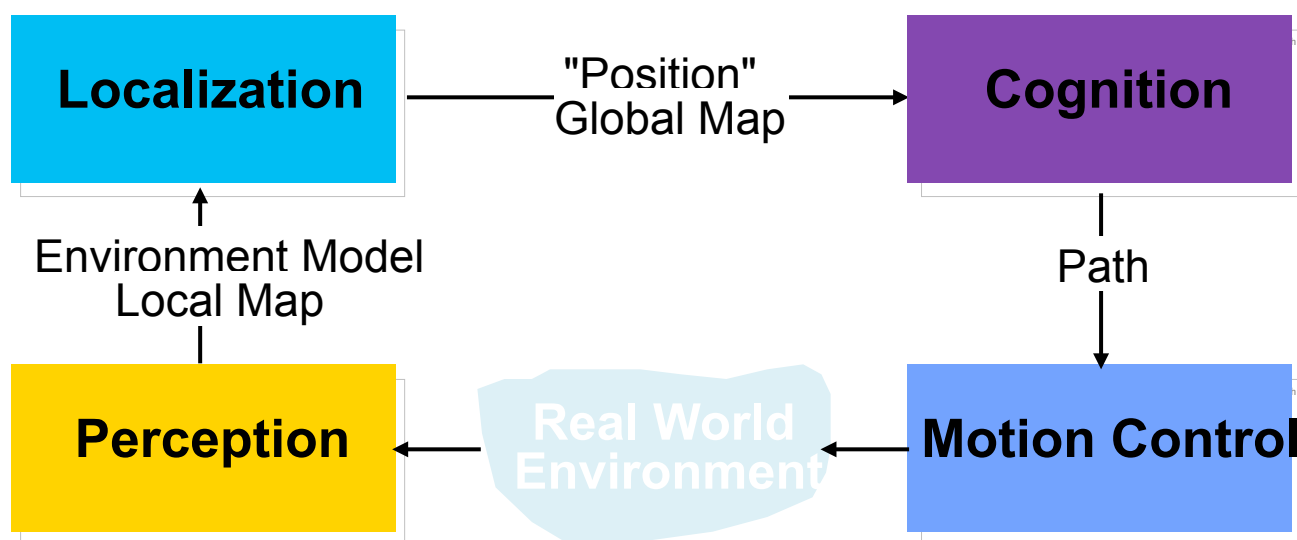
- ◆ Systematic error → deterministic failures
  - ◆ Caused by factors that can (in theory) be modeled
  - ◆ Can be corrected with calibration
- ◆ Random error → non-deterministic failures
  - ◆ No modeling or prediction possible
- ◆ How would you correct for...
  - “Fisheye” distortion on a camera lens.
  - Background noise picked up by a microphone.
  - Thermometer readings that are occasionally too high or too low.
  - A range-finding sensor that reads things as being too close.
  - Sonar distortion in an unfamiliar underwater environment.



# Wheeled Motion Control

16

- ◆ Requirements for Motion Control
  - ◆ Kinematic / dynamic model of the robot
  - ◆ Model of interaction between the wheel and the ground
  - ◆ Definition of required motion → speed & position control
  - ◆ A control law that satisfies the requirements







# Mobile Robot Kinematics

17

- ◆ Aim
  - ◆ Description of mechanical behavior of the robot for:
    - ◆ **Design purposes** – how do we design it to do what we need?
    - ◆ **Control purposes** – how do we then get it to do that?
  - ◆ Mobile robots can move with respect to environment
    - ◆ No direct way to measure the robot's position
    - ◆ Position must be integrated over time
    - ◆ Leads to inaccuracies of the position (motion) estimate
  - ◆ Understanding mobile robot motion starts with understanding **constraints** on the robot's mobility

# Mobile Position & Orientation

18

Frames of reference:

$\{X_I, Y_I\}$ : Global

$\{X_R, Y_R\}$ : Robot

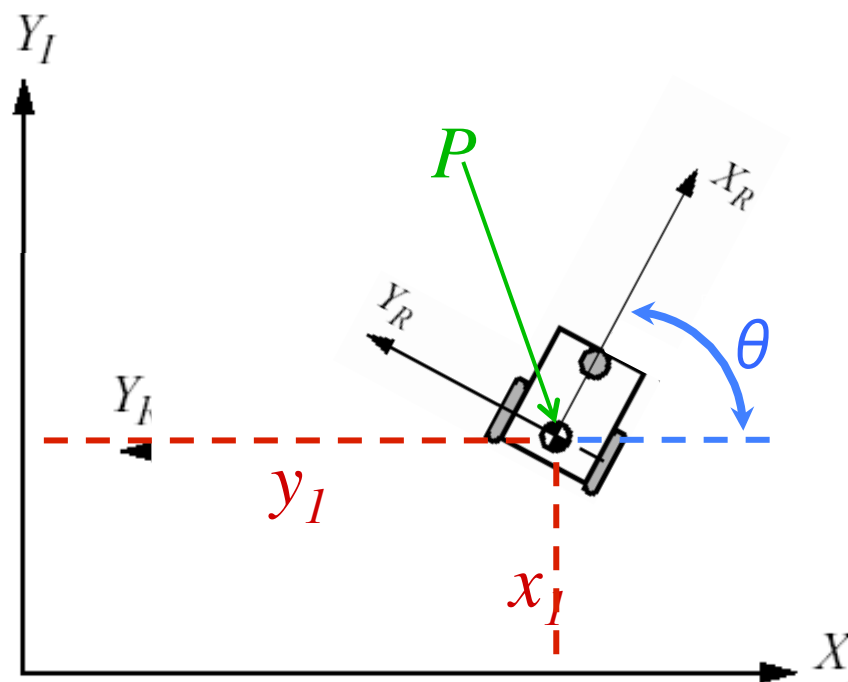
Robot: point  $P$

Position (of  $P$ ):

$\{x_{I,1}, y_{I,1}\}$

Heading:

$\{\theta\}$ : I  $\angle$  R



$$\xi_I = \begin{bmatrix} x \\ y \\ \theta \end{bmatrix}$$