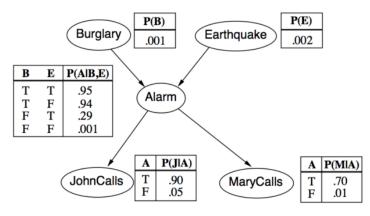
CMSC 678 Machine Learning - Fall 2024 Homework Assignment 6 Due 11:59PM on December 2nd

Consider the Bayesian Network below whose variables are Boolean and can take on values T and F:



- Write down an expression for $p(B, \overline{E}, A, J, \overline{M})$ using the conditional independencies implied by the structure of the Bayes net.
- Compute the value of that expression as a number. Show your work.
- Compute the value of p(E|J, M) by hand. Show all of your work.
- Write a function to sample values from the joint distribution defined by this network. Use that function to sample instances and use those samples to estimate p(E, J, M) and p(J, M). Use those estimates to estimate p(E|J, M). Turn in your code and show the counts that you used to estimate the probabilities and the probabilities themselves. How many samples do you need to draw to get a good estimate of p(E|J, M)? Why does it take such a large number of samples? (For what it's worth, I wrote a 28 line python solution to this question.)