

Knowledge Representation and Reasoning

Chapter 12

Some material adopted from notes by
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Overview

- Approaches to knowledge representation
- Deductive/logical methods
 - Forward-chaining production rule systems
 - Semantic networks
 - Frame-based systems
 - Description logics
- Abductive/uncertain methods
 - What's abduction?
 - Why do we need uncertainty?
 - Bayesian reasoning
 - Other methods: Default reasoning, rule-based methods, Dempster-Shafer theory, fuzzy reasoning

Introduction

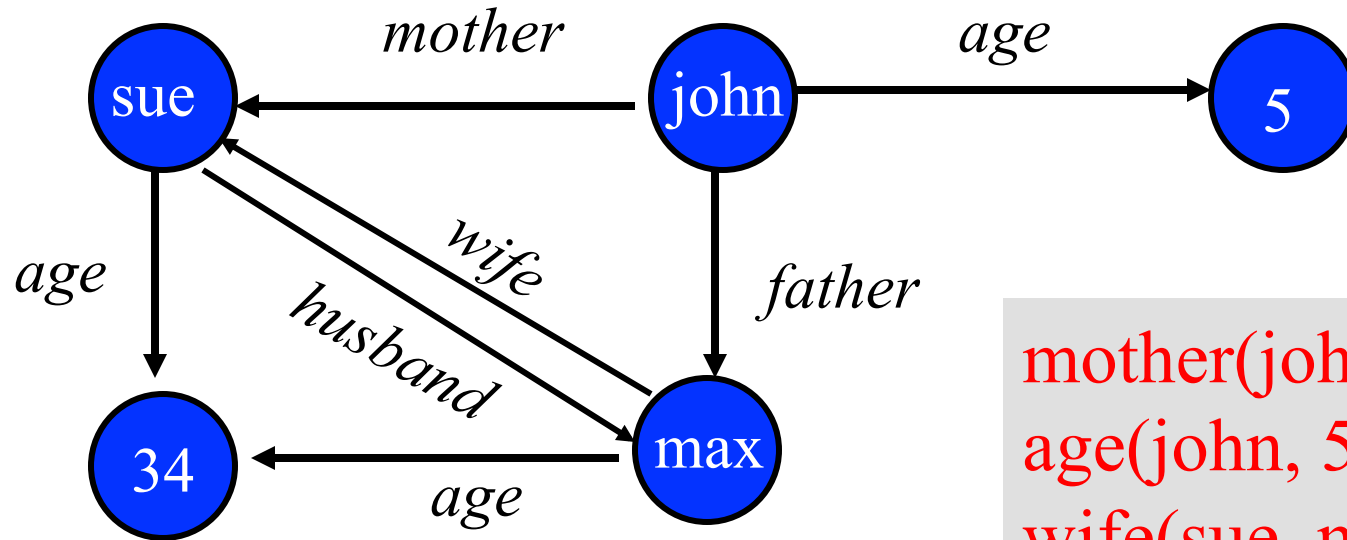
- Real knowledge representation and reasoning systems come in several major varieties
- These differ in their intended use, expressivity, features,...
- Some major families are
 - Logic programming languages
 - Theorem provers
 - Rule-based or production systems
 - Semantic networks
 - Frame-based representation languages
 - Databases (deductive, relational, object-oriented, etc.)
 - Constraint reasoning systems
 - Description logics
 - Bayesian networks
 - Evidential reasoning

Semantic Networks

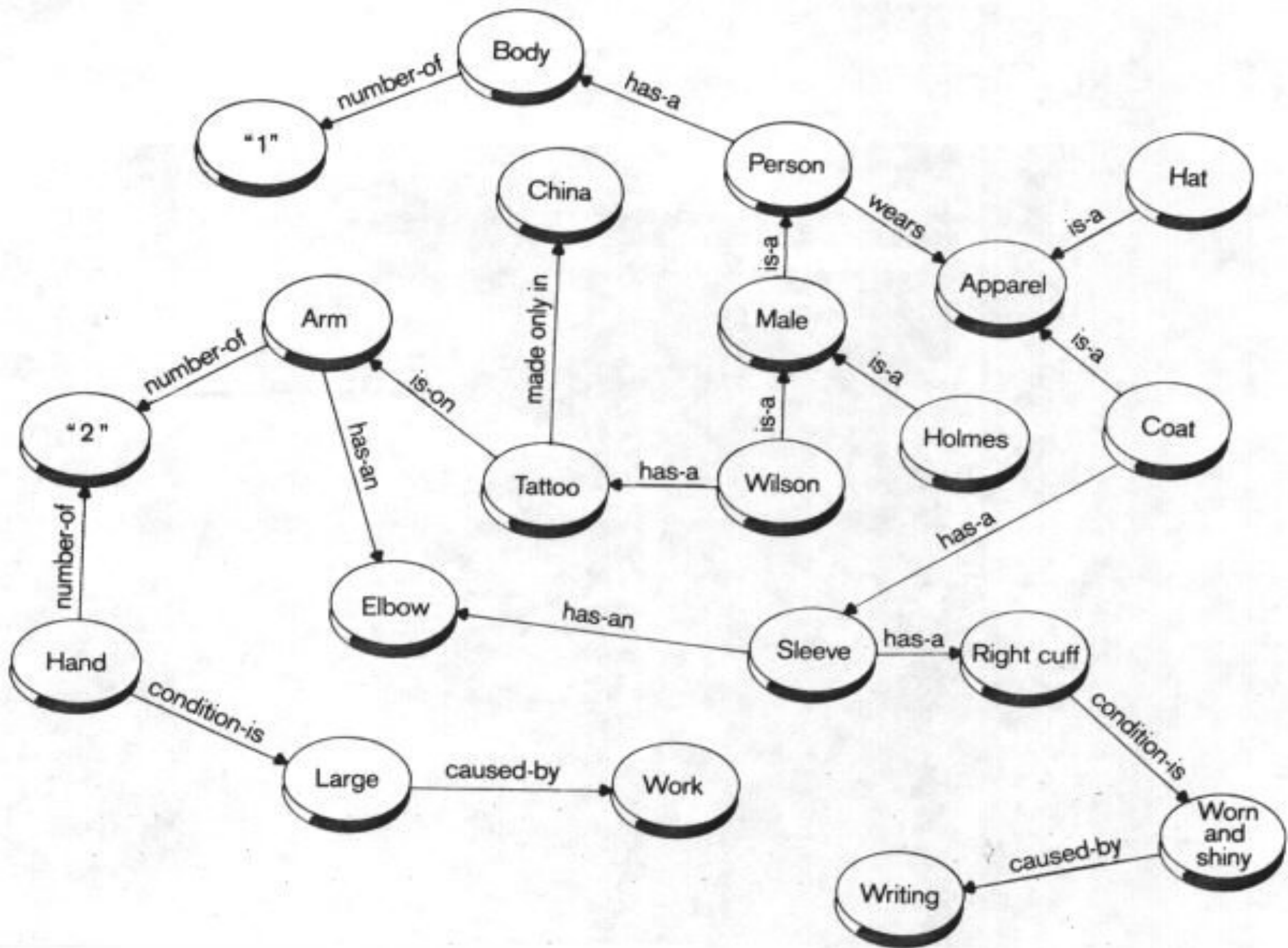
- A semantic network is a simple representation scheme that uses a graph of labeled nodes and labeled, directed arcs to encode knowledge.
 - Usually used to represent static, taxonomic, concept dictionaries
- Semantic networks are typically used with a special set of accessing procedures that perform “reasoning”
 - e.g., inheritance of values and relationships
- Semantic networks were very popular in the ‘60s and ‘70s but less used in the ‘80s and ‘90s. Back in the ‘00s as RDF
 - Much less expressive than other KR formalisms: both a feature and a bug!
- The **graphical depiction** associated with a semantic network is a significant reason for their popularity.

Nodes and Arcs

Arcs define binary relationships that hold between objects denoted by the nodes

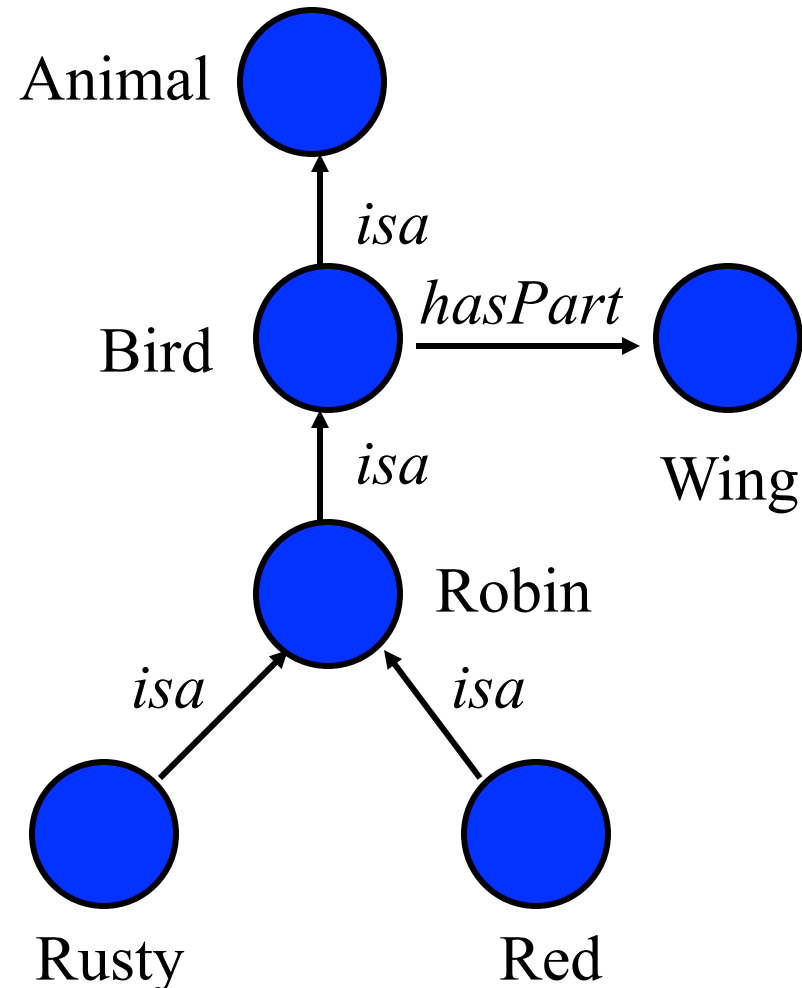


```
mother(john, sue)
age(john, 5)
wife(sue, max)
age(max, 34)
...
```



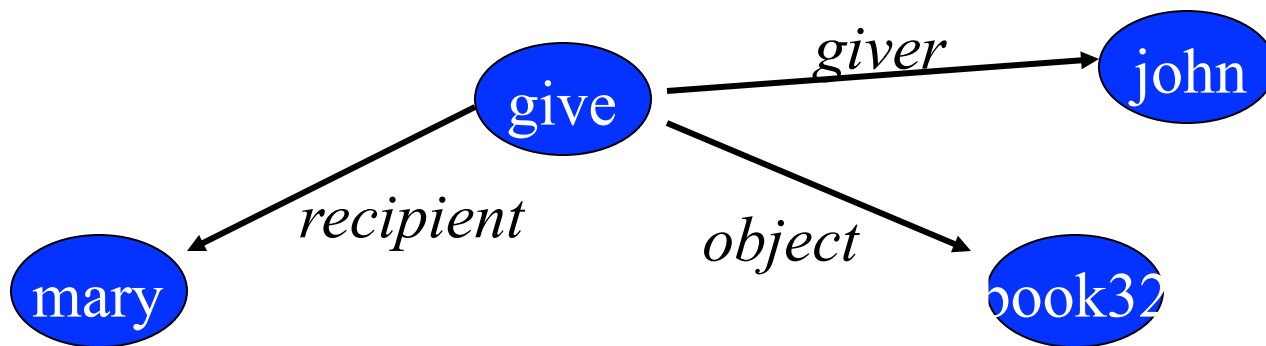
Semantic Networks

- The ISA (is-a) or AKO (a-kind-of) relation is often used to link instances to classes, classes to superclasses
- Some links (e.g. hasPart) are inherited along ISA paths.
- The *semantics* of a semantic net can be relatively informal or very formal
 - often defined at the implementation level



Reification

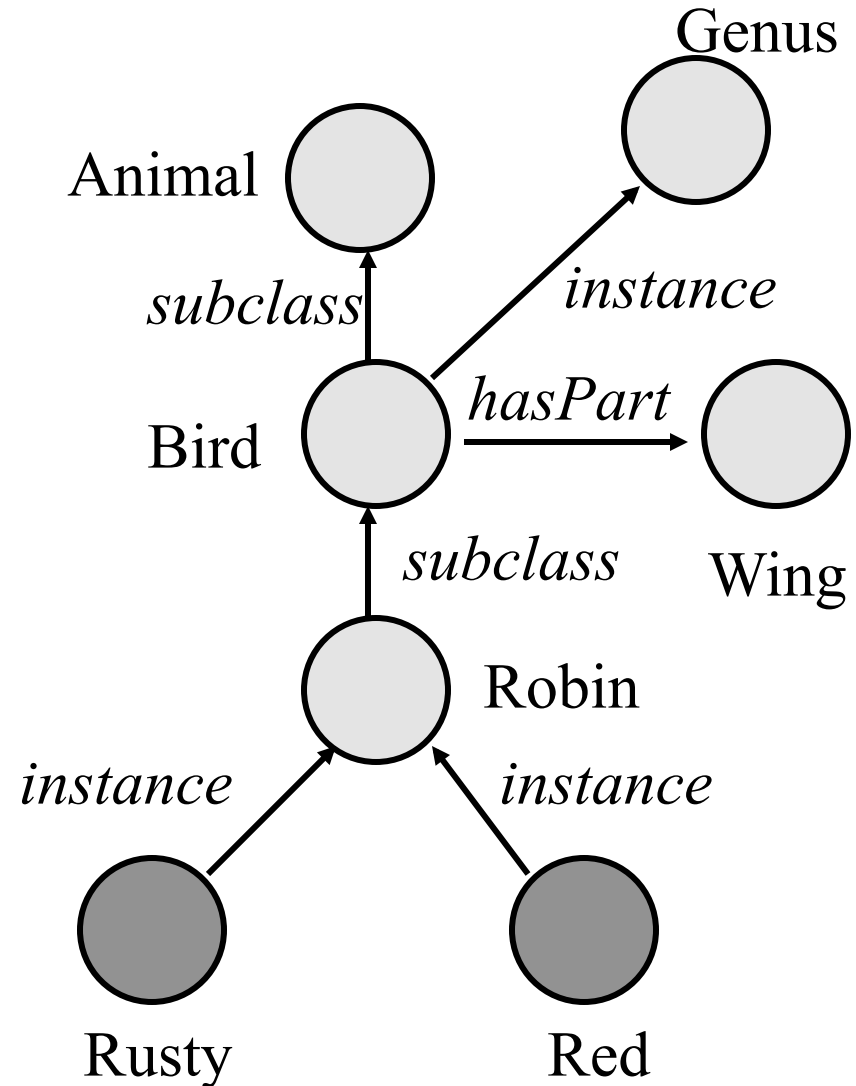
- Non-binary relationships can be represented by “turning the relationship into an object”
- This is an example of what logicians call “reification”
 - reify v : consider an abstract concept to be real
- We might want to represent the generic give event as a relation involving three things: a giver, a recipient and an object, `give(john,mary,book32)`



Individuals and Classes

Many semantic networks distinguish

- nodes representing individuals and those representing classes
- the “subclass” relation from the “instance-of” relation



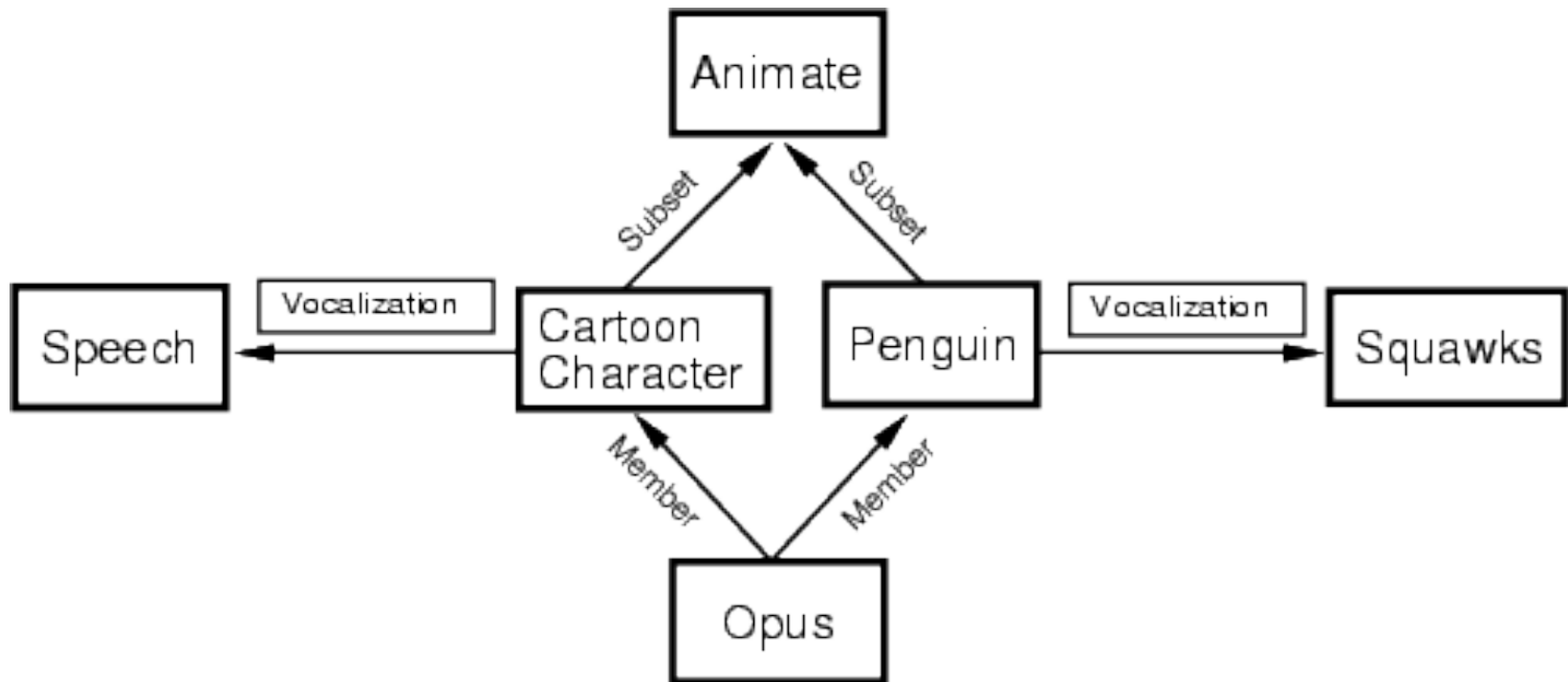
Link types

Link Type	Semantics	Example
$A \xrightarrow{\text{Subset}} B$	$A \subset B$	$Cats \subset Mammals$
$A \xrightarrow{\text{Member}} B$	$A \in B$	$Bill \in Cats$
$A \xrightarrow{R} B$	$R(A, B)$	$Bill \xrightarrow{Age} 12$
$A \xrightarrow{\boxed{R}} B$	$\forall x \ x \in A \Rightarrow R(x, B)$	$Birds \xrightarrow{\boxed{Legs}} 2$
$A \xrightarrow{\boxed{\boxed{R}}} B$	$\forall x \ \exists y \ x \in A \Rightarrow y \in B \wedge R(x, y)$	$Birds \xrightarrow{\boxed{\boxed{Parent}}} Birds$

Inference by Inheritance

- One of the main kinds of reasoning done in a semantic net is the inheritance of values along subclass and instance links
- Semantic networks differ in how they handle the case of inheriting multiple different values.
 - All possible values are inherited, *or*
 - Only the “closest” value or values are inherited

Conflicting inherited values

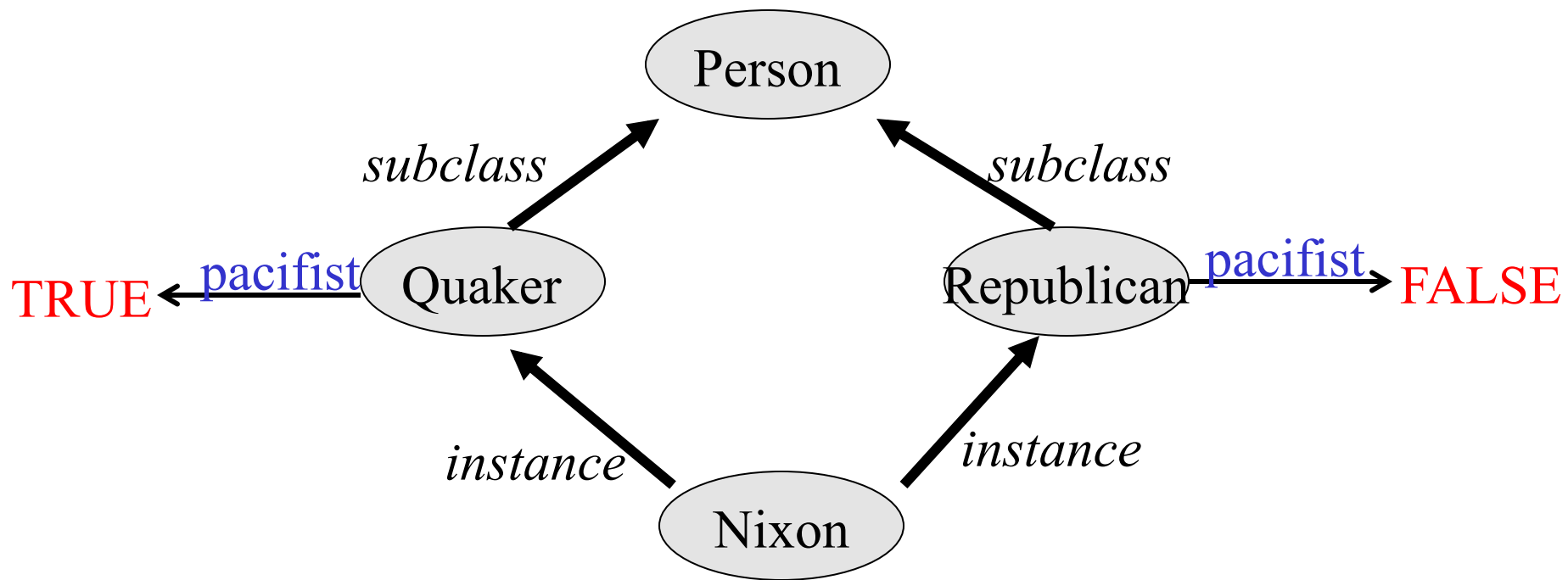


Multiple inheritance

- A node can have any number of super-classes that contain it, enabling a node to inherit properties from multiple parent nodes and their ancestors in the network
- These rules are often used to determine inheritance in such “tangled” networks where multiple inheritance is allowed:
 - If $X < A < B$ and both A and B have property P, then X inherits A’s property.
 - If $X < A$ and $X < B$ but neither $A < B$ nor $B < A$, and A and B have property P with different and inconsistent values, then X does not inherit property P at all.

Nixon Diamond

- This was a classic example circa 1980

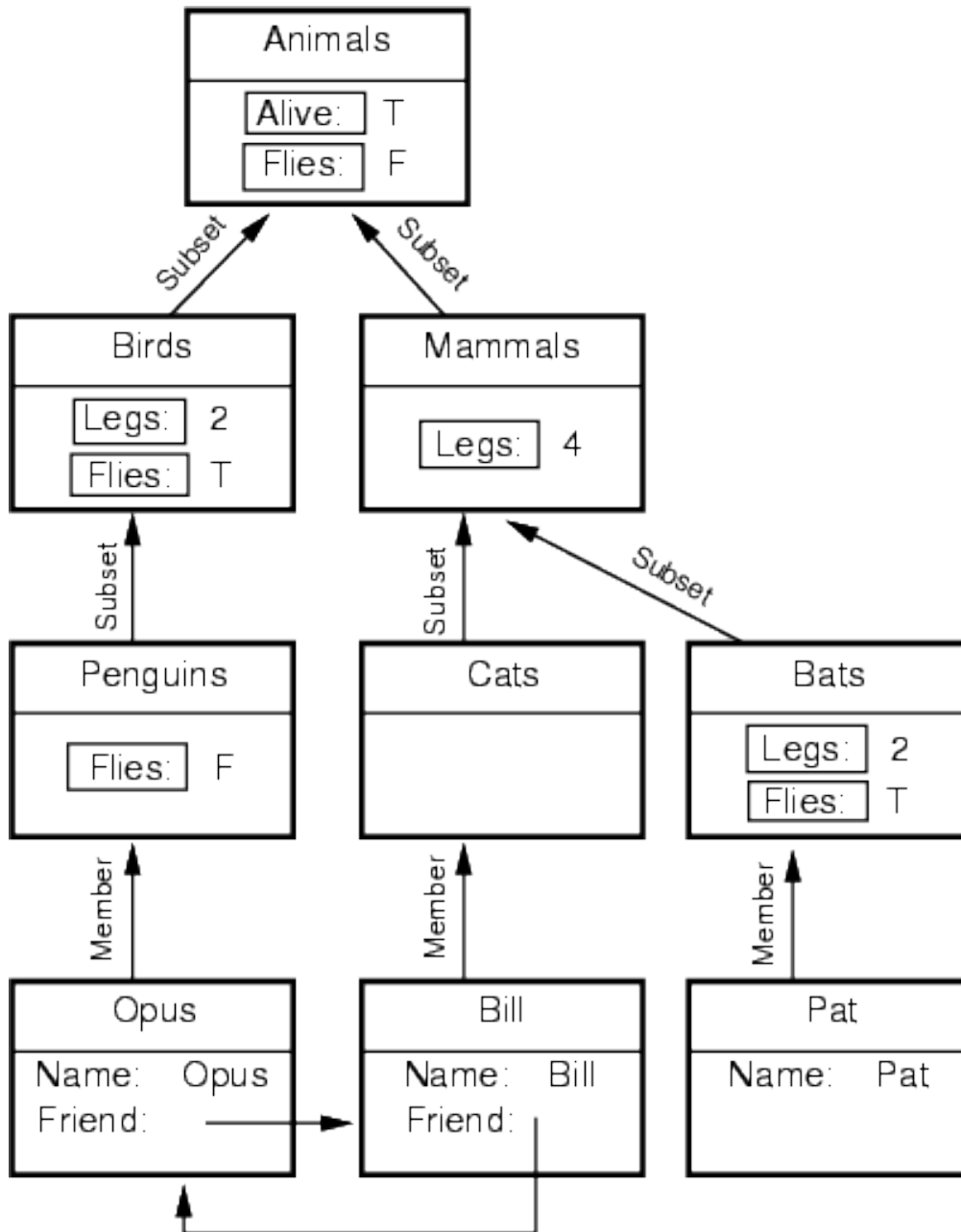


From Semantic Nets to Frames

- Semantic networks morphed into Frame Representation Languages in the 70s and 80s
- A frame is a lot like the notion of an object in OOP, but has more meta-data
- A **frame** has a set of **slots**
- A **slot** represents a relation to another frame or to a literal value value (e.g., a number or string)
- A slot has one or more **facets**
- A **facet** represents some aspect of the relation

Facets

- A slot in a frame can hold more than a value
- Other facets might include:
 - **Value:** current fillers
 - **Default:** default fillers
 - **Cardinality:** minimum and maximum number of fillers
 - **Type:** type restriction on fillers (usually expressed as another frame object)
 - **Procedures:** attached procedures (if-needed, if-added, if-removed)
 - **Salience:** measure on the slot's importance
 - **Constraints:** attached constraints or axioms
- In some systems, the slots themselves are instances of frames.



(a) A frame-based knowledge base

$\text{Rel}(\text{Alive}, \text{Animals}, \text{T})$

$\text{Rel}(\text{Flies}, \text{Animals}, \text{F})$

$\text{Birds} \subset \text{Animals}$

$\text{Mammals} \subset \text{Animals}$

$\text{Rel}(\text{Flies}, \text{Birds}, \text{T})$

$\text{Rel}(\text{Legs}, \text{Birds}, 2)$

$\text{Rel}(\text{Legs}, \text{Mammals}, 4)$

$\text{Penguins} \subset \text{Birds}$

$\text{Cats} \subset \text{Mammals}$

$\text{Bats} \subset \text{Mammals}$

$\text{Rel}(\text{Flies}, \text{Penguins}, \text{F})$

$\text{Rel}(\text{Legs}, \text{Bats}, 2)$

$\text{Rel}(\text{Flies}, \text{Bats}, \text{T})$

$\text{Opus} \in \text{Penguins}$

$\text{Bill} \in \text{Cats}$

$\text{Pat} \in \text{Bats}$

$\text{Name}(\text{Opus}, \text{"Opus"})$

$\text{Name}(\text{Bill}, \text{"Bill"})$

$\text{Friend}(\text{Opus}, \text{Bill})$

$\text{Friend}(\text{Bill}, \text{Opus})$

$\text{Name}(\text{Pat}, \text{"Pat"})$

(b) Translation into first-order logic

Description Logics

- Description logics are a family of frame-like KR systems with a formal semantics.
 - E.g., KL-ONE, OWL
- An additional kind of inference done by these systems is automatic **classification**
 - finding the right place in a hierarchy of objects for a new description
- Current systems keep the languages simple, so that all inference can be done in polynomial time (in the number of objects), ensuring tractability of inference
- The Semantic Web language OWL is based on description logic

Abduction

- **Abduction** is a reasoning process that tries to form plausible explanations for observations
 - Distinctly different from deduction and induction
 - Inherently unsound and uncertain
- Uncertainty is an important issue in abductive reasoning
- Some major formalisms for representing and reasoning about uncertainty
 - Mycin's certainty factors (an early representative)
 - **Probability theory (esp. Bayesian belief networks)**
 - Dempster-Shafer theory
 - Fuzzy logic
 - Truth maintenance systems
 - Nonmonotonic reasoning

Abductive reasoning

- **Definition** (Encyclopedia Britannica): reasoning that derives an explanatory hypothesis from a given set of facts
 - The inference result is a **hypothesis** that, if true, could **explain** the occurrence of the given facts
- Example: Dendral, an expert system to construct 3D structure of chemical compounds
 - Fact: mass spectrometer data of the compound and its chemical formula
 - KB: chemistry, esp. strength of different types of bonds
 - Reasoning: form a hypothetical 3D structure that satisfies the chemical formula, and that would most likely produce the given mass spectrum

Abduction examples (cont.)

- Example: Medical diagnosis
 - Facts: symptoms, lab test results, and other observed findings (called manifestations)
 - KB: causal associations between diseases and manifestations
 - Reasoning: one or more diseases whose presence would causally explain the occurrence of the given manifestations
- Many other reasoning processes (e.g., word sense disambiguation in natural language process, image understanding, criminal investigation) can also be seen as abductive reasoning

abduction, deduction and induction

Deduction: major premise: All balls in the box are black
minor premise: These balls are from the box
conclusion: These balls are black

$A \Rightarrow B$
A

B

Abduction: rule: All balls in the box are black
observation: These balls are black
explanation: These balls are from the box

$A \Rightarrow B$
B

Possibly A

Induction: case: These balls are from the box
observation: These balls are black
hypothesized rule: All ball in the box are black

Whenever A then B

Possibly $A \Rightarrow B$

Deduction reasons from causes to effects

Abduction reasons from effects to causes

Induction reasons from specific cases to general rules

Characteristics of abductive reasoning

- *Conclusions* are **hypotheses**, not theorems (may be false *even if* rules and facts are true)
 - E.g., misdiagnosis in medicine
- There may be multiple plausible hypotheses
 - Given rules $A \Rightarrow B$ and $C \Rightarrow B$, and fact B , both A and C are plausible hypotheses
 - Abduction is inherently uncertain
 - Hypotheses can be ranked by their plausibility (if it can be determined)

Reasoning as a hypothesize-and-test cycle

- **Hypothesize**: Postulate possible hypotheses, any of which would explain the given facts (or at least most of the important facts)
- **Test**: Test the plausibility of all or some of these hypotheses
- One way to test a hypothesis H is to ask whether something that is currently unknown—but can be predicted from H —is actually true
 - If we also know $A \Rightarrow D$ and $C \Rightarrow E$, then ask if D and E are true
 - If D is true and E is false, then hypothesis A becomes more plausible (**support** for A is increased; **support** for C is decreased)

Non-monotonic reasoning

- Abduction is a *non-monotonic* reasoning process
- In a monotonic reasoning system, your knowledge can only increase
 - Propositions don't change their truth value
 - You never unknow things
- In abduction, the plausibility of hypotheses can increase/decrease as new facts are collected
- In contrast, deductive inference is **monotonic**: it never change a sentence's truth value, once known
- In abductive (and inductive) reasoning, some hypotheses may be discarded, and new ones formed, when new observations are made

Default logic

- Default logic is another kind of non-monotonic reasoning
- We know many facts which are mostly true, typically true, or true by default
 - E.g., birds can fly, dogs have four legs, etc.
- Sometimes these facts are wrong however
 - Ostriches are birds, but can not fly
 - A dead bird can not fly
 - Uruguay President José Mujica has a three-legged dog

Negation as Failure

- Prolog introduced the notion of *negation as failure*, which is widely used in logic programming languages and many KR systems
- Proving P in classical logic can have three outcomes: true, false, unknown
- Sometimes being unable to prove something can be used as evidence that it is not true
- This is typically the case in a database context
 - Is John registered for CMSC 671?
- If we don't find a record for John in the registrar's database, he is not registered

Default reasoning in Prolog

```
%% this is a simple example of default reasoning in Prolog
:- dynamic can_fly/1, neg/1, bird/1, penguin/1, eagle/1, dead/1, injured/1.
```

```
%% We'll use neg(P) to represent the logical negation of P.
```

```
%% The \+ operator in prolog can be read as 'unprovable'
```

```
% Assume birds can fly unless we know otherwise.
```

```
can_fly(X) :- bird(X), \+ neg(can_fly(X))
```

```
bird(X) :- eagle(X).
```

```
bird(X) :- owl(X).
```

```
bird(X) :- penguin(X).
```

```
neg(can_fly(X)) :- penguin(X).
```

```
neg(can_fly(X)) :- dead(X).
```

```
neg(can_fly(X)) :- injured(X).
```

```
% here are some individuals
```

```
penguin(chilly).
```

```
penguin(tux).
```

```
eagle(sam).
```

```
owl(hedwig).
```

Circumscription

- Another useful concept is being able to declare a predicate as ‘complete’ or circumscribed
 - If a predicate is complete, then the KB has all instances of it
 - This can be explicit (i.e., materialized as facts) or implicit (provable via a query)
- If a predicate, say `link(From,To)` is circumscribed then not being able to prove that `link(nyc,tampa)` means that `neg(link(nyc,tampa))` is true

Default Logic

- We have a standard model for first order logic
- There are several models for default reasoning
 - All have advantages and disadvantages, supporters and detractors
- None is completely accepted
- Default reasoning also shows up in object oriented systems
- And in epistemic reasoning (reasoning about what you know)
 - Does President Obama have a wooden leg?

Sources of Uncertainty

- Uncertain **inputs** -- missing and/or noisy data
- Uncertain **knowledge**
 - Multiple causes lead to multiple effects
 - Incomplete enumeration of conditions or effects
 - Incomplete knowledge of causality in the domain
 - Probabilistic/stochastic effects
- Uncertain **outputs**
 - Abduction and induction are inherently uncertain
 - Default reasoning, even deductive, is uncertain
 - Incomplete deductive inference may be uncertain
- ▶ Probabilistic reasoning only gives probabilistic results (summarizes uncertainty from various sources)

Decision making with uncertainty

Rational behavior:

- For each possible action, identify the possible outcomes
- Compute the **probability** of each outcome
- Compute the **utility** of each outcome
- Compute the probability-weighted **(expected) utility** over possible outcomes for each action
- Select action with the highest expected utility (principle of **Maximum Expected Utility**)

Bayesian reasoning

- We will look at using probability theory and Bayesian reasoning next time in some detail
- Bayesian inference
 - Use probability theory and information about independence
 - Reason diagnostically (from evidence (effects) to conclusions (causes)) or causally (from causes to effects)
- Bayesian networks
 - Compact representation of probability distribution over a set of propositional random variables
 - Take advantage of independence relationships

Other uncertainty representations

- Rule-based methods
 - Certainty factors (Mycin): propagate simple models of belief through causal or diagnostic rules
- Evidential reasoning
 - Dempster-Shafer theory: $\text{Bel}(P)$ is a measure of the evidence for P ; $\text{Bel}(\neg P)$ is a measure of the evidence against P ; together they define a belief interval (lower and upper bounds on confidence)
- Fuzzy reasoning
 - Fuzzy sets: How well does an object satisfy a vague property?
 - Fuzzy logic: “How true” is a logical statement?

Uncertainty tradeoffs

- **Bayesian networks:** Nice theoretical properties combined with efficient reasoning make BNs very popular; limited expressiveness, knowledge engineering challenges may limit uses
- **Nonmonotonic logic:** Represent commonsense reasoning, but can be computationally very expensive
- **Certainty factors:** Not semantically well founded
- **Dempster-Shafer theory:** Has nice formal properties, but can be computationally expensive, and intervals tend to grow towards $[0,1]$ (not a very useful conclusion)
- **Fuzzy reasoning:** Semantics are unclear (fuzzy!), but has proved very useful for commercial applications