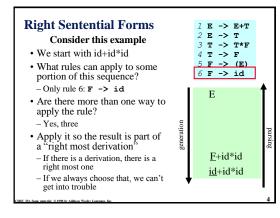
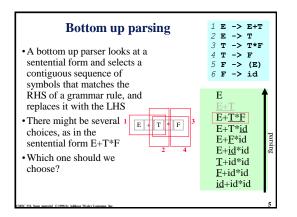
# 4d Bottom Up Parsing

## Motivation

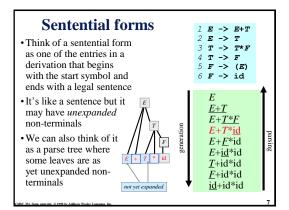
- In the last lecture we looked at a table driven, top-down parser
  - -A parser for LL(1) grammars
- In this lecture, we'll look a a table driven, bottom up parser
  - -A parser for LR(1) grammars
- In practice, bottom-up parsing algorithms are used more widely for a number of reasons

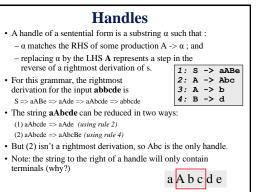
Right Sentential Forms		1 E -> E+T	
<ul> <li>Recall the definition of a derivation and a rightmost derivation</li> </ul>		2 E -> T 3 T -> T*F 4 T -> F 5 F -> (E) 6 F -> id	
• Each of the lines is a (right) sentential form	I	Е	4
• A form of the parsing problem is finding the correct RHS in a right- sentential form to reduce to get the previous right- sentential form in the derivation	generation	$\frac{\underline{E+T}}{\underline{E+T*F}}$ $\underline{E+T*id}$ $\underline{E+F*id}$ $\underline{E+id*id}$ $\underline{T+id*id}$ $\underline{F+id*id}$ $\underline{id+id*id}$	

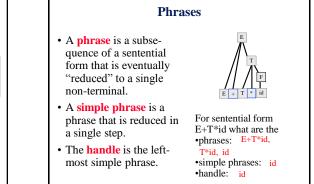




<b>Bottom up parsing</b> • If the wrong one is chosen, it leads to failure • E.g.: replacing E+T with E	1 E -> E+T 2 E -> T 3 T -> T*F 4 T -> F 5 F -> (E) 6 F -> id
in E+T*F yields E+F, which can't be further reduced using the given grammar	<i>error</i> E*F <u>E+T</u> *F
•The handle of a sentential form is the RHS that should be rewritten to yield the next sentential form in the right	$\begin{array}{c} E+T^*\underline{id} \\ E+\underline{F}^*\underline{id} \\ E+\underline{id}^*\underline{id} \\ \underline{T}+\underline{id}^*\underline{id} \\ F+\underline{id}^*\underline{id} \end{array}$
most derivation	<u>id</u> +id*id

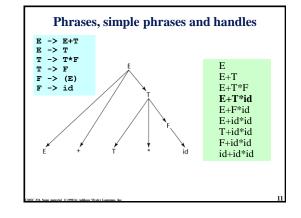






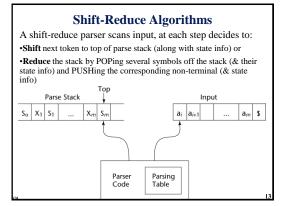
#### Phrases, simple phrases and handles

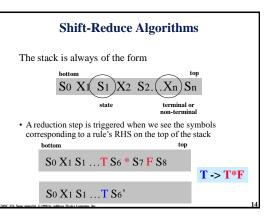
- **Def:**  $\beta$  is the *handle* of the right sentential form  $\gamma = \alpha\beta w$  if and only if  $S =>*rm \alpha Aw => \alpha\beta w$
- **Def:**  $\beta$  is a *phrase* of the right sentential form  $\gamma$  if and only if  $S = >^* \gamma = \alpha 1 A \alpha 2 = >+ \alpha 1 \beta \alpha 2$
- **Def:**  $\beta$  is a *simple phrase* of the right sentential form  $\gamma$  if and only if  $S =>^* \gamma = \alpha 1A\alpha 2 => \alpha 1\beta\alpha 2$
- The handle of a right sentential form is its leftmost simple phrase
- Given a parse tree, it is now easy to find the handle
- · Parsing can be thought of as handle pruning

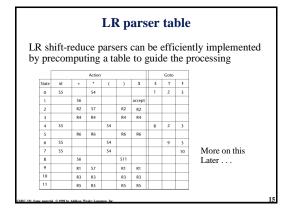


#### On to shift-reduce parsing

- How to do it w/o having a parse tree in front of us?
- Look at a shift-reduce parser the kind that yacc uses
- A shift-reduce parser has a queue of input tokens & an initially empty stack. It takes one of 4 possible actions:
- -Accept: if the input queue is empty and the start symbol is the only thing on the stack
- -**Reduce:** if there is a handle on the top of the stack, pop it off and replace it with the rule's RHS
- -Shift: push the next input token onto the stack
- -Fail: if the input is empty and we can't accept
- In general, we might have a choice of (1) shift, (2) reduce, or (3) maybe reducing using one of several rules
- The algorithm we next describe is deterministic

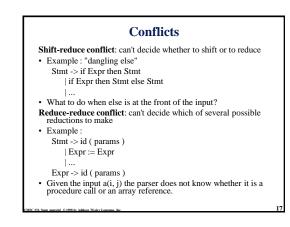






#### When to shift, when to reduce

- Key problem in building a shift-reduce parser is deciding whether to shift or to reduce
- repeat: reduce if a handle is on top of stack, shift otherwise
- Succeed if there is only S on the stack and no input
- A grammar may not be appropriate for a LR parser because there are <u>conflicts</u> which can not be resolved
- · Conflict occurs when the parser can't decide whether to:
- $-\operatorname{shift}$  or reduce the top of stack (a shift/reduce conflict), or
- reduce the top of stack using one of two possible productions (a reduce/reduce conflict)
- There are several varieties of LR parsers (LR(0), LR(1), SLR and LALR), with differences depending on amount of lookahead and on construction of the parse table



### LR Table

- An LR configuration stores the state of an LR parser (S<sub>0</sub>X<sub>1</sub>S<sub>1</sub>X<sub>2</sub>S<sub>2</sub>...X<sub>m</sub>S<sub>m</sub>, a<sub>i</sub>a<sub>i+1</sub>...a<sub>n</sub>\$)
- LR parsers are table driven, where the table has two components, an ACTION table and a GOTO table
- The ACTION table specifies the action of the parser (shift or reduce) given the parser state and next token
  - -Rows are state names; columns are terminals
- The GOTO table specifies which state to put on top of the parse stack after a reduce
  - -Rows are state names; columns are non-terminals

Г											
				Action					Goto		
						-				-	
	State	id	+	*	(	)	\$	E	T	F	
	0	\$5		S4				1	2	3	
	f in stat		S6				accept				
ic	i, then S		R2	S7		If in state					
a	nd go to	o state 5	R4	R4		no more i we are do					
	4	S5			<b>S4</b>			8	2	3	
	5		R6	R6		R6	R6				
		If in state 5 a is *, then RE			S4				9	3	
	7	6. Use goto t state to selec	able and	exposed	S4					10	
	8 L	state to selec	56	ie	1	S11				1: E -	> E+T
	9		R1	S7		R1	R1		1	2: E -	> т
	10		R3	R3		R3	R3			3: Т - 4: Т -	
	11		R5	R5		R5	R5			5: F - 6: F -	
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# **Parser actions**

Initial configuration: (S0, a1...an\$)

#### Parser actions:

1 If ACTION[S<sub>m</sub>, a<sub>i</sub>] = Shift S, the next configuration is:  $(S_0X_1S_1X_2S_2...X_mS_ma_iS, a_{i+1}...a_n)$ 2 If ACTION[S<sub>m</sub>, a<sub>i</sub>] = Reduce  $A \rightarrow \beta$  and  $S = GOTO[S_{m,r}, A]$ , where r = the length of  $\beta$ , the next configuration is

 $(S_00X_1S_1X_2S_2...X_{m-r}S_{m-r}AS, a_ia_{i+1}...a_n\$)$ 3 If ACTION[ $S_m$ ,  $a_i$ ] = Accept, the parse is complete and no errors were found

4 If ACTION[S<sub>m</sub>,  $a_i$ ] = Error, the parser calls an error-handling routine

Example $2: E \to T$ $3: T \to T \neq F$ $4: T \to F$ $5: F \to (E)$ $6: F \to id$					
Stack	Input	action			
0	Id + id * id \$	Shift 5			
0 id 5	+ id * id \$	Reduce 6 goto(0,F)			
0 F 3	+ id * id \$	Reduce 4 goto(0,T)			
0 т 2	+ id * id \$	Reduce 2 goto(0,E)			
0 E 1	+ id * id \$	Shift 6			
0 E 1 + 6	id * id \$	Shift 5			
0 E 1 + 6 id 5	* id \$	Reduce 6 goto (6, F)			
0 E 1 + 6 F 3	* id \$	Reduce 4 goto(6,T)			
0 E 1 + 6 T 9	* id \$	Shift 7			
0 E 1 + 6 T 9 * 7	id \$	Shift 5			
0 E 1 + 6 T 9 * 7 id 5	\$	Reduce 6 goto(7,E)			
0 E 1 + 6 T 9 * 7 F 10	\$	Reduce 3 goto(6,T)			
0 E 1 + 6 T 9	\$	Reduce 1 goto(0,E)			
0 E 1	\$	Accept			

	Action						Goto			
State	id	+	*	(	)	s	E	Т	F	
0	\$5		S4				1	2	3	
1		S6				accept				
2		R2	S7		R2	R2				
3		R4	R4		R4	R4				
4	\$5			S4			8	2	3	
5		R6	R6		R6	R6				
6	\$5			S4				9	3	
7	\$5			S4					10	
8		S6			S11					
9		R1	S7		R1	R1				
10		R3	R3		R3	R3				
11		R5	R5		R5	R5				

<ul> <li>Yacc as a LR parser</li> <li>The Unix yacc utility is just such a parser.</li> <li>It does the heavy lifting of computing the table</li> <li>To see the table information, use the -v flag when calling yacc, as in yacc -v test.y</li> <li>To see the table information of the set o</li></ul>	)' . E \$end (0) ft 2 E ')' (5) t 1
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