### **PROGRAMMING IN HASKELL**



### Chapter 4 - Defining Functions

## **Conditional Expressions**

As in most programming languages, functions can be defined using <u>conditional</u> <u>expressions</u>.

> abs :: Int  $\rightarrow$  Int abs n = if n  $\geq$  0 then n else -n

abs takes an integer n and returns n if it is non-negative and -n otherwise. Conditional expressions can be nested:

signum :: Int  $\rightarrow$  Int signum n = if n < 0 then -1 else if n == 0 then 0 else 1

### Note:

In Haskell, conditional expressions must have an else branch, which avoids any possible ambiguity problems with nested conditionals.

## **Guarded Equations**

As an alternative to conditionals, functions can also be defined using <u>guarded</u> <u>equations</u>.



As previously, but using guarded equations.

Guarded equations can be used to make definitions involving multiple conditions easier to read:

> signum n | n < 0 = -1 | n == 0 = 0 | otherwise = 1

### Note:

The catch all condition <u>otherwise</u> is defined in the prelude by otherwise = True.

### Pattern Matching

Many functions have a particularly clear definition using <u>pattern matching</u> on their arguments.

not :: Bool  $\rightarrow$  Bool not False = True not True = False

not maps False to True, and True to False.

Functions can often be defined in many different ways using pattern matching. For example

(&&):: Bool  $\rightarrow$  Bool  $\rightarrow$  BoolTrue && True = TrueTrue && False = FalseFalse && True = FalseFalse && False = False

can be defined more compactly by

True && True = True && = False However, the following definition is more efficient, because it avoids evaluating the second argument if the first argument is False:

> True && b = bFalse && = False

Note:

The underscore symbol \_ is a <u>wildcard</u> pattern that matches any argument value. Patterns are matched <u>in order</u>. For example, the following definition always returns False:

Patterns may not <u>repeat</u> variables. For example, the following definition gives an error:

> b && b = b&& = False

### List Patterns

Internally, every non-empty list is constructed by repeated use of an operator (:) called "<u>cons</u>" that adds an element to the start of a list.

# Functions on lists can be defined using <u>x:xs</u> patterns.

head ::  $[a] \rightarrow a$ head (x:\_) = x tail ::  $[a] \rightarrow [a]$ tail (\_:xs) = xs

head and tail map any non-empty list to its first and remaining elements.



x:xs patterns only match <u>non-empty</u> lists:

> head [] Error

 x:xs patterns must be <u>parenthesised</u>, because application has priority over (:).
For example, the following definition gives an error:

head 
$$x: = x$$

## **Integer Patterns**

As in mathematics, functions on integers can be defined using n+k patterns, where n is an integer variable and k>0 is an integer constant.

> pred ::  $Int \rightarrow Int$ pred (n+1) = n

pred maps any positive integer to its predecessor.



□ n+k patterns only match integers  $\geq k$ .

> pred 0 Error

 n+k patterns must be <u>parenthesised</u>, because application has priority over +.
For example, the following definition gives an error:

pred n+1 = n

### Lambda Expressions

Functions can be constructed without naming the functions by using <u>lambda</u> <u>expressions</u>.

 $\lambda x \rightarrow x + x$ 

the nameless function that takes a number x and returns the result x+x.

### Note:

The symbol λ is the Greek letter lambda, and is typed at the keyboard as a backslash \.

In mathematics, nameless functions are usually denoted using the [symbol, as in x ] x+x.

In Haskell, the  $\lambda$  symbol comes from the <u>lambda calculus</u>, the theory of functions on which Haskell is based.

# Why Are Lambdas Useful?

Lambda expressions can be used to give a formal meaning to functions defined using <u>currying</u>.

For example:

add x y = x+y

#### means

add =  $\lambda x \rightarrow (\lambda y \rightarrow x+y)$ 

Lambda expressions are also useful when defining functions that return <u>functions as</u> <u>results</u>.

For example:

const ::  $a \rightarrow b \rightarrow a$ const x \_ = x

is more naturally defined by

const :: a  $\rightarrow$  (b  $\rightarrow$  a) const x =  $\lambda_{-} \rightarrow$  x Lambda expressions can be used to avoid naming functions that are only <u>referenced</u> once.

For example:

odds n = map f [0..n-1] where f x = x\*2 + 1

can be simplified to

odds n = map ( $\lambda x \rightarrow x^*2 + 1$ ) [0..n-1]



An operator written <u>between</u> its two arguments can be converted into a curried function written <u>before</u> its two arguments by using parentheses.

For example:

This convention also allows one of the arguments of the operator to be included in the parentheses.

For example:

> (1+) 2 3 > (+2) 1 3

In general, if  $\oplus$  is an operator then functions of the form ( $\oplus$ ), (x $\oplus$ ) and ( $\oplus$ y) are called <u>sections</u>.

# Why Are Sections Useful?

Useful functions can sometimes be constructed in a simple way using sections. For example:

- (1+) successor function
  - (1/) reciprocation function
- (\*2) doubling function
- (/2) halving function

### Exercises

(1) Consider a function <u>safetail</u> that behaves in the same way as tail, except that safetail maps the empty list to the empty list, whereas tail gives an error in this case. Define safetail using:

(a) a conditional expression;(b) guarded equations;(c) pattern matching.

Hint: the library function null ::  $[a] \rightarrow Bool can be used to test if a list is empty.$ 

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Give three possible definitions for the logical or operator (||) using pattern matching.

(3) Redefine the following version of (&&) using conditionals rather than patterns:

True && True = True && = False

(4) Do the same for the following version:

True && b = bFalse && = False